

Homework for Lecture 23 of Dr. Z.'s Dynamical Models in Biology class

Email the answers (either as .pdf file and/or .txt file) to

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by 8:00pm Monday, Dec. 8, 2025.

Subject: hw21

with an attachment hw23FirstLast.pdf and/or hw23FirstLast.txt

1. In the Maple package DMB.txt run

`ExpGenLotka(2,50);`

ten times.

In how many cases did all the sepecies survive? In how many cases was there agreement with the positive stable equilibrium points, and between the three initial conditions?

2. In the Maple package DMB.txt run

`ExpGenLotka(3,50);`

ten times.

In how many cases did all the sepecies survive? In how many cases was there agreement with the positive stable equilibrium points, and between the three initial conditions?

3. In the Maple package DMB.txt run

`ExpGenLotka(4,50);`

ten times.

In how many cases did all the sepecies survive? In how many cases was there agreement with the positive stable equilibrium points, and between the three initial conditions?

4. In the Maple package DMB.txt run

`ExpGenLotka(5,50);`

ten times.

In how many cases did all the sepecies survive? In how many cases was there agreement with the positive stable equilibrium points, and between the three initial conditions?

1)

The Equilibrium points are

{[0, 0], [0, 0.8474576271], [0.5208333333, 0], [0.5220646178, -0.01970055162]}

The stable Equilibrium points are

{[0.5208333333, 0]}

at time $t=$, 50, with initial conditions, [0.5, 0.5], the ultimate behavior is

[0.5189098018, 0.02997972993]

and with initial conditions, [0.1, 0.1]

[0.5190809992, 0.02735103168]

and with initial conditions, $\left[\frac{1}{2}, 1\right]$

[0.5188099176, 0.03150983934]

The Equilibrium points are

{[0, 0], [0, 1.162790698], [0.2104770814, 0.8886810103], [2.777777778, 0.]}

The stable Equilibrium points are

{[0, 1.162790698], [2.777777778, 0.]}

at time $t=$, 50, with initial conditions, [0.5, 0.5], the ultimate behavior is[2.777777723, 7.455287790 $\times 10^{-15}$]

and with initial conditions, [0.1, 0.1]

[2.777777723, 2.596930501 $\times 10^{-15}$]and with initial conditions, $\left[\frac{1}{2}, 1\right]$ [2.777777723, 2.263413087 $\times 10^{-12}$]

The Equilibrium points are

{[0, 0], [0, 0.6493506494], [0.5244755245, 0.5880483153], [1.086956522, 0.]}

The stable Equilibrium points are

{[0.5244755245, 0.5880483153]}

at time $t=$, 50, with initial conditions, [0.5, 0.5], the ultimate behavior is

[0.5301601430, 0.5836721247]

and with initial conditions, [0.1, 0.1]

[0.6311761384, 0.4963779390]

and with initial conditions, $\left[\frac{1}{2}, 1\right]$

[0.5092912292, 0.5992974787]

{[0, 0], [0, 4.166666667], [0.6410256410, 0], [1.103565365, -0.7074136955]}

The stable Equilibrium points are

{[0, 4.166666667], [1.103565365, -0.7074136955]}

at time $t=$, 50, with initial conditions, [0.5, 0.5], the ultimate behavior is[3.521629977 $\times 10^{-46}$, 4.166666592]

and with initial conditions, [0.1, 0.1]

[1.294779416 $\times 10^{-43}$, 4.166666592]and with initial conditions, $\left[\frac{1}{2}, 1\right]$ [3.825889182 $\times 10^{-48}$, 4.166666592]

The Equilibrium points are

{[0, 0], [0, 0.694444444], [0.6756756757, 0], [0.8389261745, -0.4474272931]}

The stable Equilibrium points are

{[0.6756756757, 0.]}

at time $t=$, 50, with initial conditions, [0.5, 0.5], the ultimate behavior is[0.6756755828, 1.531484977 $\times 10^{-7}$]

and with initial conditions, [0.1, 0.1]

[0.6756754648, 3.492703019 $\times 10^{-7}$]and with initial conditions, $\left[\frac{1}{2}, 1\right]$ [0.6756755522, 2.046475062 $\times 10^{-7}$]

The Equilibrium points are

{[0, 0], [0, 0.781250000], [2.532833021, 0.1876172608], [2.631578947, 0.]}

The stable Equilibrium points are

{[2.532833021, 0.1876172608]}

at time $t=$, 50, with initial conditions, [0.5, 0.5], the ultimate behavior is

[2.505751554, 0.2348318993]

and with initial conditions, [0.1, 0.1]

[2.526871595, 0.1981735395]

and with initial conditions, $\left[\frac{1}{2}, 1\right]$

[2.499420252, 0.2455921211]

> ExpGenLotka(2, 50);

a) survived

agreement
between
I.C.
↳ similar
values

> ExpGenLotka(2, 50);

> ExpGenLotka(2, 50);

match

All
survive

{[0, 0], [0, 0.9615384615], [1.250000000, 0.], [1.966292135, -1.685393258]}

The stable Equilibrium points are

{[1.250000000, 0.]}

at time $t=$, 50, with initial conditions, [0.5, 0.5], the ultimate behavior is

[1.249999883, 2.412660284 $\times 10^{-9}$]

and with initial conditions, [0.1, 0.1]

