

Solutions to Quiz # 5 for Dr. Z.'s Number Theory

1. (5 points) Using divisibility tests, determine whether 517286 is divisible by 11.

Sol. of 1: We take the *alternating sum*

$$5 - 1 + 7 - 2 + 8 - 6 \pmod{11} = 4 + 5 + 2 \pmod{11} = 11 \pmod{11} = 0 \quad .$$

So it is divisible by 11.

2. (5 points) What is the day of the week of Halloween 2100.

Sol. of 2: This year Oct. 31 is Thurs. so it is Day 5.

Oct. 31, 2100 will happen in $2100 - 2024 = 76$ years. There are $(2096 - 2024)/4 = 18$ leap days (Feb, 29) until then. Note that 2100 itself is **not** a leap year, since it is a multiple of 100 (and not a multiple of 400).

So we have

$$5 + 76 + 18 \pmod{7} = 5 + 6 + 4 \pmod{7} = 1 \pmod{7} \quad .$$

Ans. to 2: Sunday.