

> # Max Mekhanikov - 11/5/21 attendance quiz

>

$F := [(1 - 6 \cdot x - y) \cdot (3 - x - y), (3 - 8 \cdot x - 3 \cdot y) \cdot (1 - 4 \cdot x - 6 \cdot y)]$
 $F := [(1 - 6x - y) (3 - x - y), (3 - 8x - 3y) (1 - 4x - 6y)]$

(1)

> *RandNice* := **proc**(*var*, *K*) **local** *ra*, *i* :

ra := *rand*(1 ..*K*) :

[*seq*((*ra*() - *add*(*ra*() * *var*[*i*], *i* = 1 ..*nops*(*var*))) * (*ra*() - *add*(*ra*() * *var*[*i*], *i* = 1 ..*nops*(*var*))), *i* = 1 ..*nops*(*var*))] :

end:

> *IsStable* := **proc**(*M*) **local** *EiI*, *i* :

EiI := *Eigenvalues*(*evalf*(*Matrix*(*M*))) :

evalb(*max*(*seq*(*coeff*(*EiI*[*i*], *I*, 0), *i* = 1 ..*nops*(*M*))) < 0) :

end:

> *StEquPts* := **proc**(*F*, *var*) **local** *d*, *pt*, *E*, *S*, *J*, *i*, *j*, *J0*, *iI*, *Ei0* :

d := *nops*(*var*) :

if *nops*(*F*) ≠ *d* **then**

RETURN(*FAIL*) :

fi:

E := *EquPts*(*F*, *var*) :

S := { } :

J := [*seq*([*seq*(*diff*(*F*[*i*], *var*[*j*]), *j* = 1 ..*d*), *i* = 1 ..*d*]] : #*J* is the general Jacobian

for *pt* **in** *E* **do**

J0 := *evalf*(*subs*({*seq*(*var*[*iI*] = *pt*[*iI*], *iI* = 1 ..*d*) }, *J*)) :

if *IsStable*(*J0*) **then**

S := *S* **union** {*pt*} :

fi:

od:

S :

end:

> *EquPts* := **proc**(*F*, *var*) **local** *sol*, *iI* :

if *nops*(*F*) ≠ *nops*(*var*) **then**

RETURN(*FAIL*) :

fi:

sol := {*solve*({*op*(*F*) }, {*op*(*var*) }) } :

{*seq*(*subs*(*sol*[*iI*], *var*), *iI* = 1 ..*nops*(*sol*)) } :

end:

> *F*

$[(1 - 6x - y) (3 - x - y), (3 - 8x - 3y) (1 - 4x - 6y)]$

(2)

> *EquPts*(*F*, [*x*, *y*])

$$\left\{ [0, 1], \left[-\frac{6}{5}, \frac{21}{5} \right], \left[\frac{5}{32}, \frac{1}{16} \right], \left[\frac{17}{2}, -\frac{11}{2} \right] \right\} \quad (3)$$

> *subs*({*x* = 0, *y* = 1}, *F*)

$$[0, 0] \quad (4)$$

> *StEquPts*(*F*, [*x*, *y*])

Error, (in StEquPts) cannot determine if this expression is true or false: max(Eigenvalues(Matrix(2, 2, {(1, 1) = -12., (1, 2) = -2., (2, 1) = 40., (2, 2) = 15.}))[1], Eigenvalues(Matrix(2, 2, {(1, 1) = -12., (1, 2) = -2., (2, 1) = 40., (2, 2) = 15.}))[2]) < 0

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