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1. Assume there have prime number P_1, P_2, \dots, P_n

$$\text{and } L = P_1 P_2 \dots P_n + 1$$

L must be divisible by some prime

so it must be one of prime number from P_1, \dots, P_n

$$\text{But } P_k \mid P_1 \dots P_n \text{ so } (L - P_1 \dots P_n) = 1$$

it is contradiction

so L ~~isn't~~ isn't the largest prime

so there have infinity prime number

2. 1 2 3 5 7 11 13 17 19 23 29 31 37 41

43 47 73 79 83 89 97 101 103 107 109

113 127 131 137 139

$$3. \begin{array}{r} 3 \overline{) 3003} \\ \underline{11} \\ 11 \overline{) 1001} \\ \underline{7} \\ 7 \overline{) 191} \\ \underline{13} \end{array} \quad 3003 = 3 \cdot 7 \cdot 11 \cdot 13$$

4.