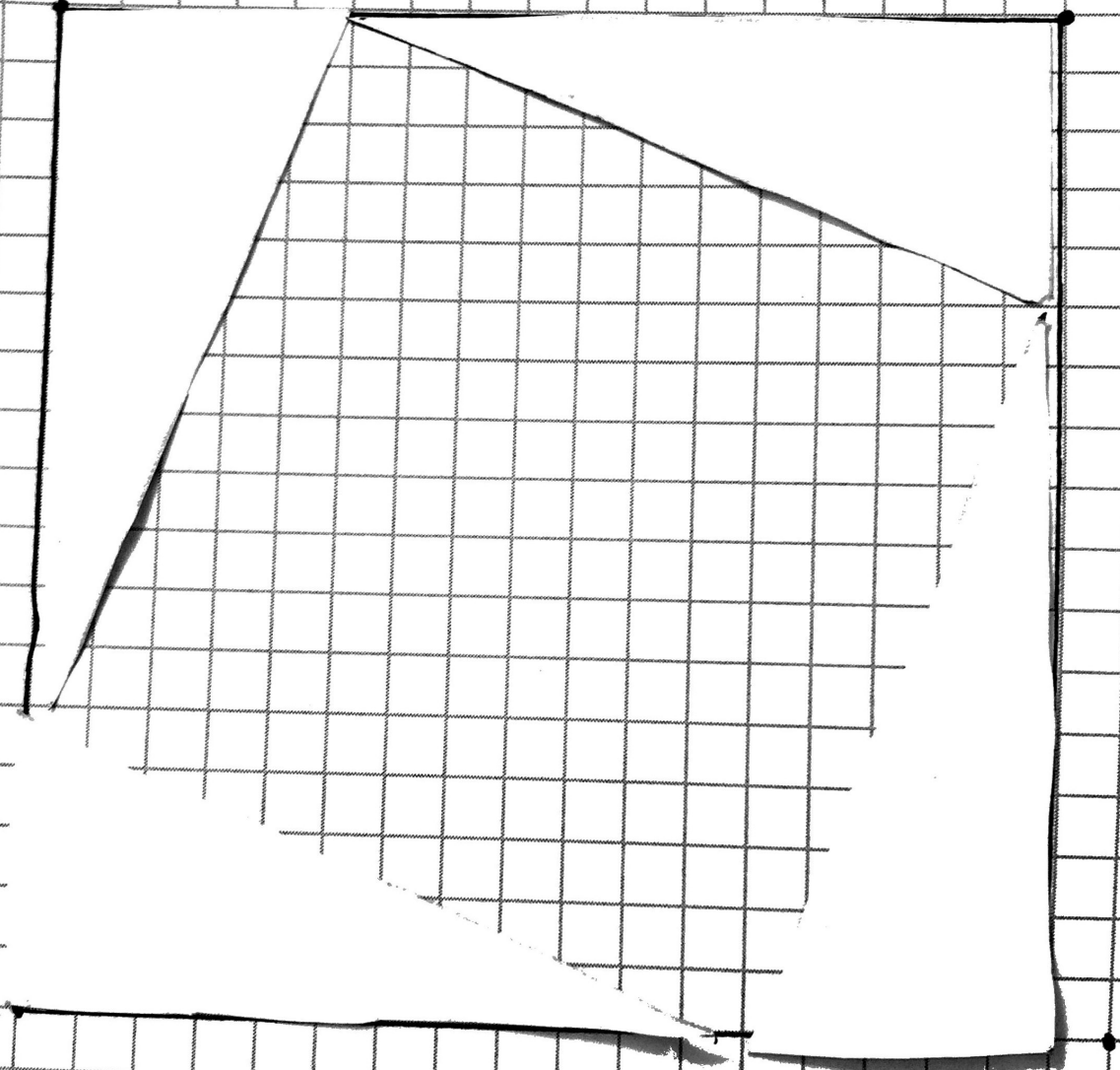
