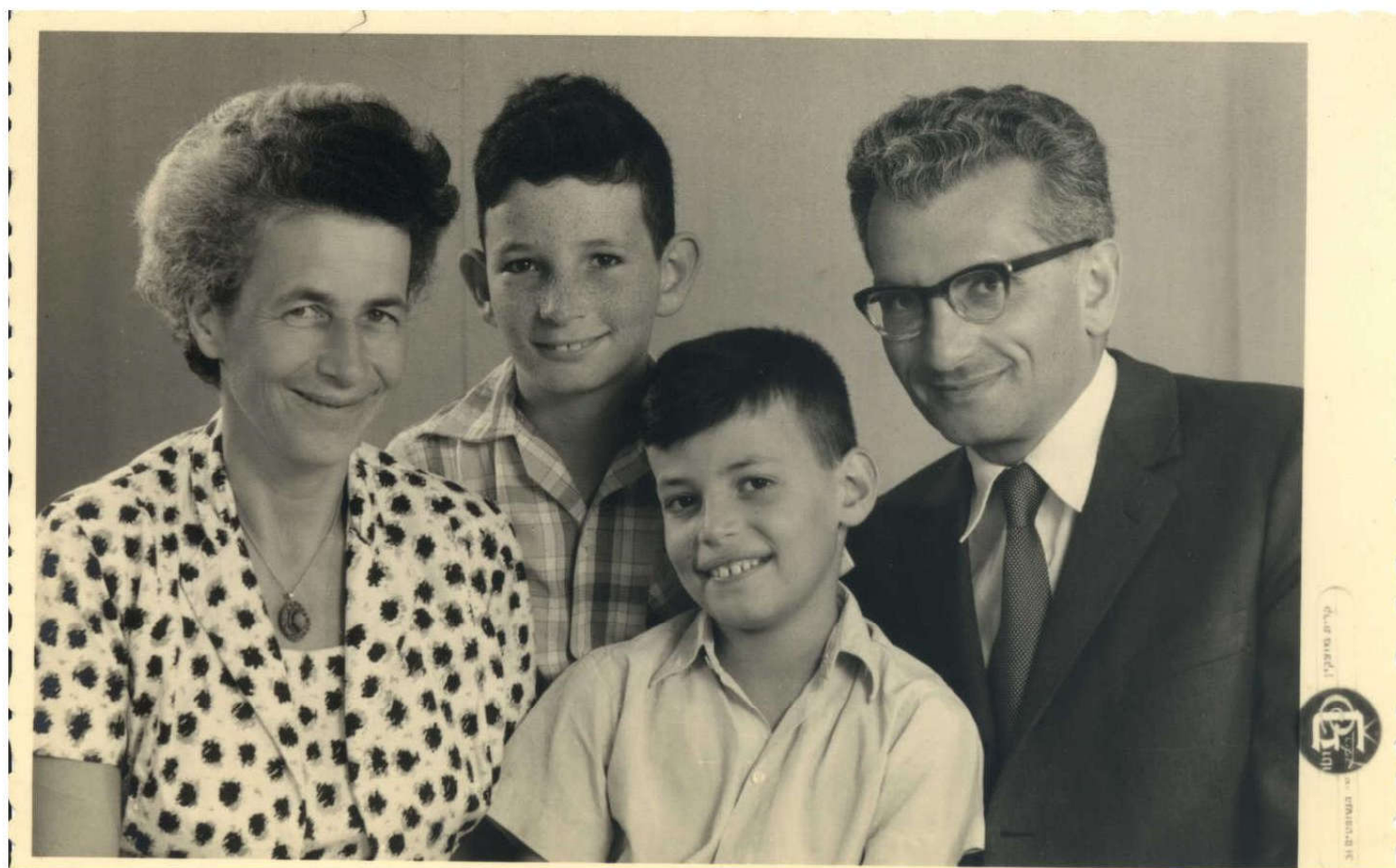


Honoring Doron

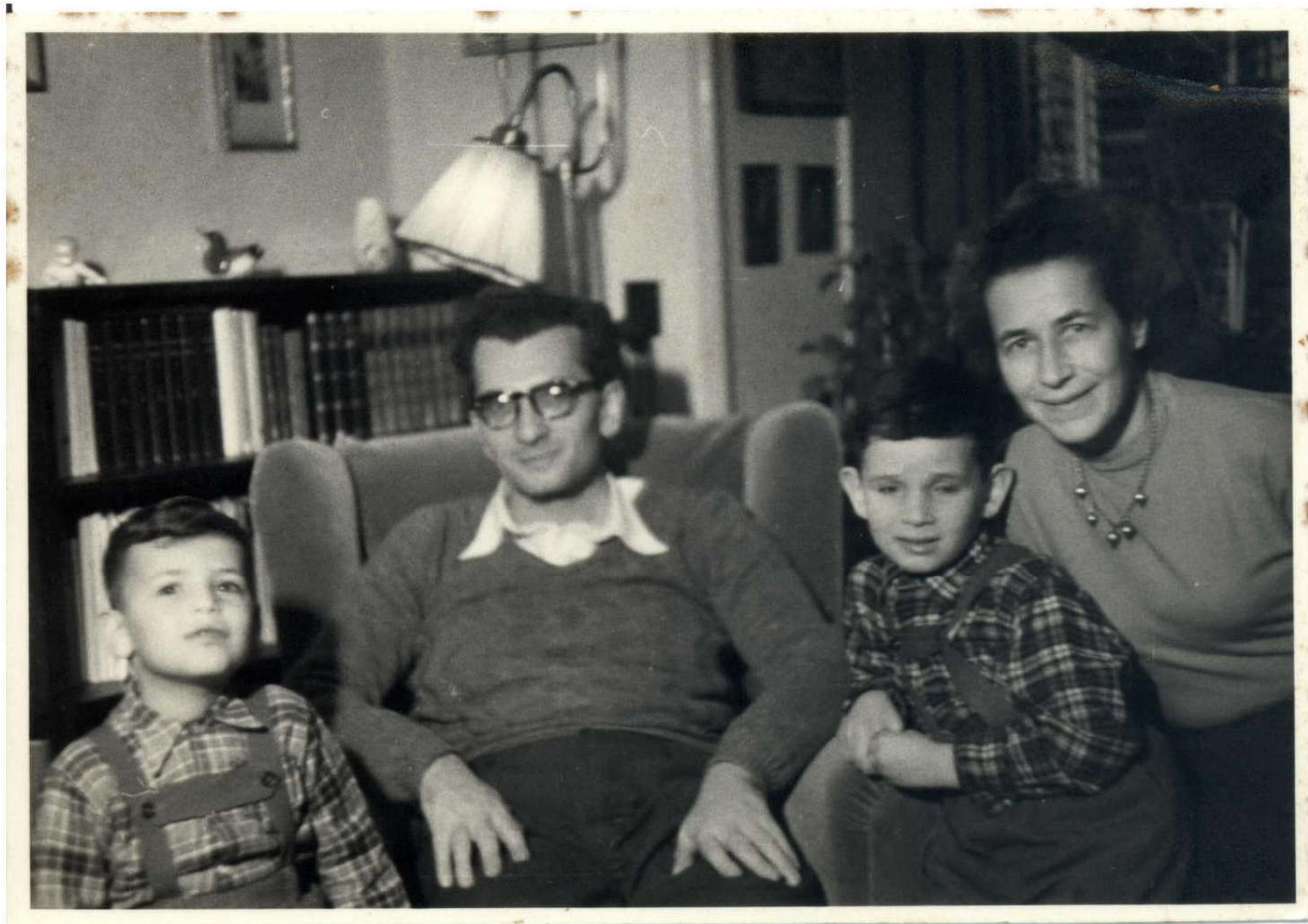
