

Homework due 9/27

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Sec. 13.3

$$3) r'(t) = \left\langle 2, \frac{1}{t}, 2t \right\rangle$$

$$|r'(t)| = \sqrt{\frac{(2t^2+1)^2}{t^2}}$$

$$\int_1^4 \sqrt{\frac{(2t^2+1)^2}{t^2}} = 15 + 2\ln(2)$$

$$9) r'(t) = \left\langle 2t, 4t, 3t^2 \right\rangle$$

$$|r'(t)| = \sqrt{t^2(9t^2+20)}$$

$$s(t) = \int_0^t \sqrt{t^2(9t^2+20)} = \frac{(9t^2+20)^{3/2} - 8 \cdot 5^{3/2}}{27}$$

$$11) \mathbf{r}'(t) = \langle 2, 4, -1 \rangle$$

$$S(4) = |\mathbf{r}'(4)| = \sqrt{21}$$

$$13) \mathbf{r}'(t) = \left\langle 1, \frac{1}{t}, \frac{2 \ln(t)}{t} \right\rangle$$

$$S(1) = |\mathbf{r}'(1)| = \sqrt{2}$$

$$15) \mathbf{r}'(t) = \langle 3 \cos(3t), -4 \sin(4t), -5 \sin(5t) \rangle$$

$$S\left(\frac{\pi}{2}\right) = |\mathbf{r}'\left(\frac{\pi}{2}\right)| = 5$$

Sec. 13.4

$$1) \mathbf{r}'(t) = \langle 8t, 9 \rangle$$

$$\mathbf{T}(t) = \left\langle \frac{8t}{\sqrt{64t^2+81}}, \frac{9}{\sqrt{64t^2+81}} \right\rangle$$

$$\mathbf{T}(1) = \left\langle \frac{8}{\sqrt{145}}, \frac{9}{\sqrt{145}} \right\rangle$$

$$5) \mathbf{r}'(t) = \langle -\pi \sin(\pi t), \pi \cos(\pi t), 1 \rangle$$

$$\mathbf{T}(t) = \left\langle \frac{-\pi \sin(\pi t)}{\sqrt{\pi^2+1}}, \frac{\pi \cos(\pi t)}{\sqrt{\pi^2+1}}, \frac{1}{\sqrt{\pi^2+1}} \right\rangle$$

$$T(1) = \left\langle 0, -\frac{\pi}{\sqrt{\pi^2+1}}, \frac{1}{\sqrt{\pi^2+1}} \right\rangle$$

$$7) r'(t) = \langle 0, e^t, 1 \rangle$$

$$r''(t) = \langle 0, e^t, 0 \rangle$$

$$K(t) = \frac{|r'(t) \times r''(t)|}{|r'(t)|^3} = \frac{e^t}{(e^{2t} + 1)^{3/2}}$$

$$11) r'(t) = \left\langle -\frac{1}{t^2}, -\frac{2}{t^3}, 2t \right\rangle$$

$$r''(t) = \left\langle \frac{2}{t^3}, \frac{6}{t^4}, 2 \right\rangle$$

$$r'(-1) = \langle -1, 2, -2 \rangle$$

$$r''(-1) = \langle -2, 6, 2 \rangle$$

$$K(1) = \frac{|r'(1) \times r''(1)|}{|r'(1)|^3} = \frac{\sqrt{296}}{27}$$

$$17) y' = 4t^3 \quad y'' = 12t^2$$

$$y'(2) = 32 \quad y''(2) = 48$$

$$K(2) = \frac{|y''(2)|}{(1 + y'(2)^2)^{3/2}} = \frac{48}{1025^{3/2}}$$

$$21) \quad r'(t) = \langle \tanh(t)^2, -\operatorname{sech}(t) \cdot \tanh(t) \rangle$$

$$r''(t) = \left\langle \frac{2 \sinh(t)}{\cosh(t)^3}, \frac{\cosh(t)^2 - 2}{\cosh(t)^3} \right\rangle$$

$$K(t) = \frac{|r'(t) \times r''(t)|}{|r'(t)|^3} = \frac{\frac{1}{\cosh(t)}}{\sqrt{\frac{\sinh(t)^2}{\cosh(t)^2}}}$$

