

Attendance for Dr. Z.'s MathHistory for Lecture 14 (due no later than 15 minutes after class)

NAME: (print!) Quin Buob

Email to DrZlinear@gmail.com right after class

Subject: p14

with an attachment p14FirstLast.pdf

Part I: List all the "attendance questions" during the lecture, followed by your answers.

Part II:

1. Perform the following permutation-product

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 4 & 5 & 7 & 6 & 1 & 2 & 3 \end{pmatrix} \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 3 & 1 & 2 & 6 & 7 & 4 & 5 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 6 & 7 & 5 & 4 & 3 & 1 & 2 \end{pmatrix}$$

2. Let

$$\pi = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 4 & 1 & 2 & 3 \end{pmatrix},$$

find π, π^2, \dots until you get the identity permutation.

$$\pi^2 = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 3 & 4 & 1 & 2 \end{pmatrix}$$

$$\pi^3 = \pi \times \pi^2 = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 2 & 3 & 4 & 1 \end{pmatrix}$$

$$\pi^4 = (\pi^2)^2 = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \end{pmatrix}$$

3. Express the permutation

$$\pi = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 \\ 3 & 1 & 2 & 5 & 4 \end{pmatrix},$$

as a product of disjoint cycles. What is the smallest i such that π^i is the identity permutation?

$$\begin{bmatrix} 1 & 3 & 2 \\ 3 & 2 & 1 \end{bmatrix} \begin{bmatrix} 4 & 5 \\ 5 & 4 \end{bmatrix} \\ (132)(45)$$

$$\pi^2 = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 2 & 3 & 1 & 4 & 5 \end{bmatrix}$$

$$\pi^3 = \pi \times \pi^2 = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 1 & 2 & 3 & 4 & 5 \end{bmatrix}$$

$$i=3$$

4. Find π^{-1} if

$$\pi = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 \\ 3 & 1 & 2 & 5 & 4 \end{pmatrix} .$$

$$\pi^{-1} = \begin{bmatrix} 3 & 1 & 2 & 5 & 4 \\ 1 & 2 & 3 & 4 & 5 \end{bmatrix}$$

$$\pi^{-1} = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 2 & 3 & 1 & 5 & 4 \end{bmatrix}$$

Quin Boob

Attendance Quiz

AQ1: Who were the 2 geniuses who proved the impossibility of a general formula for quintic?

Abel and Ruffini

AQ2: Find a way to tile an 8×8 chess board w/ 2×1 dominoes when the board is missing its 2 opposite corners?

This is impossible b/c if the squares are alternating black and white, 1 domino must always cover 1 black square and 1 white square. This means that for this to be possible there must be an equal number of white and black squares. On an 8×8 board any 2 opposite corners will be the same color, lets say black, when these are removed there will be 32 white squares and only 30 black squares so there is no way to tile this board.

AQ3: At what age did the above geniuses die?

Ruffini died at 56 and Abel died at 26

AQ4: What university did the most in classifying simple groups? What Math department has the most # of faculty members with groups named after them?