

Predator/Prey Modeling

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Nicholson-Bailey host-parasite equations

- Prey equation $\rightarrow H(t)$
- Predator equation $\rightarrow P(t)$
- Prey carrying capacity $\rightarrow K$
- Strength of Interaction between Predator/Prey $\rightarrow a$

Stability

- r = prey reproductive rate
- q = depression of prey equilibrium (how much predators suppress it)
- If both λ 's have $|\lambda| < 1 \rightarrow$ the equilibrium is stable.
- If $|\lambda| > 1 \rightarrow$ equilibrium is unstable $\rightarrow$ oscillations or chaos.

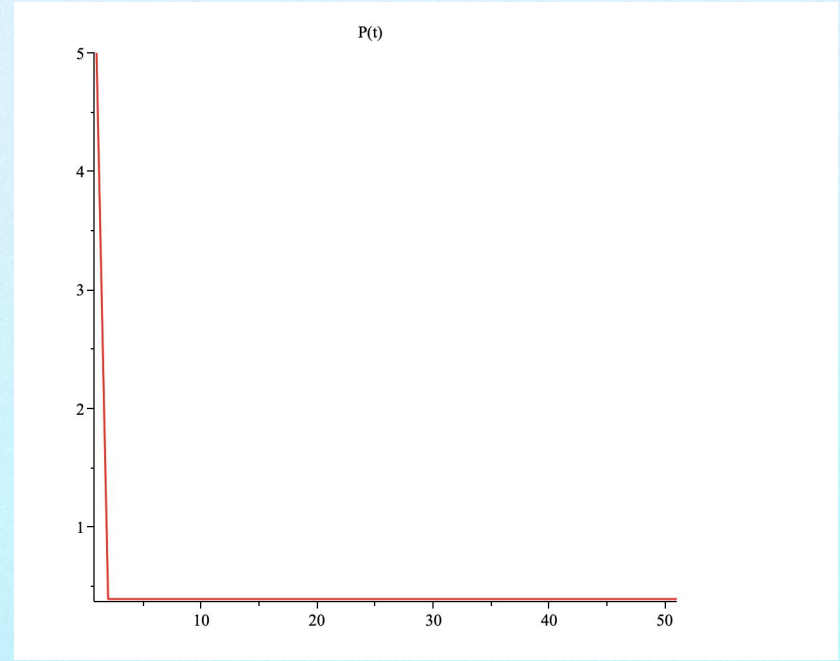
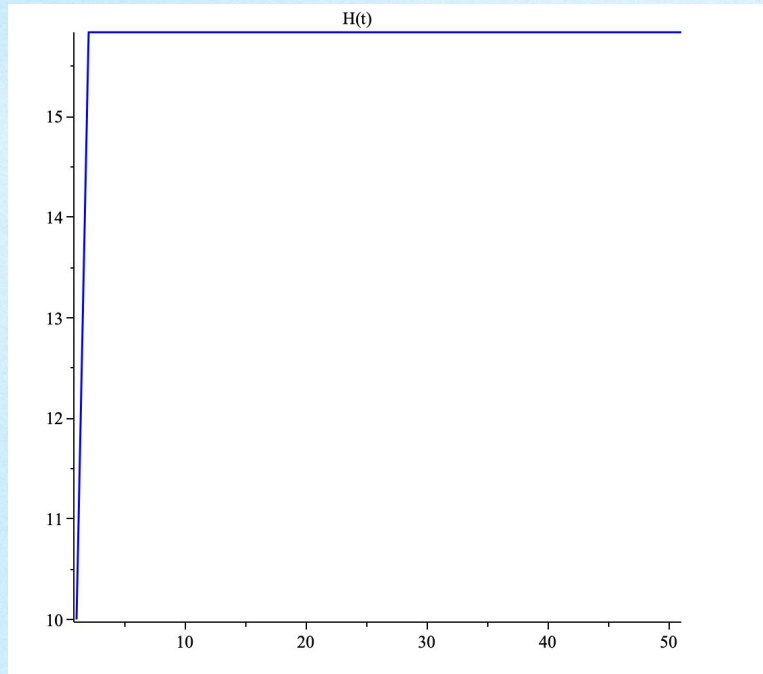
$$H_{t+1} = H_t \exp[r(1 - H_t/K) - aP_t]$$

