

Assume that  $f$  and  $g$  are odd functions defined for all real numbers.

1. What does it mean for a function  $f(x)$  to be odd?
2. Give an example of an odd function, and use the definition to show that it is odd.
3. Define a new function  $h(x) = f(x)g(x)$ . Use the definition to show that  $h$  is an even function.
4. Define another function  $k(x) = f(g(x)) = (f \circ g)(x)$ . Use the definition of an odd function to show that  $k$  is odd.

**Note:** For this problem, you should not put any examples in for  $f$  and  $g$  when you are trying to show that  $h$  is even and  $k$  is odd. You need to leave  $f$  and  $g$  as general (unknown) functions and use the fact that they are even/odd to get the result you want.