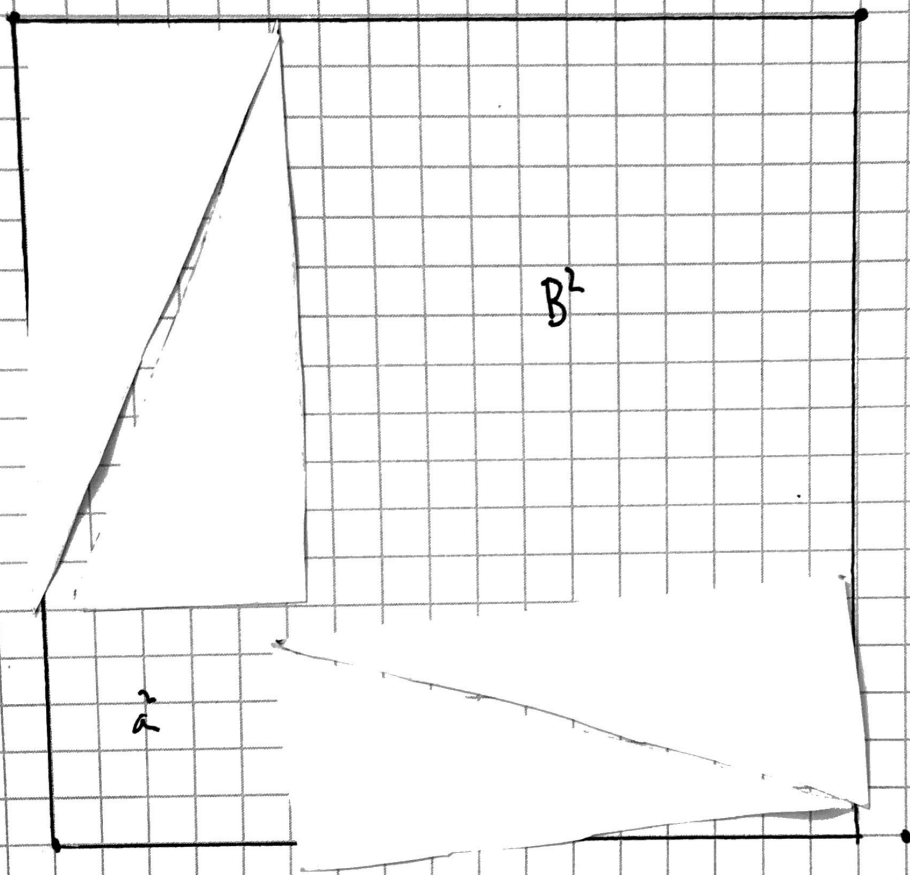


