

## Homework 5

MATH 215

(due October 7)

September 30, 2022

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**Problem 1.** Compute the following sets. No proof required.

1.  $\{a + b : a \in \{0, 5\}, b \in \{2, 4\}\} \setminus \{7, 10\}$ .

2.  $(1, 3) \cup [2, 4)$

3.  $\mathbb{Z} \cap [0, \infty)$

4.  $\mathbb{N}_{\text{even}} \Delta \mathbb{N}_+$

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**Problem 2.** Suppose that  $A = \{1, 2, 3\}$ ,  $B = \{1, 1, 2, 3\}$ ,  $C = \{1, 3, \pi\}$ ,  $D = \{x \in \mathbb{Z} \mid x \notin \mathbb{N}\}$ ,  $E = \{1, \{1, 2, 3\}, 3\}$ .

1. Determine the truth and falsity of each of the following statements.

No proof required

- (a)  $A = B$ .
- (b)  $A = C$ .
- (c)  $A \subseteq E$ .
- (d)  $A \in E$ .
- (e)  $E \subseteq D$ .

2. List all the subsets of the set  $E$ .

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**Problem 3.** Let  $X$  and  $Y$  be sets.

- (i) Prove that  $Y \setminus (Y \setminus X) = X \cap Y$ .
- (ii) Prove that  $X \subseteq Y$  if and only if  $X \cup Y = Y$ .
- (iii) Deduce that  $X \subseteq Y$  if and only if  $Y \setminus (Y \setminus X) = X$ .

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**Problem 4.** Prove that for all sets  $A, X, Y$  we have

$$A \setminus (X \cap Y) = (A \setminus X) \cup (A \setminus Y).$$

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**Problem 5.** Prove that if  $A \cap B \subseteq C$  and  $x \in A \setminus C$ , then  $x \notin B$ .

[Hint: Prove it by contradiction.]