$$P_{t+1} = aH_t[1 - \exp(-aP_t)]$$

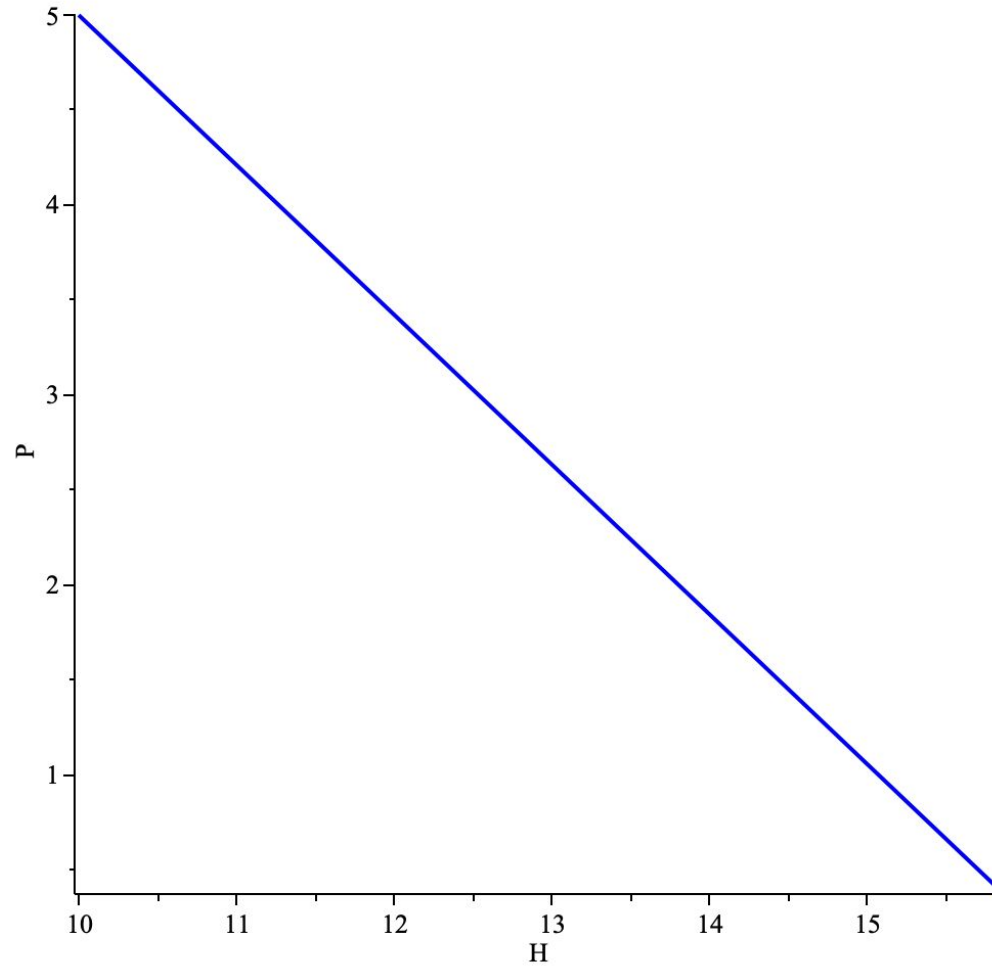
$$\lambda^2 - \lambda(1 - r + \varphi) + (1 - rq)\varphi + r^2q(1 - q) = 0$$