1

A.)





$$a^2 + b^2 = \text{same area as } c^2$$

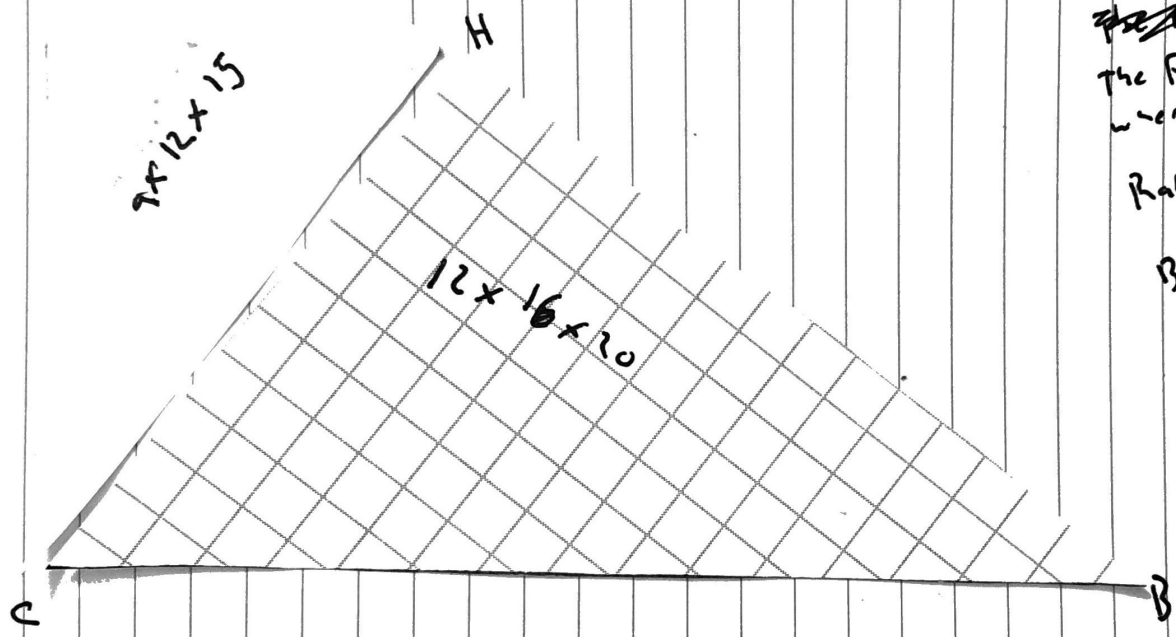
The square formed by Hypotenuse

~~is equal to the sum of the squares of the legs~~

Thus Proved

A

2.1



Similarity of Triangle leads to the equality of ratios of corresponding sides

$$\frac{BC}{AB} = \frac{BH}{BC} \quad \text{and} \quad \frac{AC}{AB} = \frac{AH}{AC}$$

~~The first~~
The first result equals cosine of θ whereas second equals sine

Ratios can be written as

$$BC^2 = AB \times BH \quad \text{and} \quad AC^2 = AB \times AH$$

Summing conditions \rightarrow

$$BC^2 + AC^2 = AB \times BH + AB \times AH$$

$$= AB \times (AH + BH) = AB^2$$

$$\text{Thus } BC^2 + AC^2 = AB^2$$

3.) A.)

main.py

Run

Shell

Clear

```
12
13 def is_coprime(m,n):
14     return math.gcd(m, n) == 1
15
16 def get_m_and_n(a, iscoprime_flag):
17     tuples = []
18     a2 = a
19     for m in range(1,a2):
20         for n in range(1,a2):
21             if m*n==a and m<=n and iscoprime_flag==False:
22                 tuples.append([m,n])
23             elif m*n==a and m<=n and iscoprime_flag==True:
24                 if is_coprime(m,n):
25                     tuples.append([m,n])
26     return tuples
27
28 def gen_tripplles_with_known_a(tuples):
29     S = []
30     for tuple in tuples:
31         m = tuple[1]
32         n = tuple[0]
33         S.append([120, m**2+n**2, m**2-n**2])
34     return S
35
```

```
[[120, 904, 896], [120, 409, 391], [120, 241, 209], [120, 169, 119],
 [120, 136, 64]]
> These are a few of the pythagorean tripples where with a = 120. These
are not nessesarily primal though some are
```

3.B)



main.py



Run

Shell

Clear

```
16- def get_m_and_n(a, iscoprime_flag):
17     tuples = []
18     a2 = a
19-     for m in range(1,a2):
20-         for n in range(1,a2):
21-             if m*n==a and m<=n and iscoprime_flag==False:
22                 tuples.append([m,n])
23-             elif m*n==a and m<=n and iscoprime_flag==True:
24-                 if is_coprime(m,n):
25                     tuples.append([m,n])
26     return tuples
27
28- def gen_tripplles_with_known_a(tuples):
29     S = []
30-     for tuple in tuples:
31         m = tuple[1]
32         n = tuple[0]
33         S.append([120, m**2+n**2, m**2-n**2])
34     return S
35
36- if __name__ == "__main__":
37     # print(generate_tripplles(10))
38     tuples = get_m_and_n(60,True)
39     print(gen_tripplles_with_known_a(tuples))
```

```
[[120, 409, 391], [120, 241, 209], [120, 169, 119]]
```

```
> These are some of the unique primal pythagorean tripples|
```



JS

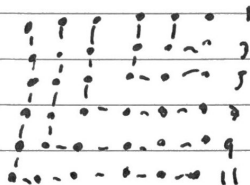
4.) Euclid's Proof

Lemma: difference of squares of any 2 #s (that are consecutive) are always odd

$$2^2 - 1^2 = 3$$

$$3^2 - 2^2 = 5$$

⋮



Geometric Proof for infinite odd #s

Since Perfect Squares form a subset of odd #s, the direction of infinity is also infinity, it follows that there must also be an infinite # of odd squares, and such there is also an infinite # of Pythagorean Triples!

5.) ~~Abraham~~ Fermat

6.) Euler

7.) Fermat

8.) Andronik