At his 70th Birthday



Beginnings













With Colleagues





JOINT
MATHEMATICS
MEETINGS
2010







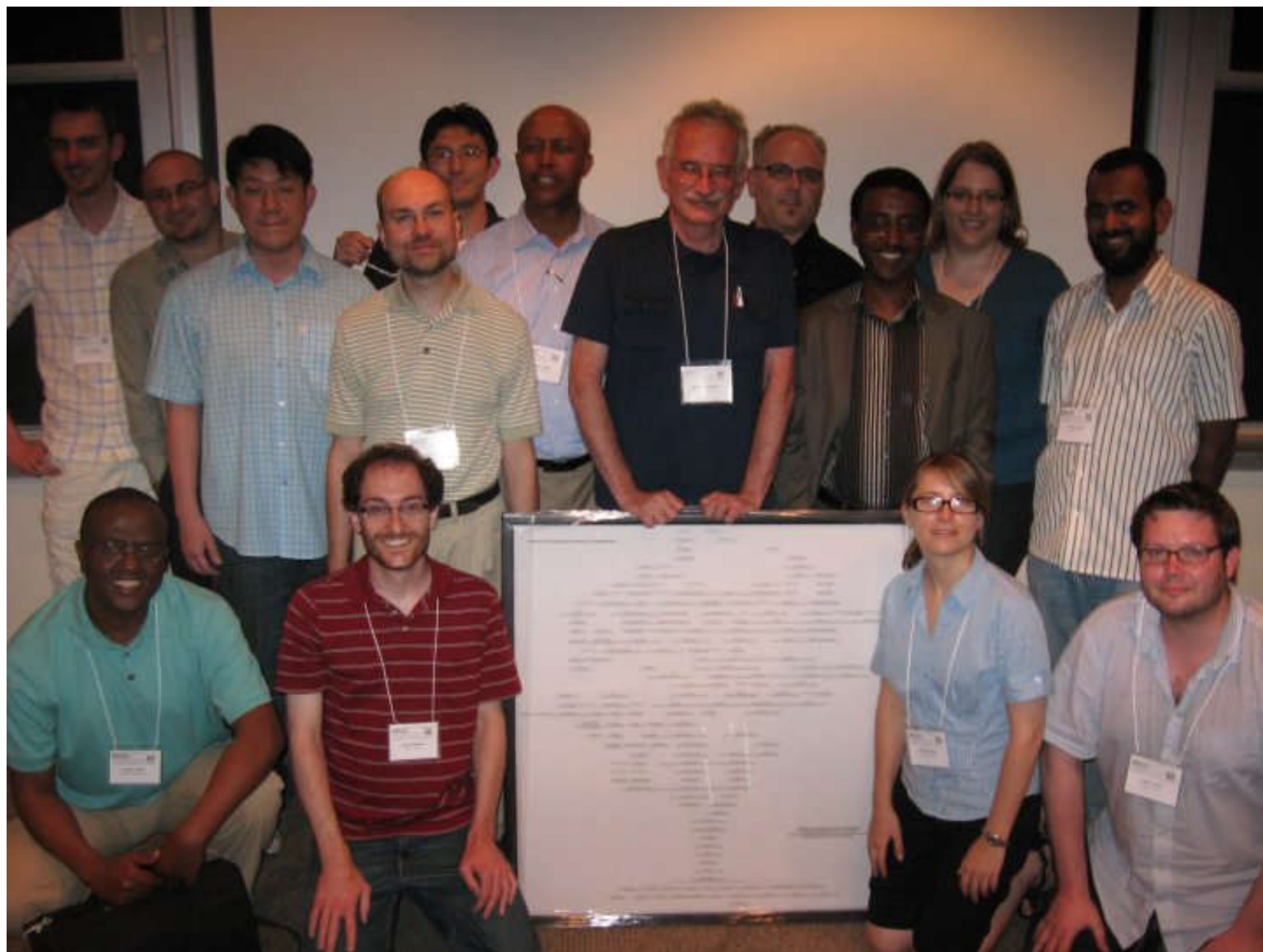














DZ Lectures



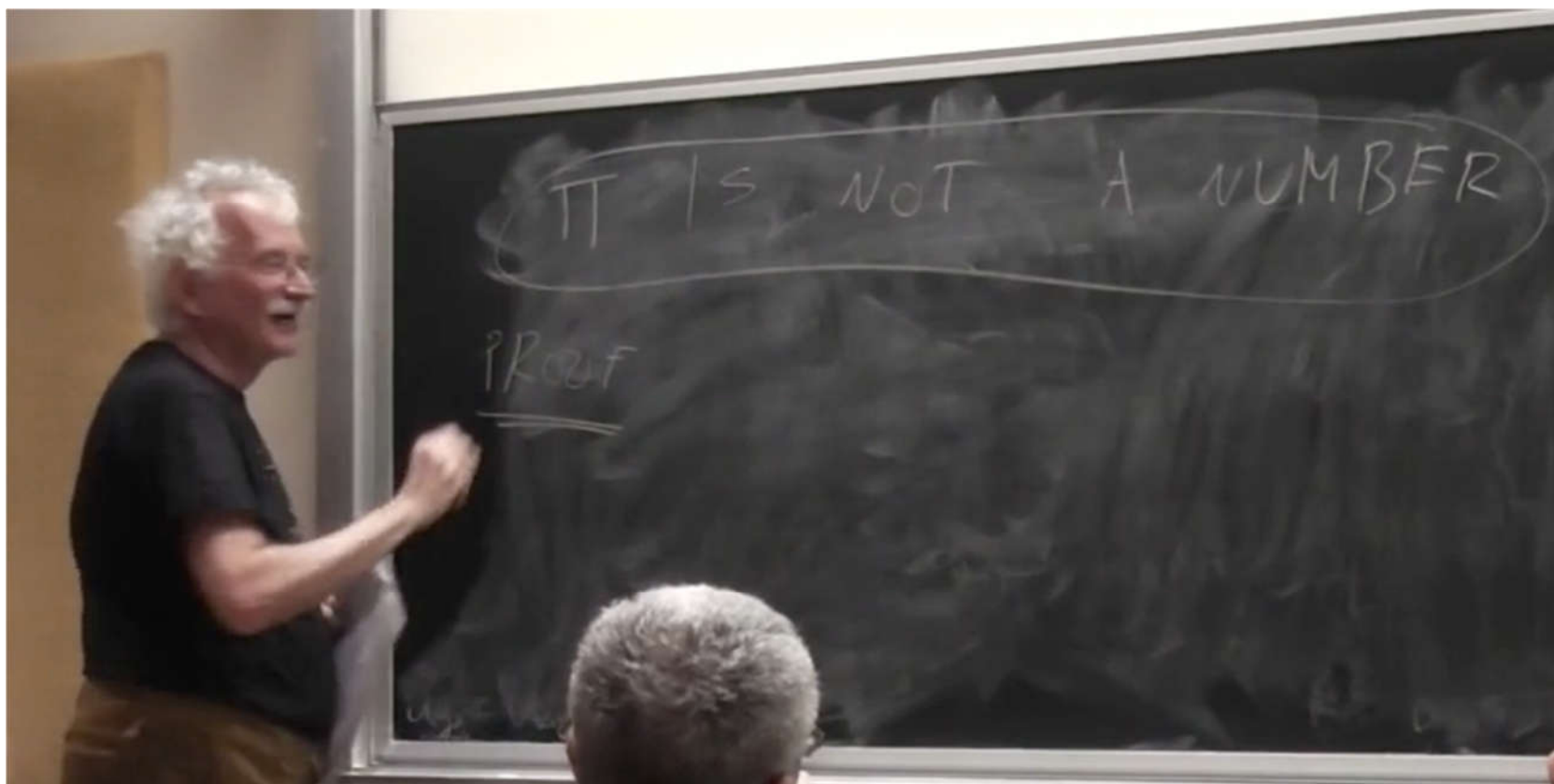