where $\varphi = r(1 - q)/\{1 - \exp[-r(1 - q)]\}$

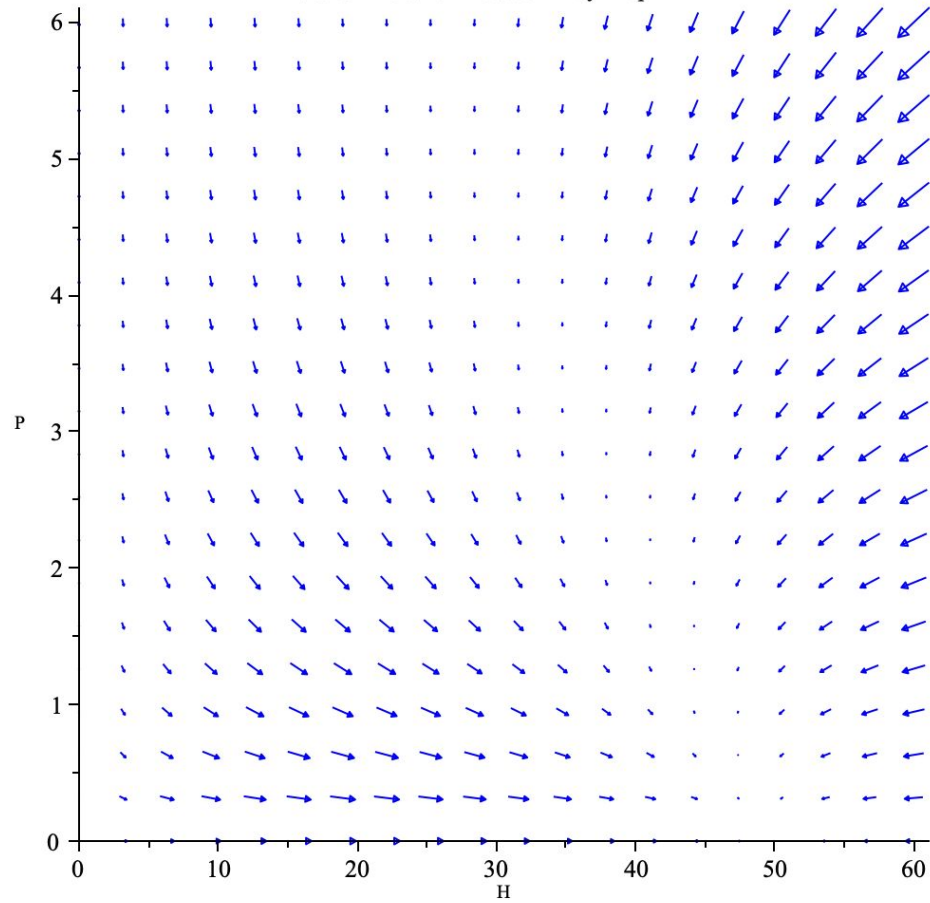
Case 1: $r=1.2$ $a=.10$, $K=50$, $H=10$, $P=5$



