

## Homework 2

MATH 300

(due Sep 20)

Sep 13, 2024

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**Problem 1.** Formalize each of the following statements using the predicate calculus (that is, find the predicate and write using the symbols of predicate calculus, and predicates  $p(x), q(x), \dots$ ).

- (a) Every real solution of  $x^2 - 5x + 6 = 0$  is positive.
- (b) Every prime number is greater than 1.

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**Problem 2.** For each of the following statements, write the negation of the sentences **without** the negation symbol “ $\neg$ ”, and prove the negation of (2):

1.  $\exists \epsilon((\epsilon > 0) \wedge (\forall x(x > 0 \Rightarrow x > \epsilon)))$ .

2.  $\forall x((x > 5) \Leftrightarrow (\forall y(y > -100)))$ .

(Hint: Recall that  $A \Leftrightarrow B \equiv (A \Rightarrow B) \wedge (B \Rightarrow A)$ )

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**Problem 3.** Prove the following statement:

If both  $a$  and  $b$  are divisible by  $n$ , then  $a - b$  is divisible by  $n$ .

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**Problem 4.** Prove the following implication:

If  $n$  is even then  $n + 2$  is even.