$$K(t) = \frac{1}{\sinh(t)} = \operatorname{csch}(t)$$

Sec. 13.5

$$3) \quad v(t) = \langle 3t^2, -1, 8t \rangle \quad v(1) = \langle 3, -1, 8 \rangle$$

$$a(t) = \langle 6t, 0, 8 \rangle \quad a(1) = \langle 6, 0, 8 \rangle$$

$$s(t) = \sqrt{9t^4 + 64t^2 + 1} \quad s(1) = \sqrt{74}$$

$$5) \quad v(t) = \langle \cos \theta, -\sin \theta, -3 \sin(3\theta) \rangle \quad v\left(\frac{\pi}{3}\right) = \left\langle \frac{1}{2}, -\frac{\sqrt{3}}{2}, 0 \right\rangle$$

$$a(t) = \langle -\sin \theta, -\cos \theta, -9 \cos(3\theta) \rangle \quad a\left(\frac{\pi}{3}\right) = \left\langle -\frac{\sqrt{3}}{2}, -\frac{1}{2}, 9 \right\rangle$$

$$s(t) = \sqrt{\cos^2 \theta + \sin^2 \theta + 9 \sin^2(3\theta)} \quad s\left(\frac{\pi}{3}\right) = 1$$

$$15) \quad V(t) = \left\langle \frac{t^2}{2} + C_x, 4t + C_y \right\rangle$$

$$\frac{0}{2} + C_x = 3$$

$$0 + C_y = -2$$

$$C_x = 3$$

$$C_y = -2$$

$$V(t) = \left\langle \frac{t^2}{2} + 3, 4t - 2 \right\rangle$$

$$r(t) = \left\langle \frac{t^3}{6} + 3t + C_x, 2t^2 - 2t + C_y \right\rangle$$

$$0 - 0 + C_x = 0 \quad 0 + C_y = 0$$

$$C_x = 0 \quad C_y = 0$$

$$r(t) = \left\langle \frac{t^3}{6} + 3t, 2t^2 - 2t \right\rangle$$

$$17) \quad V(t) = \frac{t^2}{2} \cdot k + C \quad C = i$$

$$V(t) = \frac{t^2}{2} \cdot k + i$$

$$r(t) = \frac{t^3}{6} \cdot k + t \cdot i + C \quad C = j$$

$$r(t) = \frac{t^3}{6} \cdot k + t \cdot i + j$$

$$31) 2 \langle 2, 1, -3 \rangle \cdot \langle 12, 20, 20 \rangle = -32$$

Particle is slowing down

$$33) V(t) = \langle 1, -\sin(t), \cos(t) \rangle$$

$$\alpha(t) = \langle 0, -\cos(t), -\sin(t) \rangle$$

$$a_T(t) = 0 \quad a_N(t) = 1$$

Sec. 14.1

$$1) f(2, 2) = 2 + 2 \cdot 2^3 = 18$$

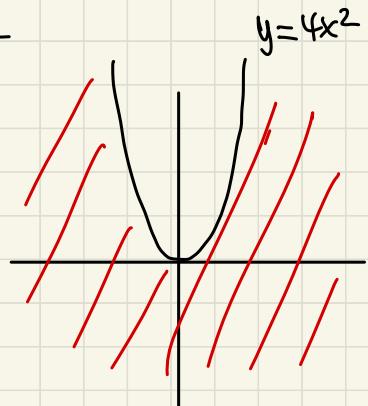
$$f(-1, 4) = -1 + 4(-1)^3 = -5$$

$$3) f(3, 8, 2) = \frac{3 \cdot 8}{4} = 6$$

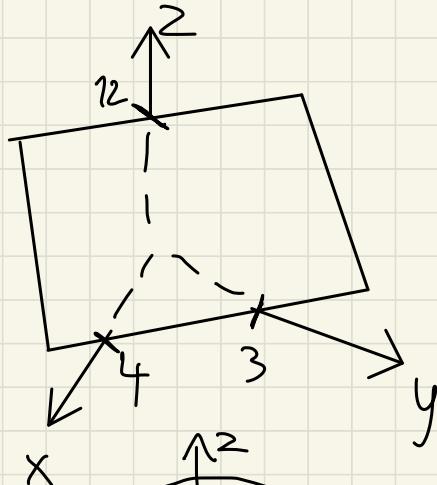
$$f(3, -2, -6) = \frac{3(-2)}{(-6)^2} = -\frac{1}{6}$$