[1.249999878, 1.553914733 $\times 10^{-8}$]

and with initial conditions, $\left[\frac{1}{2}, 1\right]$

[1.249999883, 3.636927514 $\times 10^{-9}$]

The Equilibrium points are

{[-1.574074074, 2.962962963], [0, 0.], [0, 1.388888889], [0.500000000, 0.]}

The stable Equilibrium points are

{[0, 1.388888889]}

at time $t=$, 50, with initial conditions, [0.5, 0.5], the ultimate behavior is

[3.300988967 $\times 10^{-17}$, 1.388888810]

and with initial conditions, [0.1, 0.1]

[3.632411978 $\times 10^{-16}$, 1.388888810]

and with initial conditions, $\left[\frac{1}{2}, 1\right]$

[6.915095200 $\times 10^{-18}$, 1.388888810]

The Equilibrium points are

{[0, 0.], [0, 10.], [1.785714286, 0.], [41.17647059, -14.70588235]}

The stable Equilibrium points are

{[0, 10.], [41.17647059, -14.70588235]}

at time $t=$, 50, with initial conditions, [0.5, 0.5], the ultimate behavior is

[6.440307627 $\times 10^{-168}$, 9.999999894]

and with initial conditions, [0.1, 0.1]

[2.352550413 $\times 10^{-154}$, 9.999999894]

and with initial conditions, $\left[\frac{1}{2}, 1\right]$

[4.074199769 $\times 10^{-174}$, 9.999999894]

The Equilibrium points are

{[-1.356852103, 1.797829037], [0, 0.], [0, 0.5102040816], [1.250000000, 0.]}

The stable Equilibrium points are

{[1.250000000, 0.]}

at time $t=$, 50, with initial conditions, [0.5, 0.5], the ultimate behavior is

[1.249998775, 5.741105880 $\times 10^{-7}$]

and with initial conditions, [0.1, 0.1]

[1.24999517, 2.204198505 $\times 10^{-7}$]

and with initial conditions, $\left[\frac{1}{2}, 1\right]$

[1.249996443, 1.667139436 $\times 10^{-6}$]

• # cases where all species survived = 3

• # times there was agreement w/ positive stable equ pts = 4

• # times there was agreement between 3 initial conditions = 4

For a list of the Continuous Dynamical Models procedures type: `HelpC()`; for help with a specific procedure type: `Help(ProcedureName)`; for example `Help(Feig)`:

> `ExpGenLotka(3, 50);`

The Equilibrium points are

$\{[-1.569373440, 2.205445250, -0.08322434907], [-1.553166069, 2.090800478, 0], [0, 0, 0], [0, 0, 25], [0, 0.7241063245, 0.01833180568], [0, 0.7462686567, 0], [0.7498500300, 0, 0.6298740252], [2.173913043, 0, 0]\}$

The stable Equilibrium points are

$\{[-1.569373440, 2.205445250, -0.08322434907], [0, 0, 25], [2.173913043, 0, 0]\}$

at time $t=50$, with initial conditions, $[0.5, 0.5, 0.5]$, the ultimate behavior is

$[2.170935716, 1.339759022 \times 10^{-26}, 0.000986602992]$

and with initial conditions, $[0.1, 0.1, 0.1]$

$[2.173837281, 1.202560617 \times 10^{-28}, 0.00002509691146]$

and with initial conditions, $\left[\frac{1}{3}, \frac{2}{3}, 1\right]$

$[2.487416341 \times 10^{-173}, 2.526112754 \times 10^{-358}, 22.23601387]$

The Equilibrium points are

$\{[-0.6818181818, 4.924242424, 0], [0, -10.41666667, 37.50000000], [0, 0, 0], [0, 0.2173913043], [0, 2.083333333, 0], [0.1800720288, 0, 1.680672269], [0.4129734085, -0.1152744203, 1.433655654], [1.428571429, 0, 0]\}$

The stable Equilibrium points are

$\{[-0.6818181818, 4.924242424, 0], [0, -10.41666667, 37.50000000], [1.428571429, 0, 0]\}$

at time $t=50$, with initial conditions, $[0.5, 0.5, 0.5]$, the ultimate behavior is

$[1.419157437, 7.185853403 \times 10^{-15}, 2.676216565 \times 10^{-11}]$

and with initial conditions, $[0.1, 0.1, 0.1]$

$[1.297471798, 3.887689892 \times 10^{-6}, 2.412369628 \times 10^{-9}]$

and with initial conditions, $\left[\frac{1}{3}, \frac{2}{3}, 1\right]$

$[1.409030965, 2.475792473 \times 10^{-12}, 3.053392176 \times 10^{-10}]$

The Equilibrium points are

$\{[-0.01521606817, 0.9890444309, 0], [0, 0, 0], [0, 0.1250000000], [0, 0.9803921569, 0], [0, 1.005981512, -0.4350190321], [0.07504344621, 0.9641546860, -0.4493829761], [0.3947368421, 0, 0.8059210526], [0.5319148936, 0, 0]\}$