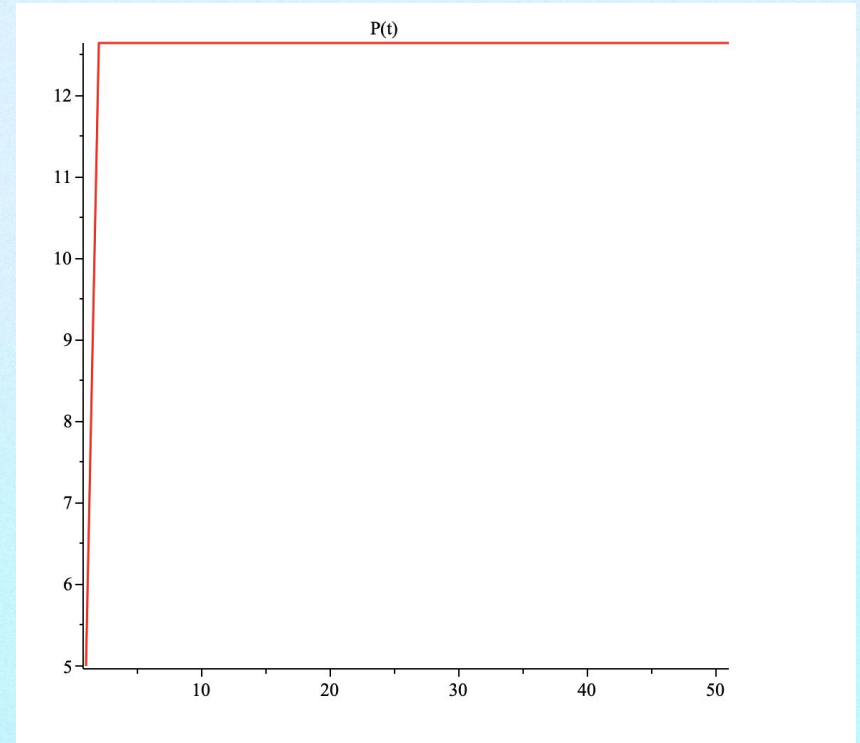
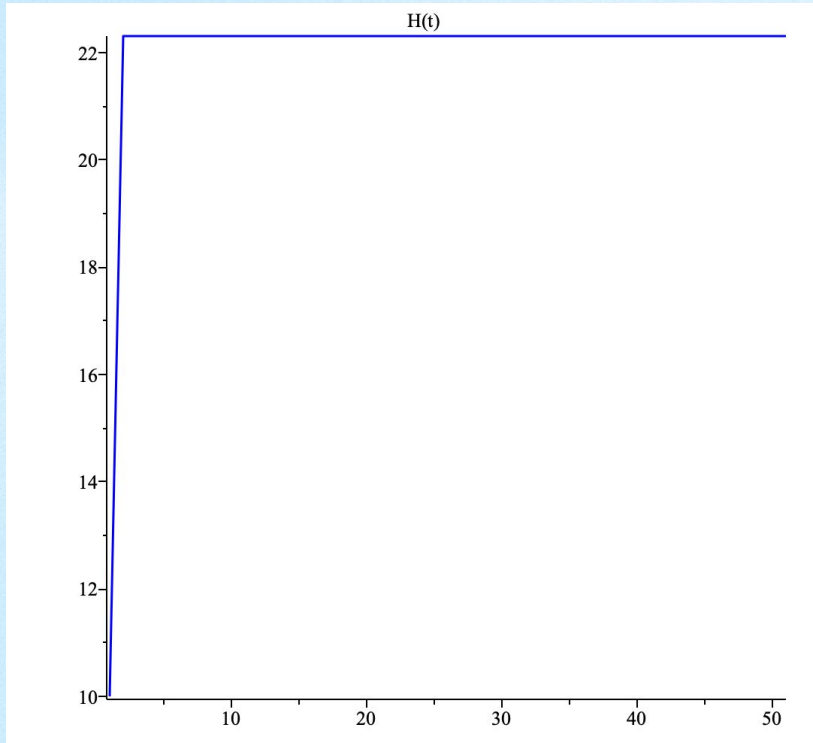
Phase Portrait: H vs P



