

16.4.

$$7. T_u = \langle 2, 1, 3 \rangle$$

$$T_v = \langle 1, -4, 0 \rangle$$

$$N = T_u \times T_v = i(0+12) - j(0-3) + k(-8-1)$$

$$= 12i + 3j - 9k$$

$$= 3(4i + j - 3k)$$

$$4x + y - 3z = 4x(2+4) + (-16 - 3 \times 3) = 0$$

$$4x + y - 3z = 0$$

13.  ~~$T_u = \langle \cos v, \sin v, 1 \rangle$~~

~~$T_v = \langle -u \sin v, u \cos v, 0 \rangle$~~

~~$ds = |T_u \times T_v| du dv =$~~

~~$(u \cos v)^2 + (u \sin v)^2 = u^2$~~

~~$x^2 + y^2 = z^2$~~

~~$0 \leq v \leq \pi \quad 0 \leq \theta \leq 2\pi$~~

~~$\iint ds = \iint \sqrt{2} r dr d\theta$~~

$$ds = \sqrt{(\cos v)^2 + (\sin v)^2 + (-u \sin v)^2 + (u \cos v)^2} du dv$$

$$= \sqrt{2} u du dv$$

$$\int_0^1 \int_0^1 \sqrt{2} u^4 du dv = \frac{\sqrt{2}}{5}$$

15.  $G(u, v) = (u, 9-v^2, v)$

$$r_u = \langle 1, 0, 0 \rangle$$

$$r_v = \langle 0, -2v, 1 \rangle$$

$$ds = |r_u \times r_v| du dv = \sqrt{4v^2 + 1} du dv$$

$$\int_0^3 \int_0^3 \frac{1}{\sqrt{4v^2+1}} du dv$$
$$= \int_0^3 \left[ \frac{\sqrt{4v^2+1}}{12} \right]_0^3 dv$$
$$= \frac{3\sqrt{13}-1}{4}$$

19.  $G(u, v) = (2 \sin u, 2 \cos u, v)$

$$r_u = \langle 2 \cos u, -2 \sin u, 0 \rangle$$

$$r_v = \langle 0, 0, 1 \rangle$$

$$ds = \sqrt{4} du dv = 2 du dv$$

$$\int_0^4 \int_0^{2\pi} 2e^{-v} du dv$$

$$= [-4\pi e^{-v}]_0^4$$

$$= 4\pi(1 - e^{-4})$$

16.5.

5.  $g = 1 - 3x + 4y$

$$P = y \quad Q = 1 - 3x + 4y \quad R = x$$

$$\iint_S F \cdot ds = \iint_D (3y - 4z + x) dA$$

$$= \iint_D (13x - 13y - 4) dA$$

$$= \int_0^1 \int_0^1 (13x - 13y - 4) dx dy$$

$$\text{Inner: } \left[ \frac{13}{2}x - 13xy - 4x \right]_0^1 = \frac{5}{2} - 13y$$

$$\text{Outer: } \left[ \frac{5}{2}y - \frac{13}{2}y^2 \right]_0^1 = -4$$

7.  $g = \sqrt{9-x^2-y^2}$

$$\iint_S F \cdot ds = \int_0^3 \int_0^{\sqrt{9-x^2}} (3y(9-x^2-y^2)^{-\frac{1}{2}} + x) dy dx$$

$$= \frac{27}{4}\pi + 9$$



$$9. \quad g = 9 - x^2 - y^2.$$

$$P = z \quad Q = z \quad R = x.$$

$$\int_0^3 \int_0^{\sqrt{9-x^2}} [2(x+y)(9-x^2-y^2) + x] dy dx = \frac{673}{5}$$

$$11. \quad ~~z = 1-x-y~~ \quad g = 1-x-y.$$

$$P = y^2, \quad Q = 2, \quad R = -x.$$

$$\int_0^1 \int_0^{1-x} (y^2 + 2 - x) dy dx = \frac{11}{12}.$$