$$f(m, n) = 0$$

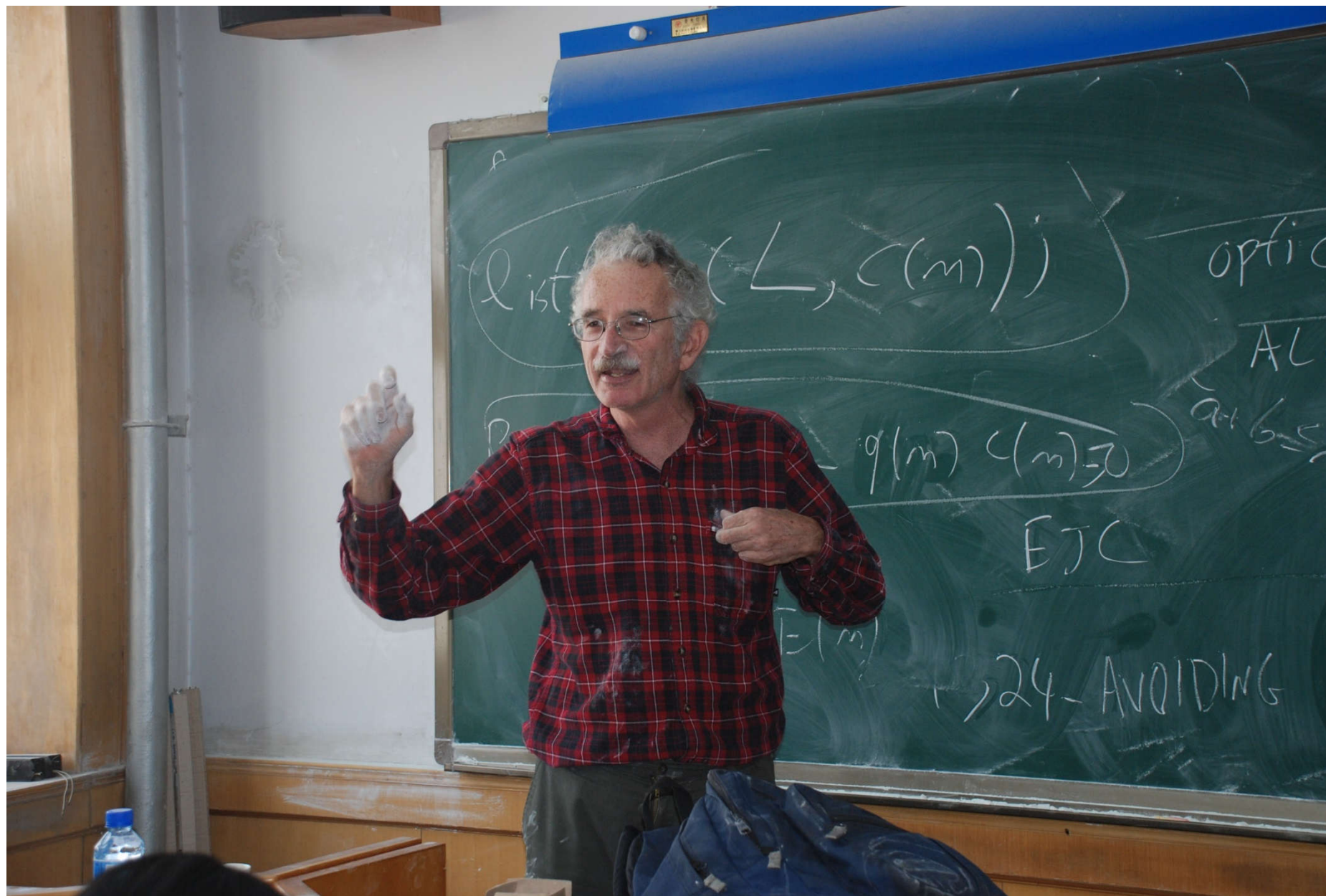
$$M f(m, n)$$

Doron Zeilberger
Rutgers University

