

HOMEWORK #2

Solutions
Math 1011
28 July, 2014

Chapter 13 (p234)

[1] (a) False. Probability 1000% is impossible because probabilities must be between 0% and 100%.

(b) True. On average, out of every 10 trials the event in question will happen 9 times and its opposite will happen once.

[3] Option (ii) is better. With option (ii) you win a dollar every time you would have won one in option (i), plus in other situations too. (For example, if you draw $\diamond \heartsuit \spadesuit \clubsuit$.)

[9] (a) The chance of getting one $\boxed{1}$ is $\frac{1}{6}$ for each roll. The rolls are independent so we use the multiplication rule to get

$$\frac{1}{6} \cdot \frac{1}{6} \cdot \dots \cdot \frac{1}{6} = \left[\left(\frac{1}{6} \right)^{10} \approx 1.65 \times 10^{-8} \right]$$

(b) This is the opposite of part (a), so the answer is

$$\left[1 - \left(\frac{1}{6} \right)^{10} \approx 0.9999998346 = 99.999998346\% \right]$$

(c) Not the same as part (b). The chance of rolling 5 or less for each die is $\frac{5}{6}$, so use mult rule:

$$\frac{5}{6} \cdot \dots \cdot \frac{5}{6} = \left[\left(\frac{5}{6} \right)^{10} \approx 16.1506\% \right]$$

(1)

Chapter 14 (p 252)

[1] (a) Only one way to get this out of 36.
 $\boxed{1/36}$

(b) Six ways to get this out of 36.
 $\boxed{\frac{6}{36} = 1/6}$

[3] (a) False. These events are not mutually exclusive so you cannot use the addition rule.
(actual chance would be $1 - (\frac{5}{6})^3$)

(b) False. Clearly you might get tails each time.

[7] In a single draw the chance of getting [2] is $2/5$. We will compute the chance of the opposite. To not get [2] 4 times the chance would be

$$\frac{3}{5} \cdot \frac{3}{5} \cdot \frac{3}{5} \cdot \frac{3}{5} = \frac{81}{625}$$

Thus the chance of getting [2] at least once is

$$\boxed{1 - \frac{81}{625} = \frac{544}{625} = 87.04\%}$$

$$\boxed{2} \mid \boxed{\text{(iii)} \left(\frac{5}{6}\right)^{10}}$$

The chance of it not landing on a $\begin{smallmatrix} \square \\ \vdots \\ \square \end{smallmatrix}$ in a single roll is $\frac{5}{6}$. Use the multiplication rule.

$\boxed{6}$ False. The lists are the same length. Pick 6 out of 8 for a committee is the same as picking 2 out of 8 to not be in the committee.

Also, you can compute

$$\left(\begin{array}{l} \frac{8!}{6! (8-6)!} = \frac{8!}{6! 2!} \\ \frac{8!}{2! (8-2)!} = \frac{8!}{2! 6!} \end{array} \right) \begin{array}{l} \nearrow \\ \searrow \end{array} \text{equal.}$$