The stable Equilibrium points are

$\{[0, 0.9803921569, 0]\}$

at time $t=50$, with initial conditions, $[0.5, 0.5, 0.5]$, the ultimate behavior is

$[0.01263777132, 0.9725043212, 0.00004051307062]$

and with initial conditions, $[0.1, 0.1, 0.1]$

$[0.01615395280, 0.9701603897, 0.00001396370501]$

and with initial conditions, $\left[\frac{1}{3}, \frac{2}{3}, 1\right]$

$[0.01107189505, 0.9735219694, 0.00003587365085]$

The Equilibrium points are

$\{[0, 0, 0], [0, 0, 1], [0, 0.03559563360, 0.9373516849], [0, 0.555555556, 0], [0.2227171492, 0, 0.8351893096], [0.4826538612, 0.2462269698, 0.2094766758], [0.6244109331, 0.2827521206, 0], [0.9615384615, 0, 0]\}$

The stable Equilibrium points are

$\{[0, 0.555555556, 0], [0.2227171492, 0, 0.8351893096]\}$

at time $t=50$, with initial conditions, $[0.5, 0.5, 0.5]$, the ultimate behavior is

$[5.570115013 \times 10^{-64}, 5.555555208, 8.028999371 \times 10^{-88}]$

and with initial conditions, $[0.1, 0.1, 0.1]$

$[1.668081084 \times 10^{-44}, 5.555501899, 4.886069652 \times 10^{-69}]$

and with initial conditions, $\left[\frac{1}{3}, \frac{2}{3}, 1\right]$

$[1.303277672 \times 10^{-68}, 5.55555440, 1.998589910 \times 10^{-91}]$

ExpGenLotka(3, 50);

The Equilibrium points are

$\{[-1.504424779, 0, 1.799410029], [-1.361111111, -2.313492063, 2.898148148], [0, -1.495016611, 1.937984496], [0, 0, 0], [0, 0, 1.190476190], [0, 0.8928571429, 0], [0.09633911368, 0.8670520231, 0], [0.6410256410, 0, 0]\}$

The stable Equilibrium points are

$\{[0, 0, 1.190476190]\}$

at time $t=50$, with initial conditions, $[0.5, 0.5, 0.5]$, the ultimate behavior is

$[4.490317784 \times 10^{-19}, 2.270247180 \times 10^{-9}, 1.190379535]$

and with initial conditions, $[0.1, 0.1, 0.1]$

$[2.686779155 \times 10^{-14}, 1.048175637 \times 10^{-6}, 1.188986057]$

and with initial conditions, $\left[\frac{1}{3}, \frac{2}{3}, 1\right]$

$[1.336042711 \times 10^{-21}, 7.887464056 \times 10^{-11}, 1.190460799]$

ExpGenLotka(3, 50);

The Equilibrium points are

$\{[-10.07604563, 3.041825095, 0], [-1.360544218, 0, 1.870748299], [-0.2173646828, 0.3926340926, 0.4951934852], [0, -0.8522727273, 1.014610390], [0, 0, 0], [0, 0, 0.5102040816], [0, 1.515151515, 0], [2.380952381, 0, 0]\}$

The stable Equilibrium points are

$\{[-1.360544218, 0, 1.870748299], [0, 1.515151515, 0]\}$

at time $t=50$, with initial conditions, $[0.5, 0.5, 0.5]$, the ultimate behavior is

$[3.213217917 \times 10^{-22}, 1.515151413, 1.326396896 \times 10^{-10}]$

and with initial conditions, $[0.1, 0.1, 0.1]$

$[1.745127132 \times 10^{-20}, 1.515151413, 3.808195337 \times 10^{-10}]$

and with initial conditions, $\left[\frac{1}{3}, \frac{2}{3}, 1\right]$

$[6.499788911 \times 10^{-22}, 1.515151413, 4.597429474 \times 10^{-10}]$

• `ExpGenLotka(3, 50);`

The Equilibrium points are

$\{[-0.1667284179, 0, 1.130048166], [0, -0.9391771020, 1.319320215], [0, 0, 0], [0, 0, 1], [0, 0.6578947368, 0], [0.08196721311, 0.6147540984, 0], [0.4092405552, -0.6485357774, 0.9012945313], [0.5000000000, 0, 0]\}$

The stable Equilibrium points are

$\{[0, 0, 1]\}$

at time $t= 50$, with initial conditions, $[0.5, 0.5, 0.5]$, the ultimate behavior is

$[0.00004608033477, 8.328159460 \times 10^{-7}, 0.9999559754]$

and with initial conditions, $[0.1, 0.1, 0.1]$

$[0.00009453898335, 7.186145671 \times 10^{-7}, 0.9999101640]$

and with initial conditions, $\left[\frac{1}{3}, \frac{2}{3}, 1\right]$

$[0.0002507449630, 6.352220998 \times 10^{-7}, 0.9999759542]$

• `ExpGenLotka(3, 50);`

The Equilibrium points are

$\{[-0.5943536404, 1.560178306, 0], [-0.1869060594, 0.7442780933, 0.2705596665], [0, 0, 0], [0, 0, 1.086956522], [0, 0.7246376812, 0], [0, 1.465201465, -0.8241758242], [0.7936507936, 0, 0.4313319531], [3.846153846, 0, 0]\}$

