

"QUIZ" for Lecture 11

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E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q11FirstLast.pdf) ASAP BUT NO LATER THAN Oct. 12, 8:00pm Deadline extended to Oct. 17

1. Use Lagrange multipliers (no credit for other methods) to find the **smallest** value that  $x + y + z$  can be, given that  $xyz = 125$

$$\begin{aligned} \nabla f &= \langle 1, 1, 1 \rangle & \lambda \nabla f &= \nabla g \\ \nabla g &= \langle yz, xz, xy \rangle & \lambda \langle 1, 1, 1 \rangle &= \langle yz, xz, xy \rangle \\ & & \lambda = yz & \lambda = xz & \lambda = xy \\ & & y = \frac{\lambda}{z} & z = \frac{\lambda}{x} & x = \frac{\lambda}{y} \\ xyz &= \frac{\lambda^3}{xyz} & \lambda^3 &= 125 & \lambda = 5 \\ y &= \frac{1}{2} & z &= \frac{1}{x} & x = \frac{1}{y} \\ y &= x & z &= y & x = z \\ x &= y = z & \rightarrow & x = y = z = 5 \\ x^3 &= 125 \\ x &= 5 \end{aligned}$$

$$f(5, 5, 5) = 5 + 5 + 5 = \boxed{15}$$

2. Use Lagrange multipliers (no credit for other methods) to find the **largest** value that  $xyz$  can be, given that  $x + y + z = 15$

$$\begin{aligned} \nabla f &= \langle yz, xz, xy \rangle & \nabla f &= \lambda \nabla g \\ \nabla g &= \langle 1, 1, 1 \rangle & \langle yz, xz, xy \rangle &= \lambda \langle 1, 1, 1 \rangle \\ & & yz &= \lambda & xz &= \lambda & xy &= \lambda \\ & & y &= \frac{\lambda}{z} & z &= \frac{\lambda}{x} & x &= \frac{\lambda}{y} \\ xyz &= \frac{\lambda^3}{xyz} \\ 1 &= \frac{\lambda^3}{125} \\ \lambda &= 5 \\ y &= \frac{1}{2} & z &= \frac{1}{x} & x &= \frac{1}{y} \\ x &= y = z \\ 3x &= 15 \\ x &= 5 \end{aligned}$$

$$f(5, 5, 5) = \boxed{125}$$