

> read `DMB8.txt`

*For a list of the Main procedures type: Help8(); for help with a specific procedure type: Help6
(ProcedureName); for example Help6(RandomMC);*

*For a list of the other procedures type: Help8a()); for help with a specific procedure type: Help6
(ProcedureName); for example Help6(RandomMC);* (1)

> $g := raRF(x, 3)$

$$g := \frac{4x^3 + 2x^2 + 2x + 10}{10x^3 + 9x^2 + 3x + 8} \quad (2)$$

> evalf(SSS(g, x))

$$[0.7396118112] \quad (3)$$

> Orb(g, x, 100.1, 1000, 1010)

$$[0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, \\ 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110] \quad (4)$$

> Orb(g, x, 10.1, 1000, 1010)

$$[0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, \\ 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110] \quad (5)$$

> Orb(g, x, -10.1, 1000, 1010)

$$[0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, \\ 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110] \quad (6)$$

> Orb(g, x, -100.1, 1000, 1010)

$$[0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, \\ 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110, 0.7396118110] \quad (7)$$

> $g := raRF(x, 3)$

$$g := \frac{9x^3 + 10x^2 + 8x + 2}{7x^3 + 7x^2 + 6x + 1} \quad (8)$$

> evalf(SSS(g, x))

$$[1.360052363] \quad (9)$$

> Orb(g, x, 100.1, 1000, 1010)

$$[1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363, \\ 1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363] \quad (10)$$

> Orb(g, x, 10.1, 1000, 1010)

$$[1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363, \\ 1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363] \quad (11)$$

> Orb(g, x, -10.1, 1000, 1010)

$$[1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363, \\ 1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363] \quad (12)$$

1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363]

> Orb($g, x, -100.1, 1000, 1010$)
[1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363,
1.360052363, 1.360052363, 1.360052363, 1.360052363, 1.360052363] (13)

>

>

> $g := raRF(x, 3)$

$$g := \frac{3x^3 + 5x^2 + 3x + 3}{x^3 + 3x^2 + 10x + 8} \quad (14)$$

> evalf(SSS(g, x))

[0.4186175181] (15)

> Orb($g, x, 100.1, 1000, 1010$)

[0.4186175182, 0.4186175181, 0.4186175180, 0.4186175179, 0.4186175182, 0.4186175181,
0.4186175180, 0.4186175179, 0.4186175182, 0.4186175181, 0.4186175180] (16)

> Orb($g, x, 10.1, 1000, 1010$)

[0.4186175181, 0.4186175180, 0.4186175179, 0.4186175182, 0.4186175181, 0.4186175180,
0.4186175179, 0.4186175182, 0.4186175181, 0.4186175180, 0.4186175179] (17)

> Orb($g, x, -10.1, 1000, 1010$)

[0.4186175182, 0.4186175181, 0.4186175180, 0.4186175179, 0.4186175182, 0.4186175181,
0.4186175180, 0.4186175179, 0.4186175182, 0.4186175181, 0.4186175180] (18)

> Orb($g, x, -100.1, 1000, 1010$)

[0.4186175182, 0.4186175181, 0.4186175180, 0.4186175179, 0.4186175182, 0.4186175181,
0.4186175180, 0.4186175179, 0.4186175182, 0.4186175181, 0.4186175180] (19)

> $g := raRF(x, 3)$

$$g := \frac{5x^3 + 5x^2 + 3x + 1}{2x^3 + 10x^2 + 10x + 10} \quad (20)$$

> evalf(SSS(g, x))

[0.1292929950] (21)

> Orb($g, x, 100.1, 1000, 1010$)

[0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950,
0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950] (22)

> Orb($g, x, 10.1, 1000, 1010$)

[0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950,
0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950] (23)

> Orb($g, x, -10.1, 1000, 1010$)

$$[0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, \\ 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950] \quad (24)$$

$$\begin{aligned} &> Orb(g, x, -100.1, 1000, 1010) \\ &[0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, \\ &0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950, 0.1292929950] \end{aligned} \quad (25)$$

$$g := \frac{9x^3 + 2x^2 + 4x + 8}{4x^3 + 7x^2 + 9x + 5} \quad (26)$$

$$\textcolor{blue}{> \text{evalf}(SSS(g, x))} \quad \textcolor{blue}{[0.9127501374]} \quad (27)$$

$$\begin{aligned} &> Orb(g, x, 100.1, 1000, 1010) \\ &[0.9127501369, 0.9127501369, 0.9127501369, 0.9127501369, 0.9127501369, 0.9127501369, \\ &0.9127501369, 0.9127501369, 0.9127501369, 0.9127501369, 0.9127501369] \end{aligned} \quad (28)$$

$$\begin{aligned} &> Orb(g, x, 10.1, 1000, 1010) \\ &[0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, \\ &0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374] \end{aligned} \quad (29)$$