The stable Equilibrium points are

$\{[-0.5943536404, 1.560178306, 0], [0, 0, 1.086956522], [3.846153846, 0, 0]\}$

at time $t= 50$, with initial conditions, $[0.5, 0.5, 0.5]$, the ultimate behavior is

$[1.567945019 \times 10^{-13}, 0.03416802557, 1.039914366]$

and with initial conditions, $[0.1, 0.1, 0.1]$

$[7.917811303 \times 10^{-18}, 0.01251869442, 1.069728425]$

and with initial conditions, $\left[\frac{1}{3}, \frac{2}{3}, 1\right]$

$[8.906618458 \times 10^{-13}, 0.09594490233, 0.9546785552]$

• `ExpGenLotka(3, 50);`

The Equilibrium points are

$\{[0, 0, 0], [0, 0, 0.9090909091], [0, 0.1611374408, 0.6161137441], [0, 1.428571429, 0], [0.2152176564, 0.005487135715, 0.5273747104], [0.2187500000, 0, 0.5312500000], [0.6336939722, 0.4327666151, 0], [1.851851852, 0, 0]\}$

The stable Equilibrium points are

$\{[0, 0, 0.9090909091], [0, 1.428571429, 0], [1.851851852, 0, 0]\}$

at time $t= 50$, with initial conditions, $[0.5, 0.5, 0.5]$, the ultimate behavior is

$[8.762401328 \times 10^{-20}, 1.428571365, 5.362429701 \times 10^{-10}]$

and with initial conditions, $[0.1, 0.1, 0.1]$

$[4.847190098 \times 10^{-19}, 1.428571365, 1.772378037 \times 10^{-10}]$

and with initial conditions, $\left[\frac{1}{3}, \frac{2}{3}, 1\right]$

$[7.311639811 \times 10^{-18}, 1.428571151, 5.068568484 \times 10^{-8}]$

The Equilibrium points are

$\{[-0.3253796095, 0, 2.422270427], [0, 0, 0], [0, 0, 2.083333333], [0, 0.3972602740, 0.5273972603], [0, 2.941176471, 0], [0.05065130858, 0.3921951431, 0.4944739097], [0.5434782609, 0, 0], [1.137270551, -0.7382282522, 0]\}$

The stable Equilibrium points are

$\{[0, 0, 2.083333333], [0, 2.941176471, 0]\}$

at time $t= 50$, with initial conditions, $[0.5, 0.5, 0.5]$, the ultimate behavior is

$[4.504041613 \times 10^{-6}, 1.149774671 \times 10^{-44}, 2.083326705]$

and with initial conditions, $[0.1, 0.1, 0.1]$

$[1.762291592 \times 10^{-42}, 2.941176420, 6.988269436 \times 10^{-71}]$

and with initial conditions, $\left[\frac{1}{3}, \frac{2}{3}, 1\right]$

$[1.559787299 \times 10^{-6}, 7.299556138 \times 10^{-49}, 2.083331033]$

•

• # cases where all species survived - 0

• # times there was agreement w/ positive stable equ pts = 0

• # times there was agreement between 3 initial conditions = 2

3

► $\text{ExpGenLotka}(4, 50);$

The Equilibrium points are

$\{[-0.5044625534, 0, 0, 1.416375631], [-0.4756292265, 0.02507711212, 0, 1.353746103], [0, -0.3833865815, 0, 1.118210863], [0, 0, 0, 0], [0, 0, 0.7462686567], [0, 0, 1.315789474, 0], [0, 0, 2.035830619, -0.6514657980], [0, 0.2071325648, 2.210914986, -0.9726224784], [0, 0.9615384615, 0.4807692308, 0], [0, 1.666666667, 0, 0], [0.2127802165, -0.2155726078, 0.027041517, 0], [0.2139343239, -0.2653956437, 1.129625715, -0.05600329675], [0.2633242048, 0, 0.7267748051, 0], [0.344698987, 0, 0.9371698668, -0.3550463412], [0.6797583082, 0.4657603223, 0, 0], [3.125000000, 0, 0, 0]\}$

The stable Equilibrium points are

$\{[0, 0, 1.315789474, 0], [0, 1.666666667, 0, 0], [3.125000000, 0, 0, 0]\}$

at time $t=50$, with initial conditions, [0.5, 0.5, 0.5, 0.5], the ultimate behavior is

$[1.414585828 \times 10^{-20}, 0.9052415732, 0.5194185449, 4.678202092 \times 10^{-17}]$

and with initial conditions, [0.1, 0.1, 0.1, 0.1]

$[3.679242274 \times 10^{-23}, 1.524089485, 0.09690621852, 5.991695141 \times 10^{-11}]$

and with initial conditions, $\left[\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1\right]$

