

## 16.3

1.  $F = \langle y \sin(yz), x \sin(yz) + xyz \cos(yz), xy^2 \cos(yz) \rangle$

$$P_y = Q_x = \sin(yz) + yz \cos(yz)$$

$$P_z = R_x = y^2 \cos(yz)$$

$$Q_z = R_y = 2yz \cos(yz) - xy^2 z \sin(yz)$$

So,  $F$  is conservative and  $\int_C F dr = f(1,1,\pi) - f(0,0,0) = 0$

3.  $\nabla f = \langle f_x, f_y \rangle = \langle 3, 6y \rangle \int_C F dr = f(r(4)) - f(r(1)) = -\frac{9}{4}$

5.  $\nabla f = (f_x, f_y, f_z) = (ye^z, xe^z, xye^z) \int F dr = f(r(2)) - f(r(1)) = 32e - 1$

9.  $P_y = Q_x = 2y \quad P_z = R_x = 0 \quad R_z = Q_y = e^z$   
 $f = xy^2 + ye^z$

13.  $P_y = Q_x = 0 \quad P_z = R_x = \sec^2 x \quad R_z = Q_y = 1$

$$f = z \tan(x) + yz$$

15.  $P_y = Q_x = 2x \quad P_z = R_x = 0 \quad Q_z = R_y = -4$

$$f = x^2 y + 5x - 4yz$$

17.  $P_y = Q_x = 2xz \quad P_z = R_x = 2xy \quad Q_z = R_y = 0$ , the vector field is conservative

$$f = x^2 yz, \text{ the intergral equals } f(4,1,1) - f\left(0, \frac{\sqrt{2}}{2}, 1\right) = 16$$

19.  $f(1,1,0) - f(0,0,0) = 1$

$$\int F dr_1 = \int_0^1 3t^2 dt = 1$$

$$\int F dr_2 = \int_0^1 4t^3 dt = 1$$