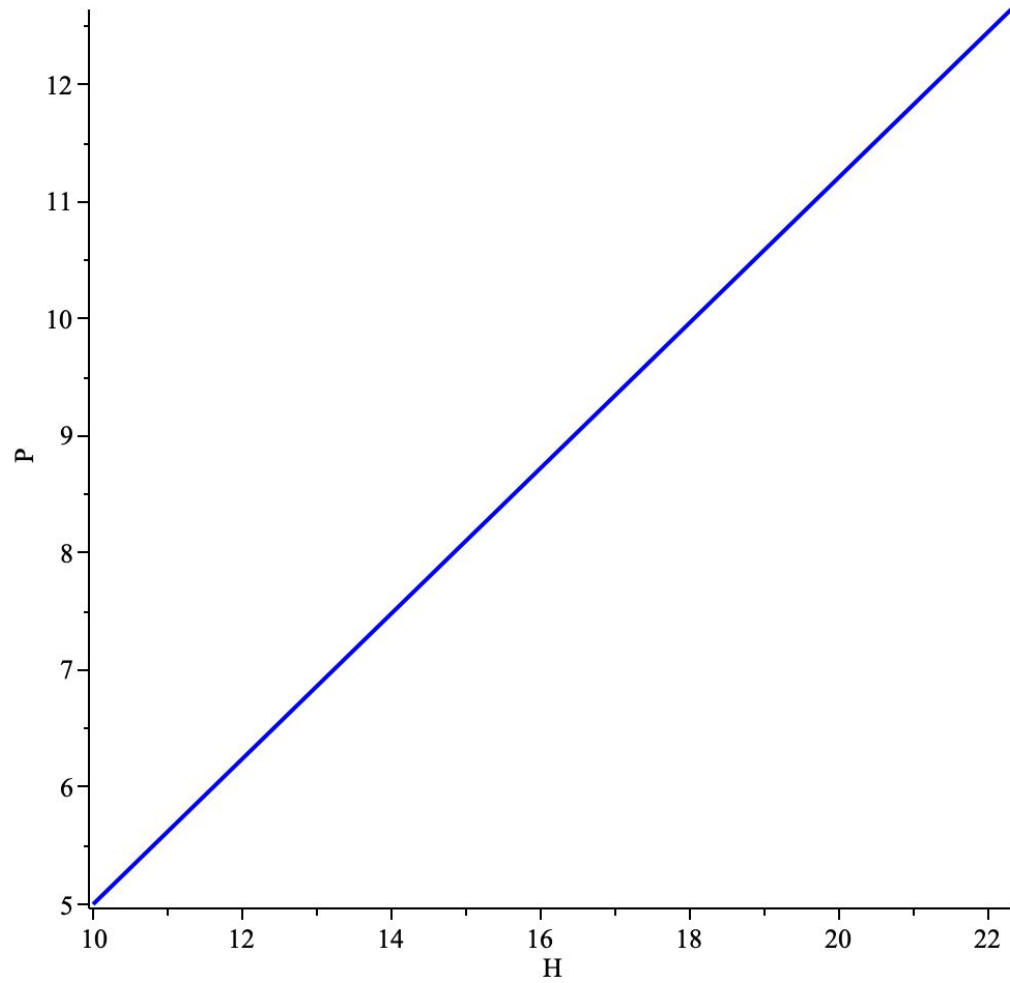
Vector Field for Predator-Prey Map



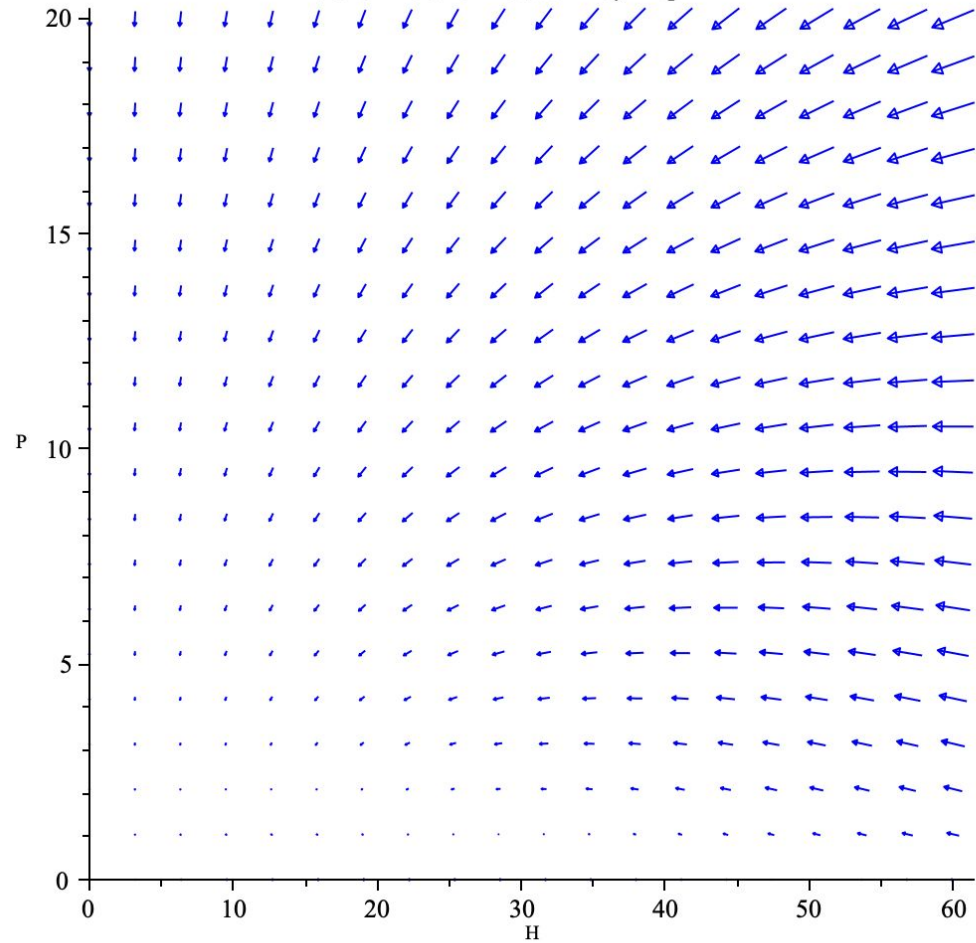
Case 2: $r=.5$, $a=.2$, $K=50$, $H=100$, $P=5$



