

Consider the function  $B$  defined by the rule  $B(x) = \int_1^x f(t) dt$  where  $f(t) = 6 - 2t$ .

1. Compute  $B(1)$  and  $B(2)$  exactly.
2. Use the first Fundamental Theorem of Calculus to find a formula for  $B(x)$  that does not involve integrals. That is, use the first FTC to evaluate  $\int_1^x (6 - 2t) dt$ .
3. Observe that  $f$  is a linear function; what kind of function is  $B$ ?
4. Using the formula that you found in part (b) that does not involve integrals, compute  $B'(x)$ .
5. While we have defined  $f$  by the rule  $f(t) = 6 - 2t$ , it is equivalent to say that  $f$  is given by the rule  $f(x) = 6 - 2x$ . What do you observe about the relationship between  $B$  and  $f$ ?