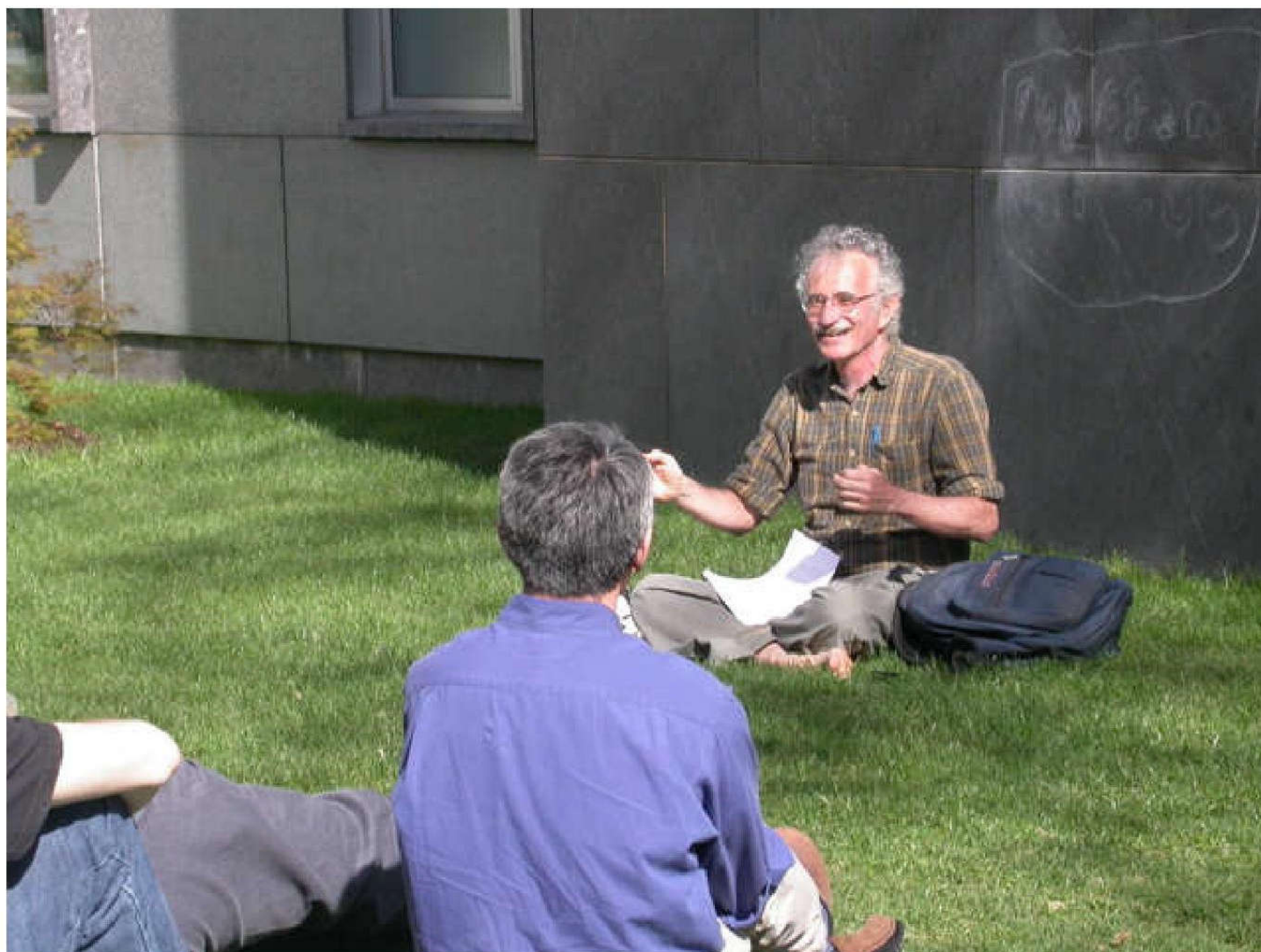
The Renaissance of Combinatorics: Advances — Algorithms — Applications