► $\text{ExpGenLotka}(4, 50);$

The Equilibrium points are

$\{[-2.858844550, 1.893488187, 0, 2.109390510], [-2.221866688, 1.484410935, 1.020938744, 0], [-1.578450716, 0.9708043808, -1.791484373, 4.896914586], [-0.7931034483, 0, -2.741379310, 14.65517241], [0, -4.166666667, 0, 8.333333333], [0, -3.826530612, 4.336734694, 0], [0, -2.083333333, 0.208333333, 8.333333333], [0, 0, -22.2222222, 38.8888889], [0, 0, 0, 0], [0, 1.282051282], [0, 0, 1.315789474, 0], [0, 0.5102040816, 0, 0], [0.3481012658, 0, 0.7911392405], [1.666666667, 0, 0, 0], [2.676240209, -1.892950392, 0, 0], [11.77777778, 0, -3.333333333, 0]\}$

The stable Equilibrium points are

$\{[0, 0, 1.315789474, 0], [11.77777778, 0, -3.333333333, 0]\}$

at time $t=50$, with initial conditions, [0.5, 0.5, 0.5, 0.5], the ultimate behavior is

$[2.307322184 \times 10^{-16}, 4.858824557 \times 10^{-15}, 1.312710791, 0.003523227801]$

and with initial conditions, [0.1, 0.1, 0.1, 0.1]

$[1.959150851 \times 10^{-14}, 8.072782350 \times 10^{-14}, 1.314034799, 0.002007756769]$

and with initial conditions, $\left[\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1\right]$

► $\text{ExpGenLotka}(4, 50);$

The Equilibrium points are

$\{[-3.045011873, 1.464209635, 2.479451190, -0.3120608685], [-2.077027651, 1.135343457, 1.721451290, 0], [0, -23.6486485, 21.62162162, 0], [0, -0.582955776, 1.000320102, 0.6414360288], [0, 0, 0, 0], [0, 0, 0, 3.571428571], [0, 0, 0.8942457232, 0.5054432348], [0, 0, 2.272727273, 0], [0, 0.2403846154, 0, 3.365384615], [0, 0.6097560976, 0, 0], [0.09861932939, 0.4930966469, 0, 0], [0.1998957066, 0.02607335303, 0, 3.16356835], [0.5154639175, 0, 0, 2.577319588], [1.242690058, 0, 2.046783626, 0], [1.257056831, 0, 0.1298456906, 0.7019194580], [1.562500000, 0, 0, 0]\}$

The stable Equilibrium points are

$\{[0, 0.2403846154, 0, 3.365384615], [0.5154639175, 0, 0, 2.577319588], [1.242690058, 0, 2.046783626, 0]\}$

at time $t=50$, with initial conditions, [0.5, 0.5, 0.5, 0.5], the ultimate behavior is

$[1.265165365, 0.00001022126680, 1.963570147, 0.006738877078]$

and with initial conditions, [0.1, 0.1, 0.1, 0.1]

$[1.242691056, 5.533931855 \times 10^{-10}, 2.046782480, 2.617927092 \times 10^{-8}]$

and with initial conditions, $\left[\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1\right]$

$[0.0001181265093, 0.2552530434, 4.647815736 \times 10^{-24}, 3.349250636]$

► $\text{ExpGenLotka}(4, 50);$

The Equilibrium points are

$\{[-6.707317073, 0, 4.268292683, 0], [-2.836833181, 0, 1.878179210, 0.5347593583], [-1.011286046, 0.5865928342, 1.136816913, 0], [-0.5078775043, 3.911737373, 3.013766722, -4.391519526], [-0.2123896874, -0.9362484179, 0, 1.558680236], [0, -0.4359197908, 0, 1.002615519], [0, 0, 0, 0], [0, 0, 0.5617977528], [0, 0, 1.724137931, 0], [0, 0, 2.094522019, -0.214822712], [0, 0.746286567, 0, 0], [0, 1.996672213, -1.580698835, 0], [0, 6.218716821, 3.617473078, -7.068102533], [0.8833922261, 0, 0, 0.3533568905], [1.282051282, 0, 0, 0], [1.350048216, -0.2410800386, 0, 0]\}$

The stable Equilibrium points are

$\{[0, 0, 1.724137931, 0]\}$

at time $t=50$, with initial conditions, [0.5, 0.5, 0.5, 0.5], the ultimate behavior is

$[3.923202202 \times 10^{-13}, 2.365266167 \times 10^{-10}, 1.583092687, 0.03916867663]$

and with initial conditions, [0.1, 0.1, 0.1, 0.1]

$[0.0001093168990, 1.592039810 \times 10^{-6}, 1.126505859, 0.1842244700]$

and with initial conditions, $\left[\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1\right]$

$[4.691065079 \times 10^{-16}, 6.418315809 \times 10^{-12}, 1.635957352, 0.02363032341]$

► $\text{ExpGenLotka}(4, 50);$

The Equilibrium points are

$\{[-50, 0, 50, 0], [0, -0.6503744580, 0, 0.9262908948], [0, -0.6176890391, -0.3412465342, 1.127918232], [0, 0, -0.1925254813, 0.6568516421], [0, 0, 0, 0], [0, 0, 0.5319148936], [0, 0, 16.66666667, 0], [0, 0.8034026465, 1.134215501, 0], [0, 5, 0, 0], [0.07096551460, 0, -0.2167325175, 0.6559515133], [0.2643948296, 0, 0, 0.4700352526], [0.3760373444, 0.816908137, 0.6224066390, 0], [0.6214745670, 0.1722158439, 0, 0.2820346428], [0.625000000, 1.87500000, 0, 0], [0.7638715681, 0.3949831171, -0.3579894741, 0.3459377207], [3.151789474, 0, 0, 0]\}$

