

17.3

1. $\text{div}(F) = 0$.

$$\iiint_R 0 \, dV = 0.$$

3. $\text{div}(F) = 2$

$$\int_0^2 \int_{-1}^1 \int_{-\sqrt{1-y^2}}^{\sqrt{1-y^2}} 2 \, dx \, dy \, dz = 4\pi.$$

5. $\text{div}(F) = z^2$

$$\int_{-1}^1 \int_{-\sqrt{1-x^2}}^{\sqrt{1-x^2}} \int_{-\sqrt{1-x^2-y^2}}^{\sqrt{1-x^2-y^2}} z^2 \, dz \, dy \, dx = \frac{4}{15}\pi.$$

7. $\text{div}(F) = y^2 + z^2 + x^2$

$$\int_0^3 \int_{-2}^2 \int_{\sqrt{4-y^2}}^{\sqrt{4-y^2}} (x^2 + y^2 + z^2) \, dx \, dy \, dz = 60\pi$$

11. $\text{div}(F) = 3x^2 + 3z^2$

$$\int_0^2 \int_0^{\sqrt{4-y^2}} \int_0^{\sqrt{4-y^2-z^2}} (3x^2 + 3z^2) \, dx \, dz \, dy = \frac{32}{5}\pi$$

15. $\text{div}(F) = 1 + 1 = 2$

$$\int_{-3}^3 \int_{-\sqrt{9-x^2}}^{\sqrt{9-x^2}} \int_0^{\sqrt{9-x^2-y^2}} 2 \, dz \, dy \, dx = 81\pi.$$

