

Nabhanya Neb Homework 14

you can post

① a)
$$\begin{array}{ccccccccc} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 7 & 1 & 2 & 6 & 9 & 5 & 3 & 8 & 4 \end{array}$$

b)
$$\begin{array}{ccccccccc} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 8 & 6 & 1 & 5 & 3 & 2 & 7 & 4 & 9 \end{array}$$

②
$$\pi^2 = \begin{array}{cccccc} 1 & 2 & 3 & 4 & 5 \\ 5 & 2 & 1 & 4 & 3 \end{array}$$

$$\pi^3 = \begin{array}{cccccc} 1 & 2 & 3 & 4 & 5 \\ 1 & 4 & 3 & 2 & 5 \end{array}$$

$$\pi^4 = \begin{array}{cccccc} 1 & 2 & 3 & 4 & 5 \\ 3 & 2 & 5 & 4 & 1 \end{array}$$

$$\pi^5 = \begin{array}{cccccc} 1 & 2 & 3 & 4 & 5 \\ 5 & 4 & 1 & 2 & 3 \end{array}$$

$$\pi^6 = \begin{array}{cccccc} 1 & 2 & 3 & 4 & 5 \\ 1 & 2 & 3 & 4 & 5 \end{array} = \text{identity permutation}$$

③
$$\left(\begin{array}{ccc} 1 & 4 & 6 \\ 4 & 6 & 1 \end{array} \right) \left(\begin{array}{cccccc} 2 & 5 & 8 & 3 & 7 & 9 \\ 5 & 8 & 3 & 7 & 9 & 2 \end{array} \right)$$

$$(146)(258379)$$

$$\text{lcm}(3, 6) = \boxed{12}$$

$$(4) \begin{pmatrix} 1 & 9 \\ 9 & 1 \end{pmatrix} \begin{pmatrix} 2 & 4 & 7 \\ 4 & 7 & 2 \end{pmatrix} \begin{pmatrix} 3 & 5 & 6 & 8 & 10 \\ 5 & 6 & 8 & 10 & 3 \end{pmatrix}$$

$$(19)(247)(356810)$$

$$2 \quad 3 \quad 5$$

$$lcm(2, 3, 5) = 30$$

$\pi^i = \text{identity permutation if } i = 30$

$$(5) \pi^{-1} :$$

$$\text{Upside down: } \begin{pmatrix} 4 & 9 & 5 & 8 & 6 & 7 & 2 & 1 & 10 & 3 \\ 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \end{pmatrix}$$

$$\text{in order: } \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ 8 & 7 & 10 & 1 & 3 & 5 & 6 & 4 & 2 & 9 \end{pmatrix}$$

- (6) {1, 2, 3}: NONE (0)
 {1, 3, 2}: positions: (2, 3) values: (3, 2) (1)
 {2, 4, 3}: positions: (1, 2) values: (2, 1) (1)
 {2, 3, 1}: positions: (1, 3), (2, 3) values: (2, 2), (3, 2) (2)
 {3, 1, 2}: positions: (1, 2), (1, 3) vals: (3, 1), (3, 2) (2)
 {3, 2, 1}: pos: (1, 2), (1, 3), (2, 3) vals: (3, 2), (3, 1), (2, 2) (3)

(7) 1 5 2 3 7 4 6
 $0 + 3 + 0 + 0 + 2 + 0 + 0 = 5 \text{ inversions}$

$$* a[i] > a[j]$$

where $i < j$