QUIZ 7 FOR CALC 4

(1) (3 pt) Find the largest open intervals for the following differential equation where you are guaranteed to have a solution

 $\sin 2t \ y^{(4)}(t) + \tan t \ y(t) = t, \\ y(\frac{\pi}{4}) = 0, \\ y'(\frac{\pi}{4}) = 1, \\ y''(\frac{\pi}{4}) = 0, \\ y'''(\frac{\pi}{4}) = -1$

(2) (3 pt) Find the general solution of the equation

$$y''(t) - 4y'(t) + 4y(t) = \frac{e^{2t}}{1+t^2}$$

(3) (2 pt) What is the integrating factor of the first order differential equation

$$y'(t) + p(t)y(t) = g(t)?$$

and what is the general solution?