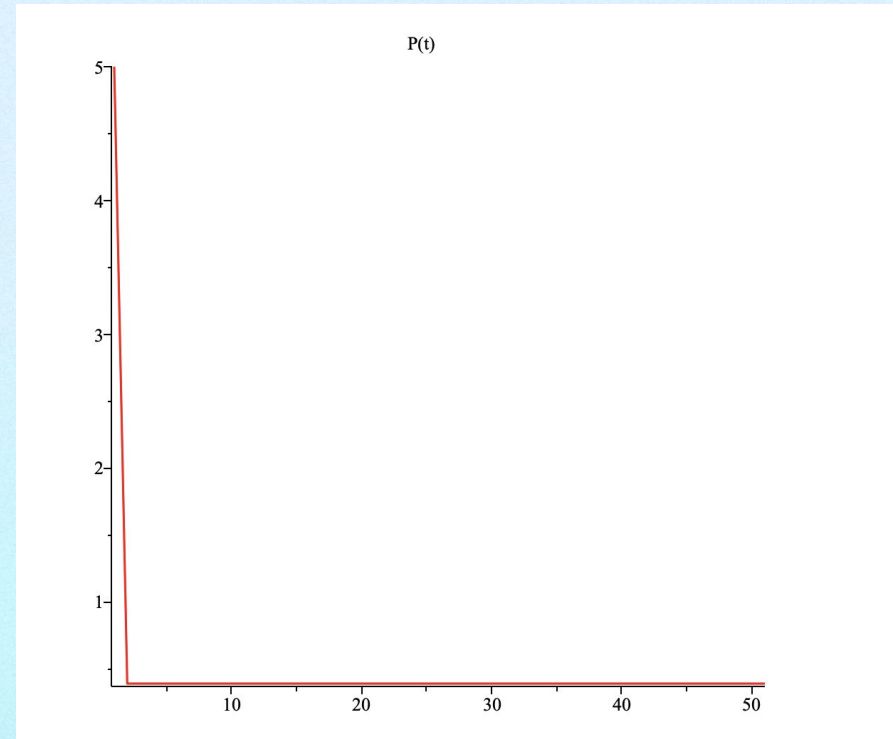
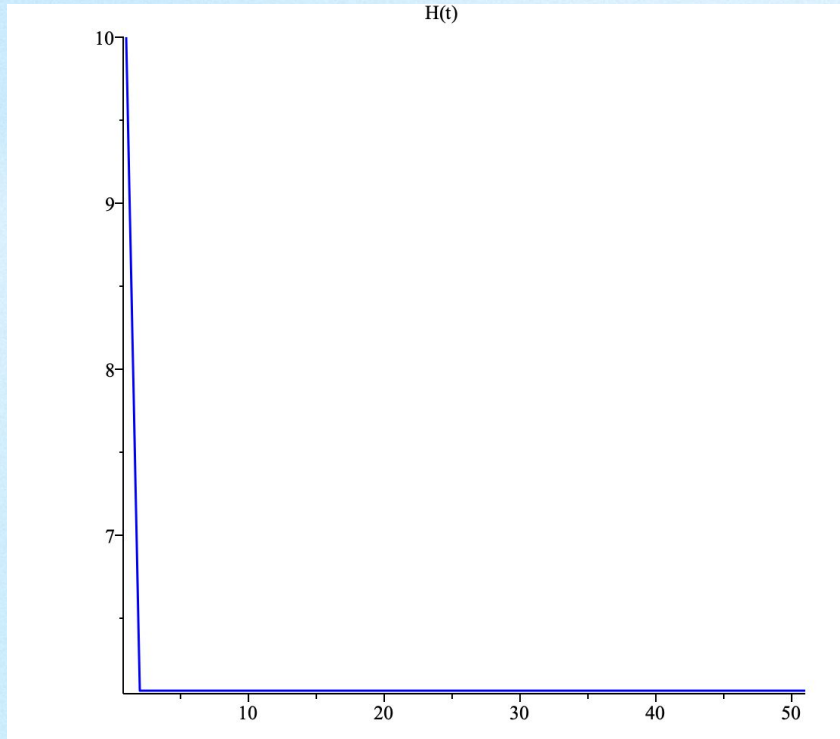
Phase Portrait: H vs P



