

**“QUIZ” for Lecture 10**

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**E-MAIL SCANNED .pdf OF COMPLETED QUIZ to DrZcalc3@gmail.com (Attachment: q10FirstLast.pdf) ASAP BUT NO LATER THAN Oct. 8, 8:00pm**

1. Find the local maximum and minimum point(s), the local maximum and minimum values, and saddle point(s) of the function

$$f(x, y) = 12x^2 - 4x^3 + 6y^2 + 12xy \quad .$$

$$f_x = 24x - 12x^2 + 12y$$

$$f_y = 12y + 12x$$

$$f_{xx} = 24 - 24x$$

$$f_{xy} = 12$$

$$f_{yy} = 12$$

$$24x - 12x^2 + 12y = 0 \quad 12x - x^2 + y = 0 \quad 12y + 12x = 0 \quad x + y = 0 \quad y = -x$$

$$x_1 = 11 \quad x_2 = 0 \quad x + y = 0 \quad y_1 = -11 \quad y_2 = 0$$

$$(11, -11) \quad (0, 0)$$

$$f_{xx}(11, -11) = -240$$

$$f_{xy}(11, -11) = 12$$

$$f_{yy}(11, -11) = 12$$

$$D = -240 \cdot 12 - 12^2 = -3024 \text{ is negative,}$$

this is a saddle point.

$$f_{xx}(0, 0) = 24$$

$$f_{xy}(0, 0) = 12$$

$$f_{yy}(0, 0) = 12$$

$$D = 24 \cdot 12 - 12^2 = 144$$

$D > 0$   $f_{xx} > 0$  is a local minimum and the local minimum value is  $f(0, 0) = 0$