Problem. Find the dimensions $x$ and $y$ of the rectangle inscribed in a circle of radius 1 that maximizes the quantity $x y^{2}$. Hint: drawing a picture is a great first step, to see how $x$ and $y$ depend on each other.