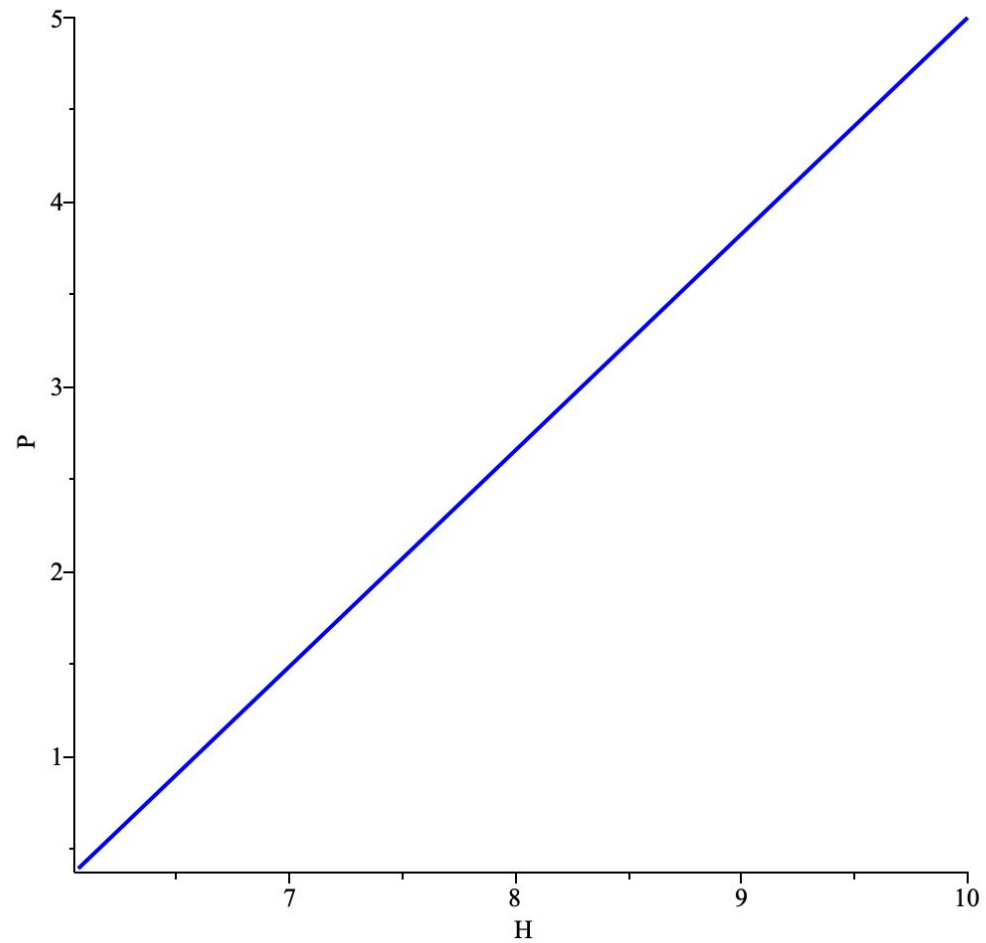
Vector Field for Predator-Prey Map



Case 3: $r=5, a=1, K=10, H=5, P=5$



Phase Portrait: H vs P



Vector Field for Predator-Prey Map

