

Homework 6

Daniel Rogers

Due 10/3

1. The parallel axiom is genuine and cannot be deduced from the other 4 axioms as the other 4 remain true in non-Euclidean geometry, while the parallel axiom does not.
2. Gödel Coding: There is a number theory statement to match every logical reasoning. A number theory statement says to itself: "I am not provable. The meta-proof says the above statement is true. Proof by contradiction suggests a statement that is wrong so that the other is true.
3. Dr. Z says there are true but unprovable statements that are meaningful, since every meaningful statement can be proved or disproved. On Turing's opinion, Dr. Z says everything is finite, if we think in a finitistic way, the problem is solved.

4. i) A: B is LT

B: A is LT

$[A, B] = [T, T]^x$, $[A, B] = [T, F]^x$, $[A, B] = [F, T]^x$ ✓

$[A, B] = [F, F]^x$

ii) A: B is TT

B: A is LT

$[A, B] = [T, T]^x$, $[A, B] = [T, F]^x$, $[A, B] = [F, T]^x$ ✓

$[A, B] = [F, F]^x$

iii) A: B is LT

B: C is LT

C: A is LT

$[A, B, C] = [T, T, T]^x$, $[A, B, C] = [T, T, F]^x$, $[A, B, C] = [T, F, T]^x$

$[A, B, C] = [F, T, T]^x$, $[A, B, C] = [T, F, F]^x$, $[A, B, C] = [F, T, F]^x$

$[A, B, C] = [F, F, T]^x$, $[A, B, C] = [F, F, F]^x$

iv) A: B is LT

B: C is LT

C: D is LT

D: A is LT

$[A, B, C, D] = [T, F, T, F]^x$, $[A, B, C, D] = [F, T, F, T]^x$ ✓

are only consistent scenarios.