

Homework for Lecture 10 of Dr. Z.'s Dynamical Models in Biology class

Email the answers (as .pdf file) to

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by 8:00pm Monday, Oct. 13, 2025.

Subject: hw8

with an attachment hw8FirstLast.pdf and/or hw8FirstLast.txt

Using

<http://sites.math.rutgers.edu/~zeilberg/Bio25/DMB10.txt>

1. Using procedure `ExactPD` find the probability of winning, and expected duration of the game in a Gambler's Ruin with max. capital 40 dollars, starting capital 20 dollars and prob. of winning a dollar at any one round $\frac{19}{40}$.

Now using `EstPD`, estimate it with (i) $K=100$, (ii) $K=1000$ (iii) $K=5000$ (Warning: this may take some time) Which of them gives the best estimate? Can you explain why?

2.

Plot `ForPD(n,100,p)[1]` from $p=0.45$ to $p=0.5$ for $n=10,20,30,40,50,60,70,80,90$.

1)

```
> ExactPD(20,40,19/40);
[0.1190277811, 304.7777751]
> EstPD(20,40,19/40,100);
[0.1100000000, 292.0600000]
> EstPD(20,40,19/40,1000);
[0.1310000000, 308.3000000]
> EstPD(20,40,19/40,5000);
[0.1234000000, 307.1728000]
```

(2) $K=5000$ gives the best estimate because
(3) more trials reduce sampling variability
(4)
(5)

2)

