

Quin Buob

HW6

1) You can't prove the parallel axiom from the other axioms because there are other non-euclidean geometries, and in these the other 4 axioms hold, but the parallel statement is false.

2) Gödel statement

$S = S$ is not provable

Proof by contradiction

Suppose that S is false, then S must be provable. This is a contradiction because if S is false the S is provable which means that a statement that is not provable is provable
→ $\leftarrow S$ must be true there is a statement that is not provable.

3) I don't know

4) i) $[A, B] = [T, T]$ Not consistent

$[A, B] = [T, F]$ Consistent

$[A, B] = [F, T]$ consistent

$[A, B] = [F, F]$ Not Consistent

ii) $[A, B] = [T, T]$ Not consistent

$[A, B] = [T, F]$ Not consistent

$[A, B] = [F, T]$ Consistent

- iii) $[A, B, C] = [T, T, T]$ Not consistent
 $[A, B, C] = [T, F, T]$ Consistent
 $[A, B, C] = [T, F, F]$ Not consistent
 $[A, B, C] = [F, T, T] =$ Not consistent
 $[A, B, C] = [F, F, T] =$ Not consistent
 $[A, B, C] = [F, F, F] =$ Not consistent

iv) I don't know