

**Difficulty guide for worksheet:***C-level or B-level exam problem:* 1, 2*A-level exam problem or challenge for extra study:* 3*beyond the scope and/or removed from syllabus:* none

- For each part, describe, in English, the set of points satisfied by the given equation in the indicated coordinate system. You should give a complete, concise, and clear English description; a graph and/or equation in rectangular coordinates is helpful but not sufficient.
 

(a) $\rho = 4y$ (spherical) (b) $\varphi = \frac{\pi}{4}$ (spherical) (c) $r = 5$ (cylindrical)	(d) $r = 2 \sec(\theta)$ (polar) (e) $z = r^2$ (cylindrical) (f) $r^2 + z^2 = 16$ (cylindrical)
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- For each part, describe the given set of points with an equation of the form  $z = f(r, \theta)$  for cylindrical coordinates or  $\rho = f(\theta, \varphi)$  for spherical coordinates.
  - the surface  $z = 3xy$  (cylindrical)
  - the sphere centered at the origin with radius 3 (spherical)
  - the sphere centered at the origin with radius 3 (cylindrical)
  - the cylinder  $y^2 + z^2 = 4$  (cylindrical)
  - the upper part of the cone  $x^2 + y^2 = z^2$  (cylindrical)
  - the plane  $z = 5$  (spherical)
- Find equations  $r = f(\theta, z)$  (cylindrical) and  $\rho = f(\theta, \varphi)$  (spherical) for the hyperboloid  $x^2 + y^2 = z^2 + 1$ . Do there exist points on the hyperboloid with  $\varphi = 0$  or  $\varphi = \pi$ ? Which values of  $\varphi$  occur for points on the hyperboloid? (A graph of the hyperboloid may help explain what is happening.)