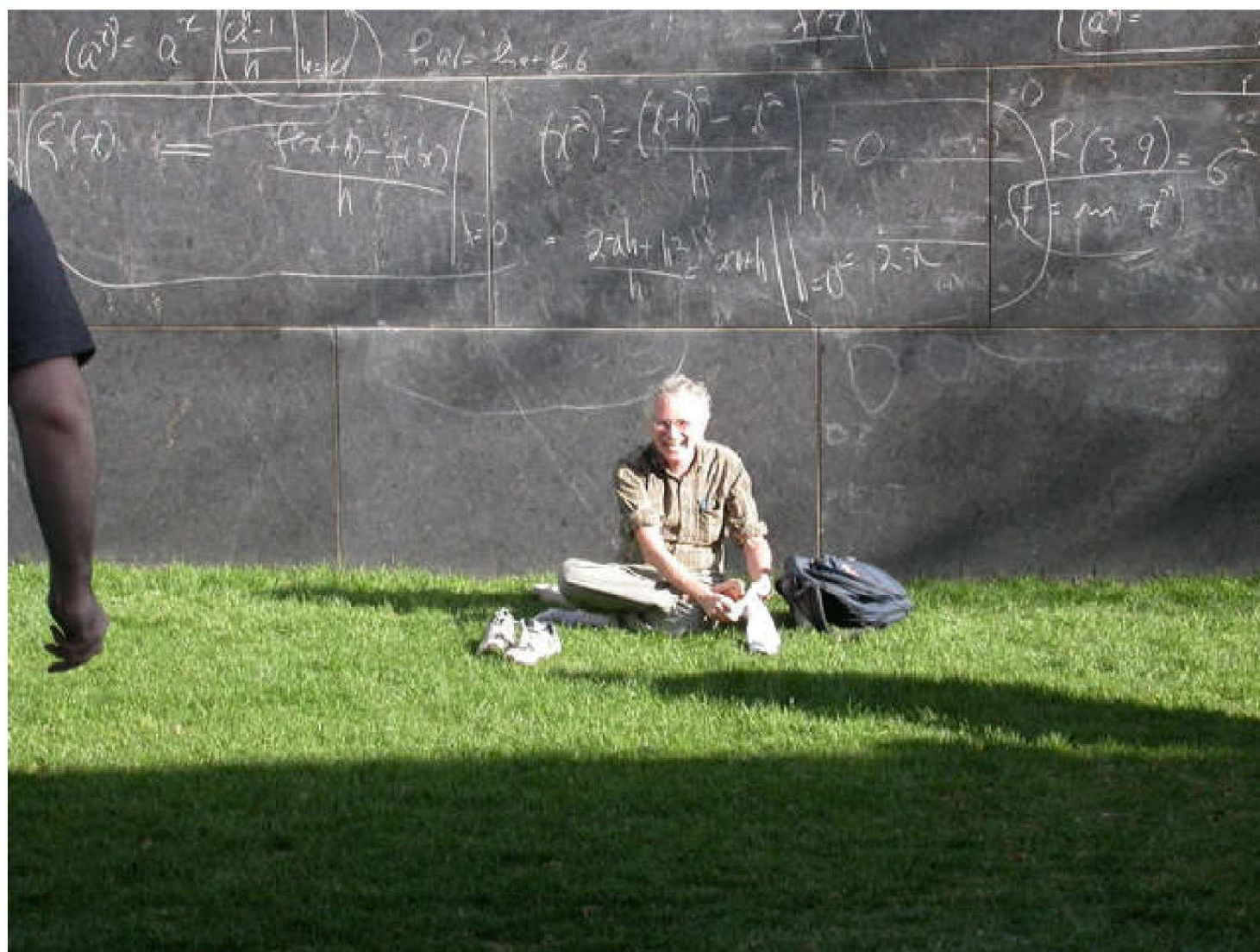
WHY IS IT SO HARD TO COUNT?