$$\begin{aligned} &> Orb(g, x, -10.1, 1000, 1010) \\ &[0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, \\ &0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374] \end{aligned} \quad (30)$$

$$\begin{aligned} &> Orb(g, x, -100.1, 1000, 1010) \\ &[0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, \\ &0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374, 0.9127501374] \end{aligned} \quad (31)$$

$$g := \frac{10x^3 + 9x^2 + 10x + 3}{8x^3 + 7x^2 + 9x + 4} \quad (32)$$

$$\textcolor{blue}{> \textit{evalf}(SSS(g, x))} \quad \textcolor{blue}{[1.164908077]} \quad \textbf{(33)}$$

$$\begin{aligned} &> Orb(g, x, 100.1, 1000, 1010) \\ &[1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076, \\ &1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076] \end{aligned} \quad (34)$$

$$\begin{aligned} &> \text{Orb}(g, x, 10.1, 1000, 1010) \\ &[1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076, \\ &1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076] \end{aligned} \quad (35)$$

$$\begin{aligned} &> Orb(g, x, -10.1, 1000, 1010) \\ &[1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076, \\ &1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076] \end{aligned} \quad (36)$$

$$\begin{aligned} &> Orb(g, x, -100.1, 1000, 1010) \\ &[1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076, \\ &1.164908076, 1.164908076, 1.164908076, 1.164908076, 1.164908076] \end{aligned} \quad (37)$$

$$\begin{aligned} &> \\ &> g := raRF(x, 3) \\ &g := \frac{2x^3 + 10x^2 + x + 9}{x^3 + 8x^2 + 7x + 4} \end{aligned} \quad (38)$$

$$\begin{aligned} &> evalf(SSS(g, x)) \\ &[1.094863281] \end{aligned} \quad (39)$$

$$\begin{aligned} &> Orb(g, x, 100.1, 1000, 1010) \\ &[1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281, \\ &1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281] \end{aligned} \quad (40)$$

$$\begin{aligned} &> Orb(g, x, 10.1, 1000, 1010) \\ &[1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281, \\ &1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281] \end{aligned} \quad (41)$$

$$\begin{aligned} &> Orb(g, x, -10.1, 1000, 1010) \\ &[1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281, \\ &1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281] \end{aligned} \quad (42)$$

$$\begin{aligned} &> Orb(g, x, -100.1, 1000, 1010) \\ &[1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281, \\ &1.094863281, 1.094863281, 1.094863281, 1.094863281, 1.094863281] \end{aligned} \quad (43)$$

$$\begin{aligned} &> \\ &> g := raRF(x, 3) \\ &g := \frac{7x^3 + x^2 + 4x + 6}{9x^3 + 5x^2 + 9x + 2} \end{aligned} \quad (44)$$

$$\begin{aligned} &> evalf(SSS(g, x)) \\ &[0.7927386281] \end{aligned} \quad (45)$$

$$\begin{aligned} &> Orb(g, x, 100.1, 1000, 1010) \\ &[0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, \\ &0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279] \end{aligned} \quad (46)$$

$$\begin{aligned} &> Orb(g, x, 10.1, 1000, 1010) \\ &[0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, \\ &0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279] \end{aligned} \quad (47)$$

0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279]

> $Orb(g, x, -10.1, 1000, 1010)$
[0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279] (48)

> $Orb(g, x, -100.1, 1000, 1010)$
[0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279, 0.7927386279] (49)

>
> $g := raRF(x, 3)$
$$g := \frac{4x^3 + 3x^2 + 4x + 9}{10x^3 + 4x^2 + 4x + 6}$$
 (50)

> $evalf(SSS(g, x))$
[0.8947709009] (51)

> $Orb(g, x, 100.1, 1000, 1010)$
[0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013] (52)

> $Orb(g, x, 10.1, 1000, 1010)$
[0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013] (53)

> $Orb(g, x, -10.1, 1000, 1010)$
[0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013] (54)

> $Orb(g, x, -100.1, 1000, 1010)$
[0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013, 0.8947709013] (55)

>
> $g := raRF(x, 3)$
$$g := \frac{2x^3 + 7x^2 + 2x + 8}{7x^3 + 5x^2 + 3x + 5}$$
 (56)

> $evalf(SSS(g, x))$
[0.9672041816] (57)

> $Orb(g, x, 100.1, 1000, 1010)$
[0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, 0.9672041817, 0.9672041817] (58)