The stable Equilibrium points are

$\{[0, -0.6176890391, -0.3412465342, 1.127918232], [0, 0, 16.66666667, 0], [0, 5, 0, 0]\}$

at time $t=50$, with initial conditions, [0.5, 0.5, 0.5, 0.5], the ultimate behavior is

$[1.111804961 \times 10^{-165}, 2.540015156 \times 10^{-88}, 16.66666607, 7.505675392 \times 10^{-120}]$

and with initial conditions, [0.1, 0.1, 0.1, 0.1]

$[2.819128146 \times 10^{-180}, 2.618587036 \times 10^{-94}, 16.66666607, 4.368871484 \times 10^{-110}]$

and with initial conditions, $\left[\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1\right]$

$[0.07977229223, 4.301122253, 1.242937167 \times 10^{-29}, 7.051478025 \times 10^{-15}]$

► $\text{ExpGenLotka}(4, 50);$

The Equilibrium points are

$\{[-4629629630, 4.282407407, 0, 0], [0, -138.4615385, 119.2307692, 0], [0, -2.08333333, 0, 2.08333333], [0, -0.9193716984, 0.1196130291, 1.560932491], [0, 0, 0, 0], [0, 0, 1.724137931], [0, 0, 0.5494505494, 0], [0, 0, 0.7243877199, -0.2242152466], [0, 3.125000000, 0, 0], [0.108492867, 0, 0.5017629509, 0], [0.2674954930, 0, 0.3400763269, 0.1176511906], [0.3967917162, 0.6821846885, 0, 0.5803344084], [0.6405933918, 0, 0, 0.0674308834], [0.6495306494, 0, 0, 0], [1.016344882, 0.3998738055, -0.4727551183, 0.2982642766], [1.258222897, 0.9108439667, -0.7843378602, 0]\}$

The stable Equilibrium points are

$\{[0, -138.4615385, 119.2307692, 0], [0, 3967917162, 0.6821846885, 0, 0.5803344084]\}$

at time $t=50$, with initial conditions, [0.5, 0.5, 0.5, 0.5], the ultimate behavior is

$[0.4057094375, 0.6569651593, 9.108602624 \times 10^{-14}, 0.5696397557]$

and with initial conditions, [0.1, 0.1, 0.1, 0.1]

$[0.4412275469, 0.5113572135, 4.099044568 \times 10^{-13}, 0.5754393742]$

and with initial conditions, $\left[\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1\right]$

$[0.3696917323, 0.7805416054, 8.073775744 \times 10^{-12}, 0.5878062120]$

> ExpGenLotka(4, 50);

The Equilibrium points are

([-1.256281407, 0, 0, 1.356783920], [-0.8191049388, 0, 1.260842278, 0.4811638049], [0, -0.6723716381, 0, 1.079869601], [0, -0.5081292361, -0.2939831178, 1.181338101], [0, 0, -0.08375209380, 0.8793969849], [0, 0, 0, 0], [0, 0, 0.8333333333], [0, 0, 0.6666666667, 0], [0, 0.009790483650, 0.665752882, 0], [0, 0.6666666667, 0, 0], [0.1352296263, -0.4322366762, -0.4845686647, 1.201987203], [0.3863119348, 0.2524551961, 0.1692282084, 0], [0.9615384615, 0, 0, 0], [1.709401709, -0.4273504274, 0, 0], [6.356837607, -2.110042735, 0, -1.041666667, 0], [13.28125000, 0, -15.62500000, 0])

The stable Equilibrium points are
([0, 0, 0, 0.8333333333], [6.356837607, -2.110042735, 0, -1.041666667])
at time $t=50$, with initial conditions, [0.5, 0.5, 0.5, 0.5], the ultimate behavior is
[8.231414142 $\times 10^{-8}$, 3.584472476 $\times 10^{-11}$, 0.003505034505, 0.8312495747]

and with initial conditions, [0.1, 0.1, 0.1, 0.1]

[1.322833831 $\times 10^{-7}$, 1.257653608 $\times 10^{-12}$, 0.004463497440, 0.8306771989]
and with initial conditions, $\left[\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1\right]$

[2.531265944 $\times 10^{-8}$, 1.089477809 $\times 10^{-13}$, 0.004023095570, 0.8309403926]

> ExpGenLotka(4, 50);

The Equilibrium points are

([-0.396148556, 9.697386520, 0, -7.565337001], [-1.087278950, 1.707929264, 0.2304620650, -0.8077581289], [-0.5694423902, 0.7617216388, 0.3697677858, 0], [-0.1831501832, 0.7326007326, 0, 0], [-0.1300390117, 0, 0.4765547311, 0.6463703817], [0, -0.2255690270, 0.5157946933, 0.8113679011], [0, 0, 0, 0], [0, 0, 1.470588235], [0, 0, 0.6250000000, 0], [0, 0, 0.7189542484, -0.3267973856], [0, 0.335952215, 0.4402224282, 0], [0, 0.4182156134, 0, 0.3020446097], [0, 0.6097560976, 0, 0], [0.3000923361, 0, 0, 0.6232686981], [0.3333333333, 0, 0, 0], [3.608247423, 0, -0.4123711340, 0, 0])

