Homework for Dr. Z.'s MathHistory for Lecture 1

0. Read and understand Chapter II, sections 1-3 (pp. 13-23) summarize its content in your own words and your own handwriting, and write it in your HISTORY notebook, [You should have at least the equivalent of two typed pages]

The other problems should be either hand-written or typed and sent as .pdf file (PLEASE no other formats) or if you prefer .txt file, to DrZlinear@gmail.com by 8:00pm Sunday, Sept. 12, 2021,

Subject: hw1

with an attachment: hw1FirstLast.pdf (or hw1FirstLast.txt)

1. Read and **understand**, and write-down, in *your own words*, the beautiful proof of the Chinese Remainder Theorem (Special Version) given in today's handout

http://www.math.rutgers.edu/~zeilberg/Hist21/crt.pdf

2. Convert the following Egyptian fraction

$$\frac{1}{2} + \frac{1}{3} + \frac{1}{5}$$

into a usual fraction, i.e. compute its value. Use the **greedy algorithm** to express it as another Egyptian fraction. Interpret both ways in terms of equally dividing pizzas among people, and say which way is better.

3.

- (a) Find the smallest two integers that have the property that
- it leaves remainder 2 when divided by 3
- it leaves remainder 6 when divided by 7
- (b) Find the smallest two integers that have the property that
- \bullet it leaves remainder 1 when divided by 3
- it leaves remainder 4 when divided by 7
- (c) Find the smallest two integers that have the property that
- \bullet it leaves remainder 0 when divided by 3
- it leaves remainder 2 when divided by 7