> $Orb(g, x, 10.1, 1000, 1010)$

$$\left[\begin{array}{l} [0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, \\ 0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, 0.9672041817] \end{array} \right] \quad (59)$$

$$\begin{array}{l} \text{> } Orb(g, x, -10.1, 1000, 1010) \\ [0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, \\ 0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, 0.9672041817] \end{array} \quad (60)$$

$$\begin{array}{l} \text{> } Orb(g, x, -100.1, 1000, 1010) \\ [0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, \\ 0.9672041817, 0.9672041812, 0.9672041817, 0.9672041812, 0.9672041817] \end{array} \quad (61)$$

>

```
> read `DMB8.txt`
```

For a list of the Main procedures type: `Help8()`; for help with a specific procedure type: `Help6(ProcedureName)`; for example `Help6(RandomMC)`;

For a list of the other procedures type: `Help8a()`; for help with a specific procedure type: `Help6 (ProcedureName)`; for example `Help6(RandomMC)`; **(1)**

```
> Orb(1·x·(1 - x), x, 0.5, 2000, 2030)
```

[0.0004976675995, 0.0004974199265, 0.0004971724999, 0.0004969253194, 0.0004966783846, (2)
0.0004964316952, 0.0004961852508, 0.0004959390510, 0.0004956930954,
0.0004954473838, 0.0004952019157, 0.0004949566908, 0.0004947117087,
0.0004944669690, 0.0004942224714, 0.0004939782155, 0.0004937342010,
0.0004934904275, 0.0004932468947, 0.0004930036022, 0.0004927605496,
0.0004925177367, 0.0004922751630, 0.0004920328281, 0.0004917907318,
0.0004915488737, 0.0004913072534, 0.0004910658706, 0.0004908247249,
0.0004905838160, 0.0004903431435]

```
> Orb(2*x*(1-x), x, 0.5, 2000, 2030)
```

(3)

```
> Orb(2.5·x·(1 - x), x, 0.5, 2000, 2030)
```

(4)

```
> Orb(3.1·x·(1 - x), x, 0.5, 2000, 2030)
```

[0.5580141245, 0.7645665203, 0.5580141245, 0.7645665203, 0.5580141245, 0.7645665203,
0.5580141245, 0.7645665203, 0.5580141245, 0.7645665203, 0.5580141245, 0.7645665203,
0.5580141245, 0.7645665203, 0.5580141245, 0.7645665203, 0.5580141245, 0.7645665203,
0.5580141245, 0.7645665203, 0.5580141245, 0.7645665203, 0.5580141245, 0.7645665203,
0.5580141245, 0.7645665203, 0.5580141245, 0.7645665203, 0.5580141245, 0.7645665203,

(5)

0.5580141245]

> $Orb(3.2 \cdot x \cdot (1 - x), x, 0.5, 2000, 2030)$

[0.5130445091, 0.7994554906, 0.5130445091, 0.7994554906, 0.5130445091, 0.7994554906,
0.5130445091, 0.7994554906, 0.5130445091, 0.7994554906, 0.5130445091, 0.7994554906,
0.5130445091, 0.7994554906, 0.5130445091, 0.7994554906, 0.5130445091, 0.7994554906,
0.5130445091, 0.7994554906, 0.5130445091, 0.7994554906, 0.5130445091, 0.7994554906,
0.5130445091, 0.7994554906, 0.5130445091, 0.7994554906, 0.5130445091, 0.7994554906,
0.5130445091]

(6)

> $Orb(3.3 \cdot x \cdot (1 - x), x, 0.5, 2000, 2030)$

[0.4794270198, 0.8236032832, 0.4794270198, 0.8236032832, 0.4794270198, 0.8236032832,
0.4794270198, 0.8236032832, 0.4794270198, 0.8236032832, 0.4794270198, 0.8236032832,
0.4794270198, 0.8236032832, 0.4794270198, 0.8236032832, 0.4794270198, 0.8236032832,
0.4794270198, 0.8236032832, 0.4794270198, 0.8236032832, 0.4794270198, 0.8236032832,
0.4794270198, 0.8236032832, 0.4794270198, 0.8236032832, 0.4794270198, 0.8236032832,
0.4794270198]

(7)

> $Orb(3.5 \cdot x \cdot (1 - x), x, 0.5, 2000, 2030)$

[0.5008842111, 0.8749972637, 0.3828196827, 0.8269407062, 0.5008842111, 0.8749972637,
0.3828196827, 0.8269407062, 0.5008842111, 0.8749972637, 0.3828196827, 0.8269407062,
0.5008842111, 0.8749972637, 0.3828196827, 0.8269407062, 0.5008842111, 0.8749972637,
0.3828196827, 0.8269407062, 0.5008842111, 0.8749972637, 0.3828196827, 0.8269407062,
0.5008842111, 0.8749972637, 0.3828196827, 0.8269407062, 0.5008842111, 0.8749972637,
0.3828196827]

(8)

> # *For some values of k , the sequence doesn't converge to a single value but repeats the same values in a cycle eventually*

