

Output sequences for Maple code (extended)

(*More sequences to be added)

King's Tour:

- The sequence for the total number of hamiltonian cycles for a 3 x n board
> seq(nops(KiTours(3, i))/2, i = 1 .. 20)
> 0, 4, 16, 120, 744, 4922, 31904, 208118, 1354872, 8826022, 57483536,
374412158, 2438639080, 15883563110, 103454037120, 673825180718,
4388811619032, 28585557862518, 186185731404016, 1212679737590398
- Generating Function for (3 x n) board:
$$[-(6*x^5 + 8*x^4 + 4*x^3 - 4*x)/(-6*x^4 - 8*x^3 - 15*x^2 - 4*x + 1), \text{ogf}]$$
- This sequence is not found on OEIS
- The sequence for the total number of hamiltonian cycles for a 2 x n board
> seq(nops(KiTours(2, i))/2, i = 2 .. 13)
> 3, 4, 8, 16, 32, 64, 128, 256, 512, 1024, 2048, 4096
- Generating Function for (2 x n) board:
$$[-(-3 + 2*x)/(-2*x + 1), \text{ogf}]$$
- OEIS A-number := A198633

Knight's Tour:

- The sequence for the total number of hamiltonian cycles for a 3 x n board
> seq(nops(KtTours(3,i))/2,i=1..28)
> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 16, 0, 176, 0, 1536, 0, 15424, 0, 147728, 0,
1448416, 0, 14060048, 0, 136947616, 0, 1332257856, 0, 12965578752
- Generating Function for 3 x n board:
$$16 * (z^5 + 5*z^6 - 34*z^7 - 116*z^8 + 505*z^9 + 616*z^{10} - 3179*z^{11} - 4*z^{12} + 9536*z^{13} - 8176*z^{14} - 13392*z^{15} + 15360*z^{16} + 13888*z^{17} + 2784*z^{18} - 3328*z^{19} - 22016*z^{20} + 5120*z^{21} + 2048*z^{22}) / (1 - 6*z - 64*z^2 + 200*z^3 + 1000*z^4 - 3016*z^5 - 3488*z^6 + 24256*z^7 - 23776*z^8 - 104168*z^9 + 203408*z^{10} + 184704*z^{11} - 443392*z^{12} - 14336*z^{13} + 151296*z^{14} - 145920*z^{15} + 263424*z^{16} - 317440*z^{17} - 36864*z^{18} + 966656*z^{19} - 573440*z^{20} - 131072*z^{21})$$
- OEIS A-number := A169764

- The sequence for the total number of hamiltonian cycles for a 2 x n board
 > seq(nops(KtTours(2, i))/2, i = 1 .. 20);
 > 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0

Queen's Tour:

- The sequence for the total number of hamiltonian cycles for a 3 x n board
 > seq(nops(QiTours(3, i))/2, i = 1 .. 4)
 > 0,24,1960,243040
- This sequence is not found on OEIS
- The sequence for the total number of hamiltonian cycles for a 2 x n board
 > seq(nops(QiTours(2, i))/2, i = 2 .. 9)
 > 3,24,108,522,2646,13150,65206,324370
- This sequence is not found on OEIS

Rook's Tour:

- The sequence for the total number of hamiltonian cycles for a 3 x n board
 > seq(nops(RiTours(3, i))/2, i = 1 .. 7)
 > 0, 6, 96, 3132, 84192, 1821912, 37359444
- This sequence is not found on OEIS
- The sequence for the total number of hamiltonian cycles for a 2 x n board
 > seq(nops(RiTours(2, i))/2, i = 1 .. 13)
 > 1, 2, 6, 20, 48, 126, 348, 936, 2512, 6788, 18322, 49406, 133296
- This sequence is not found on OEIS

Bishop's Tour: The bishop never makes a hamiltonian cycle because its diagonal path can only reach half of the vertices

- The sequence for the total number of hamiltonian cycles for a 3 x n board
 > seq(nops(BiTours(3, i))/2, i = 1 .. 15)
 > 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0
- The sequence for the total number of hamiltonian cycles for a 2 x n board
 > seq(nops(BiTours(2, i))/2, i = 1 .. 15);
 > 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0

