Calculus 251:C3

Quiz #11 - 6/15/2020

Topic: Section 14.8

Instructions. Answer the questions in the spaces provided or on your own paper, then scan and upload to Canvas. Show and label all of your work. Responses with no work may receive no credit even if the answer is correct.

10 pts

(1) Find the minimum and maximum values of the function f(x,y) = 2xy subject to the constraint  $2x^2 + 3y^2 = 12$ , and indicate the points at which these values occur. You must use the method of Lagrange multipliers to earn any credit on this quiz.

$$\nabla f = \langle 2_{\gamma}, 2_{\times} \rangle$$

$$g(x,y) = 2x^2+3y^2-12$$
  
 $\nabla g = \langle 4x, 6y \rangle$ 

$$\nabla f = \lambda \nabla g$$

$$0 2y = 4\lambda x \implies 3y^2 = 6\lambda x$$

$$\begin{array}{ccc}
0 & 2y = 4\lambda x & \Rightarrow 3y^2 = 6\lambda xy \\
\hline
2 & 2x = 6\lambda y & \Rightarrow 2x^2 = 6\lambda xy
\end{array}$$

$$2x^2 = 3y^2$$

$$2x^2 = 3y^2$$

⇒ 
$$2x^{2}+2x^{2}=|2$$
  
 $x^{2}=3$   
 $x = \pm \sqrt{3}$   
 $y = \pm \sqrt{2}$ 

$$\begin{array}{c|c}
\text{Candidate point} & f(x,y) \\
\hline
(\sqrt{3}, \sqrt{2}) & 2\sqrt{6} \\
(-\sqrt{3}, \sqrt{2}) & -2\sqrt{6} \\
(\sqrt{3}, -\sqrt{2}) & -2\sqrt{6} \\
(-\sqrt{3}, -\sqrt{2}) & 2\sqrt{6}
\end{array}$$

Max of 
$$2\sqrt{6}$$
 at  $(\sqrt{3}, \sqrt{2})$  and  $(-\sqrt{3}, -\sqrt{2})$   
Min of  $-2\sqrt{6}$  at  $(-\sqrt{3}, \sqrt{2})$  and  $(\sqrt{3}, -\sqrt{2})$