

12.5

1. $x + 3y + 2z = 3$

5. $x = 3$

9. $x + y + z = 0$

11. **b, d**

13. $(9, -4, -11)$

15. $(3, -8, 11)$

17. $P = (2, -1, 4), Q = (1, 1, 1), R = (3, 1, -2)$

$$\overrightarrow{PQ} = (-1, 2, -3) \quad \overrightarrow{PR} = (1, 2, -6) \quad \overrightarrow{PQ} \times \overrightarrow{PR} = \begin{vmatrix} i & j & k \\ -1 & 2 & -3 \\ 1 & 2 & -6 \end{vmatrix} = -6i - 9j - 4k = (-6, -9, -4)$$

the equation of the plane is $-6 * (x - 1) - 9 * (y - 1) - 4 * (z - 1) = 0$

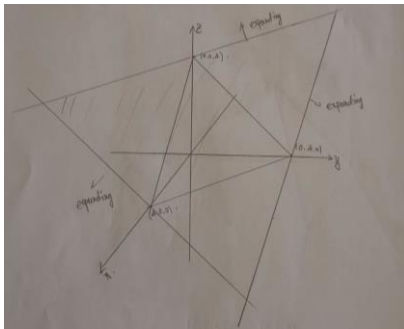
19. $P = (1, 0, 0) Q = (0, 1, 1) R = (2, 0, 1)$

$$\overrightarrow{PQ} = (-1, 1, 1) \quad \overrightarrow{PR} = (1, 0, 1) \quad \overrightarrow{PQ} \times \overrightarrow{PR} = \begin{vmatrix} i & j & k \\ -1 & 1 & 1 \\ 1 & 0 & 1 \end{vmatrix} = i + 2j - k = (1, 2, -1)$$

the equation of the plane is $(x - 1) + 2y - z = 0$

25. $(x + 2) + (z - 5) = 0, y \in R$

31.



53. the normal vector of xz - plane is $n_1 = (0, 1, 0)$

we assume that the other plane is $a * x + b * y + c * z = \alpha$

and the normal vector of the plan is $n_2 = (a, b, c)$

$$\text{the result of } n_1 \times n_2 = 0 \quad \begin{vmatrix} i & j & k \\ 0 & 1 & 0 \\ a & b & c \end{vmatrix} = c * i - a * k \text{ and we can know } \begin{cases} a = -2 \\ c = 3 \end{cases}$$

So, the equation of planes is:

$$(-2) * (x - 1) + b * y + 3 * (z - 1) = 0, b \text{ could be any real number}$$