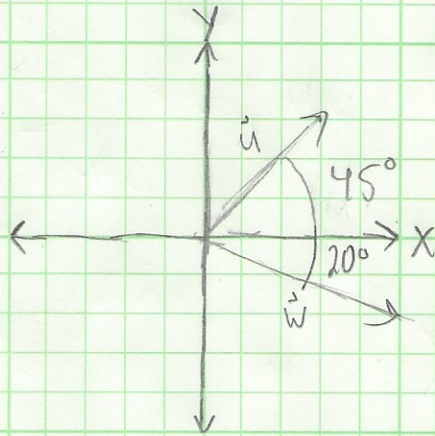


5 7 9 11 15
21 41 47

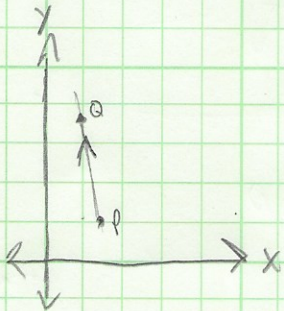
12.1 HW

Orion Kress Sanfilippo



$$5) \vec{u} = |\vec{u}| \left(\frac{\hat{i}}{\sqrt{2}} + \frac{\hat{j}}{\sqrt{2}} \right) \quad 7) \vec{w} = |\vec{w}| (\cos(20^\circ)\hat{i} - \sin(20^\circ)\hat{j})$$

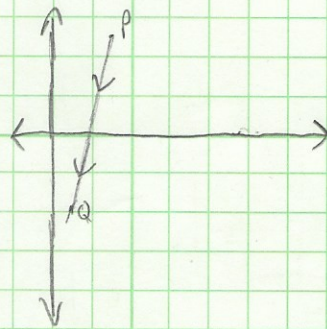
$$9) P = (3, 2) \quad Q = (2, 7) \quad |\vec{PQ}| = \sqrt{(2-3)^2 + (7-2)^2} = \sqrt{26} \quad \text{X Not Necessary}$$



$$\boxed{\vec{PQ} = -\hat{i} + 5\hat{j}} \quad \star$$

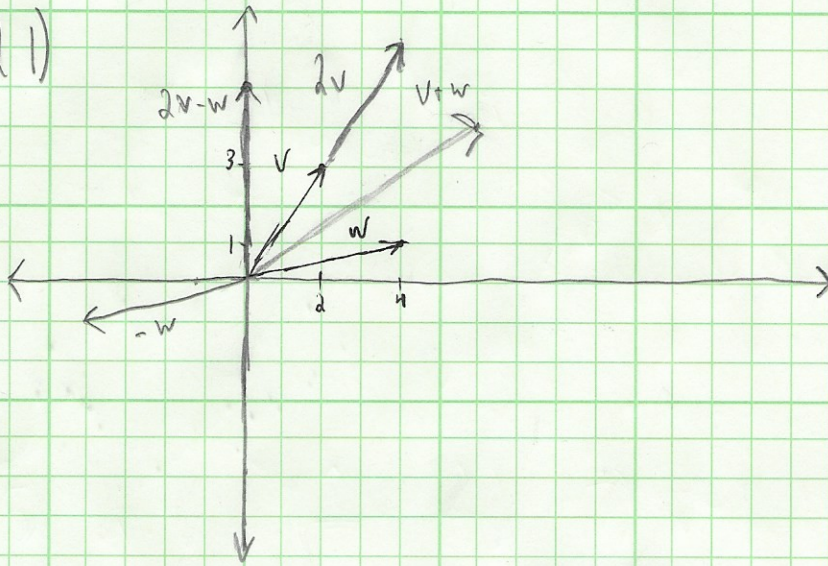
$$11) P = (3, 5) \quad Q = (1, -4)$$

$$\boxed{\vec{PQ} = -2\hat{i} - 9\hat{j}}$$



$$18) 5(6, 2) = (30, 10)$$

21)

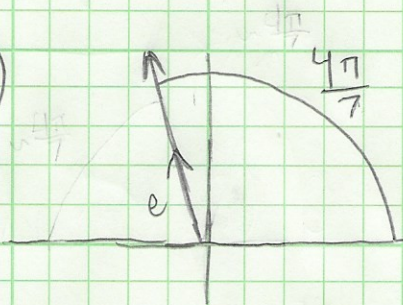


$$41) \quad e_v = \frac{\vec{v}}{|\vec{v}|} \quad |\vec{v}| = \sqrt{3^2 + 4^2} = 5$$

$$\vec{v} = 3\hat{i} + 4\hat{j}$$

$$e_v = \frac{3}{5}\hat{i} + \frac{4}{5}\hat{j}$$

47)

