

# HW 1

1) If  $n_1$  and  $n_2$  are prime meaning the greatest common denominator of  $n_1$  and  $n_2$  is equal to 1

$f(x) = (0, 0)$  where  $x$  is divisible by  $n_1$  and  $n_2$   
since we know  $n_1$  and  $n_2$  are prime,  
then  $n_1$  and  $n_2$  multiplied by each other makes  
 $n_1$  and  $n_2$  multiples. With that, we know  
that  $0 \leq x < n_1 n_2$ . And based on our  
proof we know that  $x = 0$ .  $0 \leq 0 < (0)(0)$  ✓

$$2) \frac{1}{2} + \frac{1}{3} + \frac{1}{5} = \frac{3}{6} + \frac{2}{6} = \frac{5}{6} \quad \frac{5}{6} + \frac{1}{5}$$

$$\frac{25}{30} + \frac{6}{30} = \frac{31}{30} \quad x = \frac{31}{30} \quad \text{ceil}\left(\frac{31}{30}\right) = 2$$

$$EF\left(\frac{30}{31}\right) = \frac{1}{2} + EF\left(\frac{30}{31} - \frac{1}{2}\right) \\ = \frac{29}{62} \quad \text{ceil}\left(\frac{62}{29}\right) = 3$$

$$EF\left(\frac{30}{31}\right) = \frac{1}{2} + \frac{1}{3} + EF\left(\frac{29}{62} - \frac{1}{3}\right)$$

$$\frac{25}{186} \quad \text{ceil}\left(\frac{186}{25}\right) = 8$$

$$EF\left(\frac{30}{31}\right) = \frac{1}{2} + \frac{1}{3} + \frac{1}{8} + EF\left(\frac{25}{186} - \frac{1}{8}\right)$$

$$\frac{7}{744} \quad \text{ceil}\left(\frac{744}{7}\right) = 107$$



$$EF\left(\frac{30}{31}\right) = \frac{1}{2} + \frac{1}{3} + \frac{1}{8} + \frac{1}{107} + EF\left(\frac{2}{749} - \frac{1}{107}\right)$$

$$\frac{5}{79608} \quad \text{ceil}\left(\frac{79608}{5}\right) = 15922$$

$$EF\left(\frac{30}{31}\right) = \frac{1}{2} + \frac{1}{3} + \frac{1}{8} + \frac{1}{107} + \frac{1}{15922} + EF\left(\frac{5}{79608} - \frac{1}{15922}\right)$$

$$EF\left(\frac{30}{31}\right) = \frac{1}{2} + \frac{1}{3} + \frac{1}{8} + \frac{1}{107} + \frac{1}{15922} + \frac{1}{633759288}$$

The Egyptians fractions we had initially is better as the new ones are too tedious and seems impossible to divide among people.

$$3) a) f(x) = (2 \pmod{3}, 6 \pmod{7})$$

$$2, 5, 8, 11, 14, 17, 20 \quad 6, 13, 20$$

$$\text{Ans} = \boxed{20}$$

$$b) f(x) = (1 \pmod{3}, 4 \pmod{7})$$

$$1, 9 \quad 4, 11, 18$$

$$\text{Ans} = \boxed{4}$$

$$c) f(x) = (0 \pmod{3}, 2 \pmod{7})$$

$$0, 3, 6, 9 \quad 2, 9$$

$$\text{Ans} = \boxed{9}$$