$$7) \text{The domain is } 4x^2 - y > 0$$

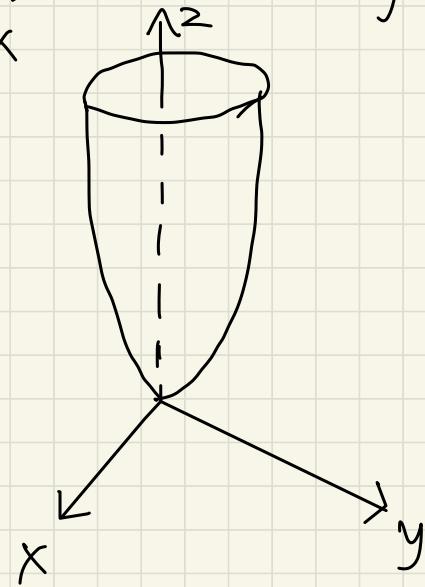
The domain is
the red region



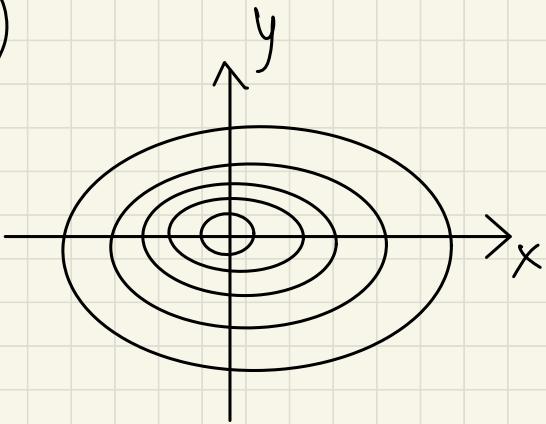
21)



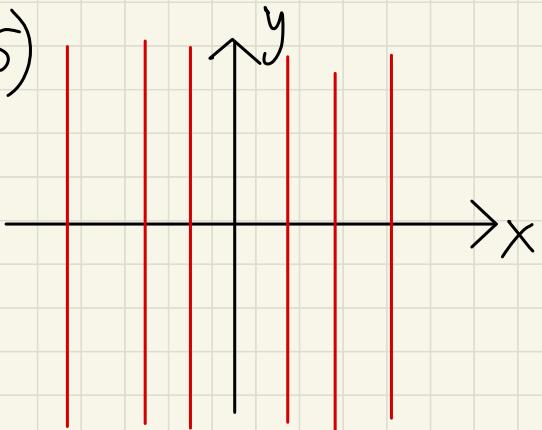
23)



33)



35)



37) For $m=6$, we have $f(x,y) = 2x+6y+6$

For $m=3$, $f(x,y) = x+3y+3$

Sec. 14.2

5) This problem is missing in the scan

$$75) \lim_{x \rightarrow 0} \frac{x^3 + (mx)^3}{x(mx)^2} = \lim_{x \rightarrow 0} \frac{x^3(1+m)}{m^3 x^3}$$

$$= \lim_{x \rightarrow 0} \frac{1+m}{m^3} = \frac{1+m}{m^3}$$

The limit depends on m , therefore it doesn't exist.

$$21) \lim_{x \rightarrow 0} \frac{x(mx)}{3x^2 + 2(mx)^2} = \lim_{x \rightarrow 0} \frac{mx^2}{x^2(3+2m^2)}$$

$$= \lim_{x \rightarrow 0} \frac{m}{3+2m^2} = \frac{m}{3+2m^2}$$

Limit doesn't exist

23) Along the x -axis we know $y=0, z=0$

$$\lim_{x \rightarrow 0} \frac{x}{x^2} = \lim_{x \rightarrow 0} \frac{1}{x} = \infty$$

27) Plugging in, this limit equals $-16e$

31) Plugging in, this limit equals $\frac{1}{5}$

35) Plugging in, this limit equals -48