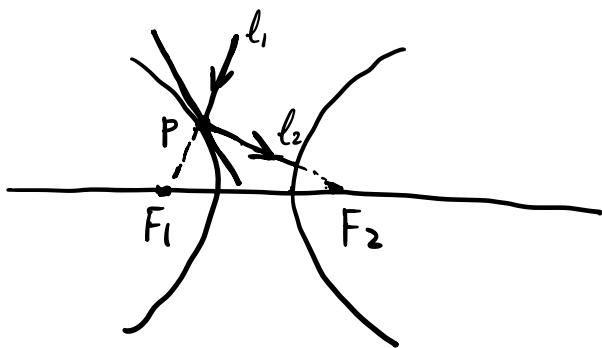
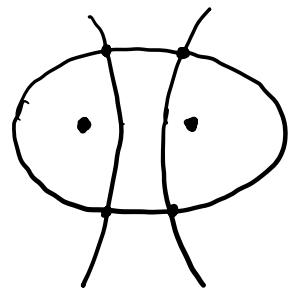


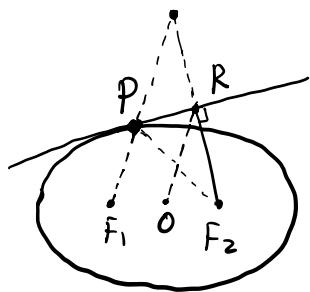
1. Give a description of tangents to hyperbola. Then use this to show that if the ray  $l_1$  passes through  $F_1$  (after extension), then its reflection  $l_2$  passes through  $F_2$



2. Guess a nice property of tangents to two confocal conics (i.e. an ellipse and a hyperbola with the same foci) at the intersection points and prove it.



3. Prove that the orthogonal projection  $R$  of a focus  $F$  onto a tangent of an ellipse lie on the circle with center  $O$  and radius  $a$ : (Hint: Prove  $|OR| = a = \frac{|F_1P| + |F_2P|}{2}$ )



4. Classify the following conic curves.

Find their centers and axes.

$$(i) 11x^2 + 6xy + 3y^2 - 12x - 12y - 12 = 0$$

$$(ii) x^2 - 2xy + y^2 - 10x - 6y + 25 = 0$$

5.2.1 - 5.2.2:

Use just straightedge to Create a perspective view of the plane filled with congruent hexagons.

See below for a sample:

