

Difficulty guide for worksheet:

C-level or B-level exam problem: 1, 3, 4, 5, 6

A-level exam problem or challenge for extra study: 2

beyond the scope and/or removed from syllabus: none

1. Calculate all first derivatives for each function f .

(a) $f(x, y) = \cos\left(\frac{y}{x+y}\right)$

(c) $f(x, y, z) = ze^{xz-x^2z^3}$

(b) $f(u, v) = \ln(u^2 + uv)$

(d) $f(s, t) = \tan^{-1}(st^2)$

2. Calculate f_{xyxzy} for the following function.

$$f(x, y, z) = y \sin(xz) \sin(x+z) + (x+z^2) \tan(y) + x \tan\left(\frac{z+z^{-1}}{y-y^{-1}}\right)$$

3. Prove that there is no function f such that $f_x = xy^2$ and $f_y = -x^2y$.

4. Find an equation of the plane tangent to the graph of f at the indicated point.

(a) $f(x, y) = 3x^2y - x^3y^2$ at $(-1, 1)$

(b) $f(x, y) = ye^{x/y}$ at $(\ln(2), 2)$

5. Use a linear approximation to estimate the value of $\sqrt{\frac{9.2}{3.9}}$.

6. Let $f(x, y) = 3x^2 - xy - y^2 - 18x$. Find all points on the graph of f where the tangent plane is parallel to the indicated plane.

(a) the xy -plane

(b) the plane $2x - 5y + 2z = 1$