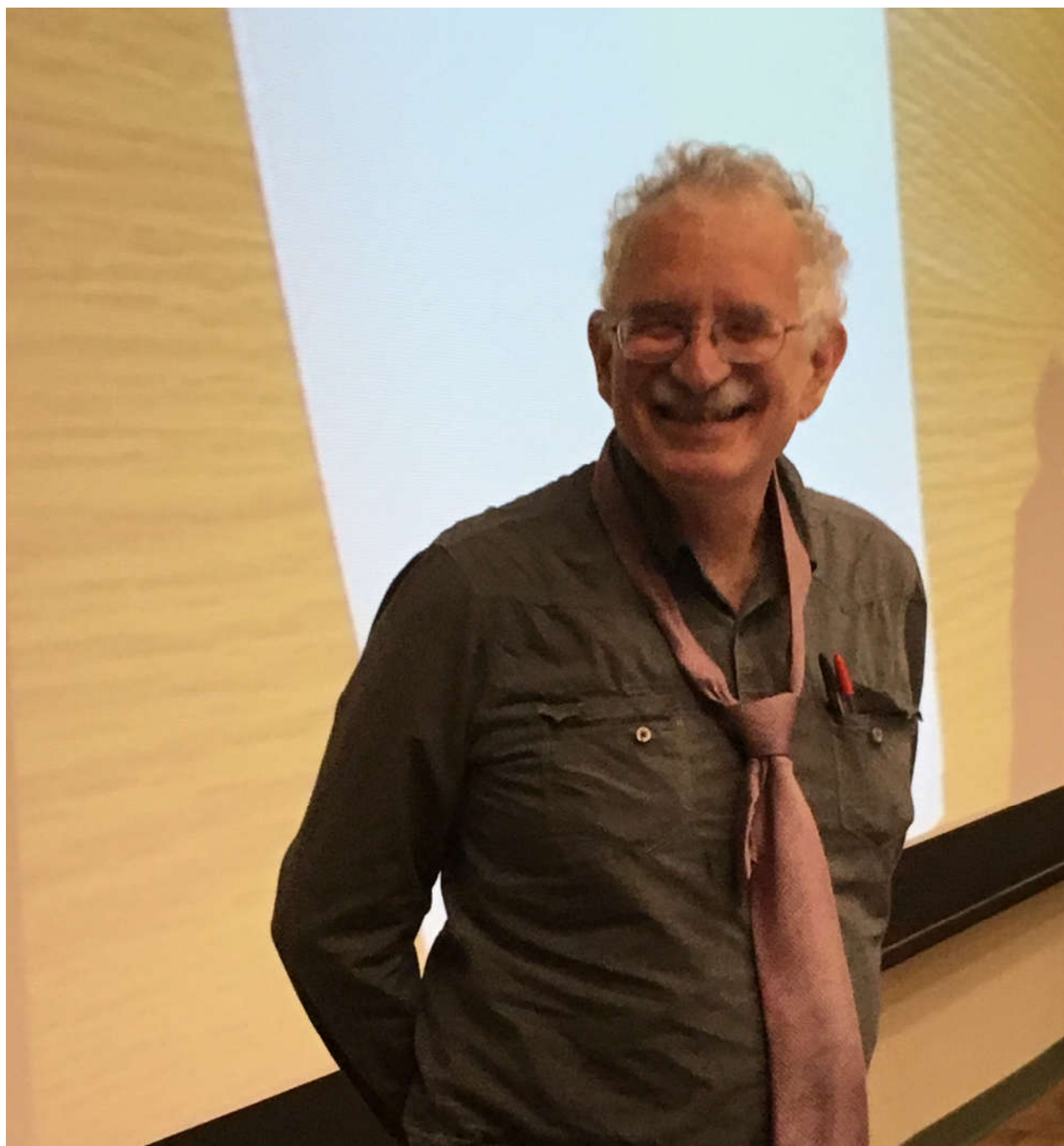






DZ in a tie ???





