MATH 251: Quiz 6 April 9, 2015

Name: ______ Sec: _____

1. Let $\vec{F} = \langle yz, xz, xy \rangle$. Compute the integral

$$\int_{\mathcal{C}} \vec{F} \cdot ds$$

for the curve $C(t) = \langle 3t^2 + \cos(\pi t^3), 2^t, t^4 + t^3 - t + 1 \rangle$ for t = 0 to 1. Hint: Is \vec{F} conservative?

2. Determine whether or not the following vector fields are conservative. If they are conservative, find a potential function.

(a)
$$\vec{F} = \langle y^2, x^2, \sin(z) \rangle$$
.

(b) $\vec{G} = \langle 3x^2 + \sin(z), 2yz, y^2 + x\cos(z) \rangle.$

3. Let f(x, y, z) = 9z + 2x and let C be the curve $c(t) = \langle t, t^2, t^3 \rangle$ for t = 0 to 1. Compute

$$\int_{\mathcal{C}} f(x, y, z) \, ds.$$