

**Math 300 Intro Math Reasoning**  
**Worksheet 03: Set Theory**

(0)  $A = \{1, 2, 3\}$ ,  $B = \{1, 1, 2, 3\}$ ,  $C = \{n \in \mathbb{N} \mid \exists y \in \mathbb{R}(|y| + |3 - n| \leq 3)\}$ ,  
 $D = \{\{1\}, \{1, 2\}, \{1, 2, 3\}\}$ ,  $E = \{1, \{1, 2, 3\}, 3\}$   $F = \{2^n - m \mid n \in \mathbb{N}, m \in \{0, 1\}\}$

No need to justify the following

- (1) How many elements are in each of the sets? (a number or  $\infty$ )
- (2) Determine if
  - (a)  $A = B$ .
  - (b)  $A \subseteq E$ .
  - (c)  $A \in E$ .
  - (d)  $A = C$ .
  - (e)  $A \subseteq C$
  - (f)  $E \subseteq D$ .
  - (g)  $A \subseteq F$
  - (h)  $C \subseteq F$

We define for every  $A \subseteq \mathbb{R}$  and  $r \in \mathbb{R}$

$$A + r = \{a + r \mid a \in A\}$$

(1) Compute (no proof):

- (1)  $\{1, 5\} + 0.5$ .
- (2)  $\mathbb{N} + 1$ .
- (3)  $\mathbb{Z} + 1$ .
- (4)  $\emptyset + r$ .

(2) Prove or disprove:

- (1) If  $A \subseteq B$  then  $A + r \subseteq B + r$ .
- (2) If for some  $r, s \in \mathbb{R}$ ,  $A + r \subseteq B + s$  then  $A \subseteq B$ .
- (3)  $A + 0 = A$

(3) Prove that for every  $r \in \mathbb{R}$ ,  $\mathbb{Q} + r = \mathbb{Q}$  if and only if  $r \in \mathbb{Q}$ .