The stable Equilibrium points are
([-1.087278950, 1.707929264, 0.2304620650, -0.8077581289], [-0.1300390117, 0, 0.4765547311, 0.6463703817], [0.3333333333, 0, 0, 0])
at time $t=50$, with initial conditions, [0.5, 0.5, 0.5, 0.5], the ultimate behavior is
[3.333333006, 1.543919566 $\times 10^{-32}$, 4.206374054 $\times 10^{-8}$, 2.715970445 $\times 10^{-55}$]

and with initial conditions, [0.1, 0.1, 0.1, 0.1]

[3.333331359, 4.787076447 $\times 10^{-29}$, 2.692139426 $\times 10^{-7}$, 9.132737852 $\times 10^{-50}$]
and with initial conditions, $\left[\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1\right]$

[3.333331373, 3.739572829 $\times 10^{-29}$, 2.678013089 $\times 10^{-7}$, 1.391725983 $\times 10^{-49}$]

The Equilibrium points are

([-5.178571429, 0, 0, 7.500000000], [-0.2311991463, -0.8587969120, 1.043112095, 0.7111588959], [0, -0.3274670139, 0.6204638159, 0.4663053678], [0, 0, 0, 0], [0, 0, 0.9090909091], [0, 0, 0.6097560976, 0, 0], [0, 1.063829787, 0, 0], [0, 1.192052980, 0, -0.06622516556], [0, 0, 2.625437573, -1.983663944, 0], [0.6785214536, -0.3657573532, 0.7890106541, 0], [0.9314985123, 0, 2.353259400, -2.972004328], [1.444444444, 0, 0.2222222222, 0], [1.770428016, -2.665369650, 0, 0.8365758755], [1.785714286, 0, 0, 0], [2.246543779, -1.612903226, 0, 0])

The stable Equilibrium points are
([-5.178571429, 0, 0, 7.500000000], [1.444444444, 0, 0.2222222222, 0])
at time $t=50$, with initial conditions, [0.5, 0.5, 0.5, 0.5], the ultimate behavior is
[1.368022132, 6.523209556 $\times 10^{-7}$, 0.2466909006, 0.00004974868319]

and with initial conditions, [0.1, 0.1, 0.1, 0.1]

[1.272724838, 0.0006333214482, 0.2726459119, 0.001050995617]
and with initial conditions, $\left[\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1\right]$

[1.260625586, 3.489063843 $\times 10^{-6}$, 0.2777152700, 0.001211678801]

> ExpGenLotka(4, 50);

The Equilibrium points are

([-0.3360961235, 0, 0.4244713988, 0.4856889070], [-0.06429096253, 0, 0, 0.6612784717], [-0.01793721973, 0, 0.6188340807, 0], [0, -2.500000000, 0, 3.750000000], [0, -2.238781844, 1.795874822, 2.623496702], [0, 0, 0, 0], [0, 0, 0.6578947368], [0, 0, 0.3981216823, 0.4797876684], [0, 0, 0.6172839506, 0], [0, 0.8196721311, 0, 0], [0, 1.003224651, -0.4478681476, 0], [0.2437592832, 0.2433999329, 0, 0.3440180154], [0.2496157168, 0.3340386273, 0.1699994779, 0.1555516306], [0.3506319568, 0.3332424845, 0.2331694153, 0], [0.6413612565, 0.1047120419, 0, 0], [0.6578947368, 0, 0.1120428019, 0])

The stable Equilibrium points are
([0, -2.238781844, 1.795874822, 2.623496702], [0.2496157168, 0.3340386273, 0.1699994779, 0.1555516306])
at time $t=50$, with initial conditions, [0.5, 0.5, 0.5, 0.5], the ultimate behavior is
[0.2562740946, 0.4338734324, 0.1032287819, 0.08692503903]
and with initial conditions, [0.1, 0.1, 0.1, 0.1]

[0.3279452003, 0.2912329466, 0.1654058591, 0.1338659866]
and with initial conditions, $\left[\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1\right]$

[0.3509488616, 0.3719697803, 0.09260953566, 0.06862130035]

{ survived

• # cases where all species survived - 1

• # times there was agreement w/ positive stable equ pts = 0

• # times there was agreement between 3 initial conditions = 1


```
> ExpGenLotka(5, 50);
```

The Equilibrium points are

The stable Equilibrium points are
 $\{[0, 0, 1.724137931, 0, 0], [0, 1.260053619, 0, 0.1876675603, 0]\}$
 at time $t=50$, with initial conditions, $[0.5, 0.5, 0.5, 0.5, 0.5]$, the ultimate behavior is
 $5.513157 \cdot 10^{-16} - 1.258618672 \cdot 10^{-22}i, 0.678525882 \cdot 10^{-22} - 2.091260110 \cdot 2.951122035 \cdot 10^{-22}i$

and with initial conditions, $[0.1, 0.1, 0.1, 0.1]$

$$[4.975752202 \times 10^{-8}, 1.257162849, 1.004778997 \times 10^{-19}, 0.1926086478, 6.075860655 \times 10^{-7}]$$

```
> ExpGenLotka(5, 50);
```

