

1. Let  $f(x) = \frac{3x+1}{x+\sqrt{4x^2+5}}$ .

- (a) Compute  $\lim_{x \rightarrow \infty} f(x)$ .
- (b) Compute  $\lim_{x \rightarrow -\infty} f(x)$ . [Warning:  $\sqrt{(-10)^2} = 10$ , not  $-10$ .]
- (c) Design a continuous function  $g(x)$  so that  $\lim_{x \rightarrow \infty} g(x) = -2$  and  $\lim_{x \rightarrow -\infty} g(x) = 0$ .
- (d) How many different horizontal asymptotes can a function have?