

# MATH 251: Quiz 1

May 28, 2015

Name: \_\_\_\_\_

1. Let  $\vec{v} = \langle 2, -1, 2 \rangle$  and  $\vec{w} = \langle -1, 3, 2 \rangle$ . Compute

(a)  $3\vec{v} + 2\vec{w}$ .

(b)  $\vec{v} \cdot \vec{w}$ .

(c)  $\vec{v} \times \vec{w}$ .

2. Find the angle between the vectors  $\langle 1, 1, -1 \rangle$  and  $\langle 0, 1, 2 \rangle$  as an inverse cosine. Is this angle acute or obtuse?

3. Let  $\vec{u} = \langle 2, 3, -2 \rangle$  and  $\vec{v} = \langle 1, 1, 1 \rangle$ . Decompose  $\vec{u}$  into  $u_{//} + u_{\perp}$  with respect to  $\vec{v}$ .

4. Find a vector  $\vec{v}$  that is perpendicular to both  $\langle 2, 1, 4 \rangle$  and  $\langle -2, 6, 1 \rangle$ .

**Possibly Helpful Formulas:**

If  $v = \langle a_1, a_2, a_3 \rangle$  and  $\vec{w} = \langle b_1, b_2, b_3 \rangle$ , then

$$\vec{v} \cdot \vec{w} = a_1b_1 + a_2b_2 + a_3b_3 = \|\vec{v}\| \|\vec{w}\| \cos(\theta)$$

$$\vec{v} \times \vec{w} = \langle a_2b_3 - a_3b_2, a_3b_1 - a_1b_3, a_1b_2 - a_2b_1 \rangle$$

$$\vec{v}_{//} = \left( \frac{\vec{v} \cdot \vec{w}}{\vec{w} \cdot \vec{w}} \right) \vec{w} \quad \text{and} \quad \vec{v}_{\perp} = \vec{v} - \vec{v}_{//}$$

for decomposing  $\vec{v}$  into components parallel and perpendicular to  $\vec{w}$ .

How's my teaching so far? I know it's only been 3 days, but just to get some feedback

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|-----------------------------|----------|---|---|---|---|---|----------|
| • Pace of material          | Too slow | 1 | 2 | 3 | 4 | 5 | Too Fast |
| • Pace/Clarity of speaking  | Too slow | 1 | 2 | 3 | 4 | 5 | Too Fast |
| • Legibility of handwriting | Bad      | 1 | 2 | 3 | 4 | 5 | Good     |
| • Any other comments?       |          |   |   |   |   |   |          |