

1. Evaluate $\lim_{x \rightarrow 1} x$.

2. Why can't we evaluate

$$\lim_{x \rightarrow 1} \frac{x^2 - x}{x - 1}$$

by direct substitution? What do we get?

3. We want to try to compute this limit anyway. Factor the numerator. Since we are **not** looking at the value at $x = 1$, we can cancel a factor. What do we get now?

4. Define

$$f(x) = \begin{cases} \frac{x^2 - x}{x - 1} & x \neq 1 \\ a & x = 1 \end{cases}$$

What value should be assigned to a in to make f a continuous function on \mathbb{R} ?

5. Use the same factoring procedure to try to evaluate the following limits. Note that direct substitution always gives the same 'answer' initially.

$$\lim_{x \rightarrow 2} \frac{x^2 - 4}{(x - 2)^3} \quad \lim_{x \rightarrow 3} \frac{(x - 3)^2}{x^2 - 9} \quad \lim_{x \rightarrow -2} \frac{x^2 + 3x + 2}{x^2 + 4x + 4}$$

6. What does that say about problems where that same answer shows up by direct substitution?