> read `DMB8.txt`

For a list of the Main procedures type: Help8(); for help with a specific procedure type: Help6 (ProcedureName); for example Help6(RandomMC);

For a list of the other procedures type: Help8a()); for help with a specific procedure type: Help6 (ProcedureName); for example Help6(RandomMC); (1)

> $f := \text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], k, x)$

$$f := \frac{x^9}{k} - \frac{36x^8}{k} + \frac{546x^7}{k} - \frac{4536x^6}{k} + \frac{22449x^5}{k} - \frac{67284x^4}{k} + \frac{118124x^3}{k} - \frac{109584x^2}{k} + \frac{40320x}{k} + x \quad (2)$$

> Help8(MakeNicePol)

MakeNicePol(L,k,x): inputs a set of numbers, outputs a polynomial having these fixed points. k is parameter you can play with. Try:

MakeNicePol([1,2,3],7,x); (3)

> Help8(SSS)

SSS(f,x): inputs a function f of x, outputs all the STABLE steady-states of the associated recurrence $a(n+1)=f(a(n))$. Try:

*SSS(5/2*x*(1-x),x);* (4)

> $\text{SSS}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 1, x), x)$
[] (5)

> $\text{SSS}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 500, x), x)$
[3, 5] (6)

> $\text{SSS}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 250, x), x)$
[] (7)

> $\text{SSS}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 375, x), x)$
[3, 5] (8)

> $\text{SSS}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 300, x), x)$
[] (9)

> $\text{SSS}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 350, x), x)$
[] (10)

> $\text{SSS}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 360, x), x)$
[] (11)

> $\text{SSS}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 367, x), x)$
[3, 5] (12)

> $\text{SSS}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 365, x), x)$
(13)

	$[3, 5]$	(13)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 363, x), x)$	
	$[3, 5]$	(14)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 361, x), x)$	
	$[3, 5]$	(15)
>	# 361 is the smallest k such that there are 2 SSS	
>	$\text{Orb}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 361, x), x, 3.4, 1000, 1010)$	
	$[3.0003249, 2.9996760, 3.0003166, 2.9996836, 3.0003200, 2.9996888, 3.0003030, 2.9996971, 3.0003073, 2.9996926, 3.0003042]$	(16)
>	$\text{Orb}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 361, x), x, 5.4, 1000, 1010)$	
	$[5.0005525, 4.9994615, 5.0005980, 4.9994259, 5.0006803, 4.9993623, 5.0005312, 4.9993682, 5.0006491, 4.9992884, 5.0006114]$	(17)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 1000, x), x)$	
	$[3, 5]$	(18)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 4000, x), x)$	
	$[1, 3, 5, 7]$	(19)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2000, x), x)$	
	$[3, 5]$	(20)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 3000, x), x)$	
	$[1, 3, 5, 7]$	(21)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2500, x), x)$	
	$[3, 5]$	(22)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2750, x), x)$	
	$[1, 3, 5, 7]$	(23)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2600, x), x)$	
	$[1, 3, 5, 7]$	(24)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2550, x), x)$	
	$[1, 3, 5, 7]$	(25)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2525, x), x)$	
	$[1, 3, 5, 7]$	(26)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2515, x), x)$	
	$[3, 5]$	(27)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2520, x), x)$	
	$[3, 5]$	(28)
>	$SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2522, x), x)$	
	$[1, 3, 5, 7]$	(29)

> $SSS(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2521, x), x)$
 $[1, 3, 5, 7]$ (30)

> # 2521 is the smallest k such that there are 4 SSS

> $\text{Orb}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2521, x), x, 1.1, 1000, 1010)$
 $[1.00446666, 0.99560040, 1.00445773, 0.99560910, 1.00444881, 0.99561775, 1.00443992,$ (31)
 $0.99562636, 1.00443108, 0.99563496, 1.00442225]$

> $\text{Orb}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2521, x), x, 3.1, 1000, 1010)$
 $[2.99999944, 2.99999942, 2.99999928, 2.99999940, 2.99999914, 2.99999952, 2.99999988,$ (32)
 $3.00000010, 3.00000054, 2.99999921, 2.99999851]$

> $\text{Orb}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2521, x), x, 5.1, 1000, 1010)$
 $[4.99998819, 5.00000686, 4.99999614, 4.99999196, 5.00000793, 4.99999232, 4.99998305,$ (33)
 $4.99999152, 4.99998645, 4.99997930, 4.99997679]$

> $\text{Orb}(\text{MakeNicePol}([1, 2, 3, 4, 5, 6, 7, 8], 2521, x), x, 7.1, 1000, 1010)$
 $[7.0092564, 6.9905882, 7.0092033, 6.9905529, 7.0092564, 6.9905882, 7.0092033, 6.9905529,$ (34)
 $7.0092564, 6.9905882, 7.0092033]$

>