The Equilibrium points are

The stable Equilibrium points are
 $\{(0, 0, 0, 0, 4.545454545), [0, 0, 29.26053538, 26.14630268, -35.18420355], [0, 0.9498787389, 0, 0.5658852061, 0], [8.333333333, 0, 0, 0, 0]\}$
 at time $t = 50$, with initial conditions $\{0.5, 0.5, 0.5, 0.5, 0.5\}$, the ultimate behavior is
 $[0.0004460774143, 0.9628053222, 3.187412202 \times 10^{-19}, 0.5651784626, 0.0005637439567]$

and with initial conditions, [0.1, 0.1, 0.1, 0.1, 0.1]

$$[8.183690977, 0.01334524793, 4.800455113 \times 10^{-93}, 1.254910225 \times 10^{-62}, 1.062510807 \times 10^{-2}, \\ \text{and with initial conditions, } \left[\frac{1}{5}, \frac{2}{5}, \frac{3}{5}, \frac{4}{5}, 1 \right]]$$

[0.00006737444388, 1.010921031, 2.069247826 $\times 10^{-21}$, 0.5639022519, 0.00022308928]

```
> ExpGenLotka(5, 50);
```

The Equilibrium points are

The stable Equilibrium points are $\{(0.3275360098, 0.2790760037, 0, 0, 0.4160281949)\}$ at time $t=100$, with initial conditions, $\{0.1, 0.5, 0.5, 0.5, 0.5\}$; the ultimate behavior is $\{0.2154799200, 0.3385904462, 0.2244238491, 0.04907994846, 0.2700241110\}$ and with initial conditions, $\{0.1, 0.1, 0.1, 0.1, 0.1\}$ and $\{0.2439807495, 0.1443315741, 0.07885314336, 0.2567546569, 0.2183838065\}$ and initial conditions, $\left[\begin{array}{ccccc} 1 & 2 & 3 & 4 & 1 \\ 5 & 5 & 5 & 5 & 1 \end{array}\right]$ all survived \Rightarrow NO agreement \Rightarrow = agreement between

S. S. S. 15 (52)

$\{ -0.3597769383, 0, 0, -0.7910095741, 1.184265755, [-0.2177639337, 0.3575408934, 0, -0.0497291323, 0.7168062818], [-0.189759586, 0.3799673201, 0.0825651504, -0.06926151321, 0.6452546513], [-0.1425201494, 0.3366424219, 0, 0.6290544525], [-0.1032958850, 0, 1.108692205, -1.676746448, 0.6171886727], [-0.06563900260, 0.3556323794, 0.1102761578, 0.48475435359], [0, 0, -1.560121766, 1.141552511], [0, 0, 0, 0], [0, 0, 0, 0.5376344086], [0, 0, 0, 8.333333333], [0, 0, 0, 0.4381161008, 0, 0.2738225630], [0, 0, 0.5208333333, 0, 0], [0, 0, 1.248112286, -1.941014480, 0.5374433686], [0, 0, 3.104575163, -5.637254902, 0], [0, 0.3642441315, 0, 0, 0.4929577463], [0, 0.3617387179, 0.1237243454, 0, 0.1646577639], [0, 0.4595830045, 0, -0.210481452, 0.5623250126], [0, 0.4727271463, 0.1166662963, -0.2142396827, 0.4893181745], [0, 0.5077030812, 0.140056224, 0, 0], [0, 0.5208333333, 0, 0, 0], [0, 1.086418675, 0.1222493888, -0.980138165, 0], [0, 1.196172687, 0, -0.1020408163, 0], [0, 0.00940625872, 0.1812361829, 0.1836125035, 0], [0, 0.2143501805, 0, 0.282227377, -0.54690433, 0], [0, 0.2587694077, 0.4336785392, 0.1820969906, 0, 0], [0.2941174706, 0, 0, 0.303709810, 0, 0, 0.20610577], [0, 0.40395756, 0.4998837167, 0, 0], [0.510240816, 0, 0, 0.15486846, 0, 0.3785614796, 0, 0], [0, 0.9024606782]\}$

The stable Equilibrium points are
 $\{(0, 0, 0, 8.333333333, 0, 0, 0.4727271463, 0.1166662963, -0.2142396827, 0.4893181745)\}$
at time $t = 50$, with initial conditions, $[0.5, 0.5, 0.5, 0.5, 0.5]$, the ultimate behavior is
 $[0.01824017979, 1.581970019 \times 10^{-30}, 3.337602564 \times 10^{-74}, 8.22781183, 7.203933757 \times 10^{-10}]$
and with initial conditions, $[0.1, 0.1, 0.1, 0.1, 0.1]$
 $[0.01866365908, 3.067639236 \times 10^{-30}, 2.27982203 \times 10^{-72}, 8.271396782, 2.339506966 \times 10^{-10}]$
and with initial conditions, $\left[\frac{1}{5}, \frac{2}{5}, \frac{3}{5}, \frac{4}{5}, \frac{1}{5}\right]$

o survive

• # cases where all species survived -

times there was agreement w/ positive stable equ pts = 0

times there was agreement between 3 initial conditions = 0