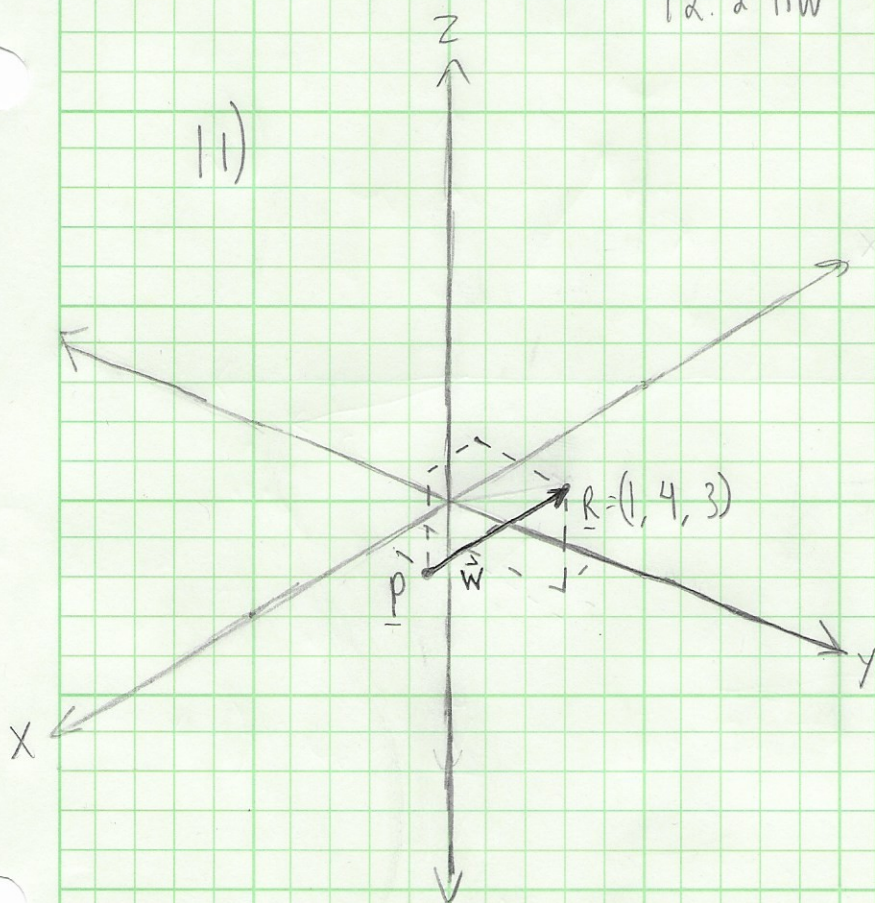


$$\hat{e} = \cos\left(\frac{4\pi}{7}\right)\hat{i} + \sin\left(\frac{4\pi}{7}\right)\hat{j}$$

Proof that this is a unit vector:

$$\cos^2(x) + \sin^2(x) = 1$$

11)



$$\text{If } \vec{w} = \vec{PR}, \quad -\vec{w} = \vec{RP}$$

$$\underline{R} \rightarrow \underline{P}$$

$$\underline{P} = (2, 1, 0)$$

$$13) \quad \vec{v} = (4, 8, 12)$$

a) $(2, 4, 6)$ is parallel to and points in the same dir. as \vec{v}

b) $(-1, -2, -3)$ is parallel to \vec{v} but does not pt. in the same dir.

c) $(-7, -14, -21)$ is parallel " " " " not pt. in the same dir.

d) $(6, 10, 14)$ is neither parallel nor pts in the same dir.

$$19) -2(8, 11, 3) + 4(2, 1, 1) =$$

$$(-16, -22, -6) + (8, 4, 4) =$$

$$(-8, -18, -2)$$

$$25) \vec{u} = (4, 2, -6) \quad \vec{v} = (2, -1, 3)$$

||?

Not parallel: y & z coords change magnitude

& sign consistently, but x does not

$$27) \vec{u} = (-3, 1, 4) \quad \vec{v} = (6, -2, 8)$$

Not parallel: vectors are not a scalar multiple
of each other

$$31) \quad \vec{v} = (-4, 4, 2) \quad \vec{u}_v = \left(\frac{\vec{v}}{|\vec{v}|} \right) \cdot (-1)$$

$$|\vec{v}| = \sqrt{(-4)^2 + (4)^2 + (2)^2} = \sqrt{32 + 4} = \sqrt{36} = 6$$

$$\vec{u}_v = \left(\frac{+2}{3}, \frac{-2}{3}, \frac{-1}{3} \right)$$

$$49) \quad r_1(t) = (5, 5, 2) + t(0, -2, 1) \quad (5, 5, 2) + t(0, -2, 1)$$

$$r_2(t) = (5, 1, 4) + t(0, 2, 1)$$

$$51) \quad r_1(t) = (-1, 2, 2) + t(4, -2, 1)$$

$$s_1(t) = (0, 1, 1) + t(2, 0, 1)$$

$$r_x(t) = -1 + 4t = s_x(p) = 2p$$

$$r_y(t) = 2 - 2t = s_y(p) = 1$$

$$r_z(t) = 2 + t = s_z(p) = 1 + p$$

$$\textcircled{1} \quad -1 + 4t = 2p$$

$$\textcircled{2} \quad 2 - 2t = 1$$

$$\textcircled{3} \quad 2 + t = 1 + p$$

$$\textcircled{2} + 2 \cdot \textcircled{3} \quad 2 - 4 + (-2t) + 2t = 1 + 2 + 2p \Rightarrow 4 = 1 + 2p \Rightarrow \boxed{\frac{3}{2} = p} \quad \textcircled{a}$$

$$\textcircled{1} - 2 \cdot \textcircled{2} \quad -1 - 3 + 4t = 0 \Rightarrow 4t = 4 \Rightarrow t = 1$$

$$\textcircled{1} \quad -1 + 4(1) = 2 \left(\frac{3}{2} \right) \quad \textcircled{2} \quad 2 - 2(1) = 1$$