

Experimenting with the Garsia-Milne Involution Principle

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In memory of Adriano M. Garsia (1928-2024) and in honor of Stephen C. Milne on his 75th birthday

Abstract: We use symbolic computation to find explicit expressions for the average, variance, and many higher moments, for the complexity of mappings produced by the amazing Garsia-Milne Involution Principle.

References

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Jan. 25, 2025