And with T-shirts, of course

Permutations, shuffles, descents
○○○○○

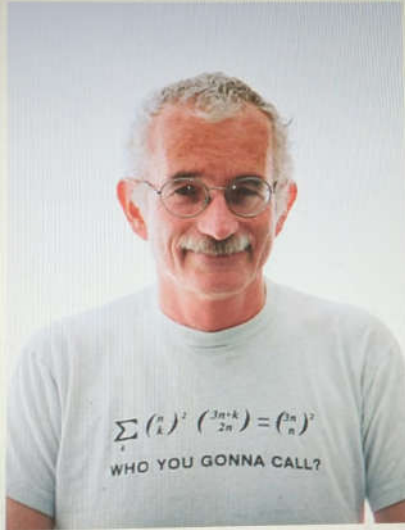
Cyclic permutations etc.
○○○○

Sym, QSym, cQSym
○○○○○○○

Other proof ingredients
○○●○○

Summary
○○○

A triple binomial identity



$$\sum_k \binom{n}{k}^2 \binom{3n-k}{2n} = \binom{3n}{n}^2$$

WHO YOU GONNA CALL?

Doron Zeilberger

2021/7/28 15:01

A triple binomial identity

$$\sum_k \binom{n}{k}^2 \binom{3n+k}{2n} = \binom{3n}{n}^2$$

WHO YOU GONNA CALL?

This is a special case of the triple-binomial identity

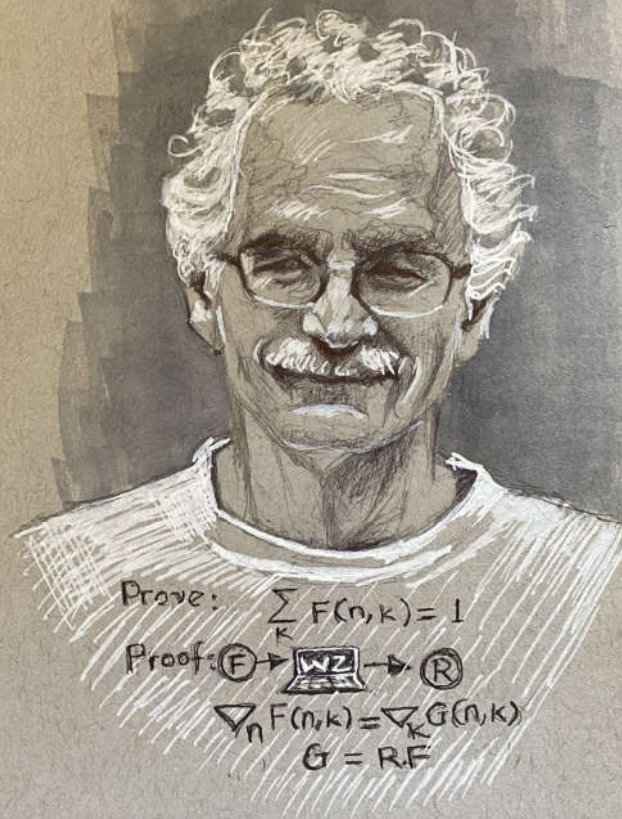
$$\sum_k \binom{m-x+y}{k} \binom{n-y+x}{n-k} \binom{x+k}{m+n} = \binom{x}{m} \binom{y}{n}$$

which is equivalent to the hypergeometric identity

$${}_3F_2 \left(\begin{matrix} a, b, -n \\ c, a+b-c-n+1 \end{matrix} \middle| 1 \right) = \frac{(c-a)^{\bar{n}}(c-b)^{\bar{n}}}{c^{\bar{n}}(c-a-b)^{\bar{n}}}$$

due to Pfaff (1797) and Saalschütz (1890). We use the general case.

HAPPY
BIRTHDAY



Dr. Z

Akalin Tefera
July 1, 2020

MAZAL TOV

Doron !

AD 120 !