# Oral Qualifying Exam Syllabus Lara Pudwell 

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Committee: J. Beck, D. Maclagan, V. Retakh, D. Zeilberger (chair)

## Combinatorics and Experimental Mathematics

- Basic Enumeration: counting arguments, generating functions, recurrence relations, inclusion-exclusion, pigeonhole principle, Stirling numbers, Bell numbers, Catalan numbers, Eulerian numbers
- Permutations and Tableaux: Descents, Cauchy's Convolution Formula, Major index, Inversions, Applications of Inversions to Determinants and Graphs, Inversions in Multiset Permutations, Gaussian coefficients, the Füredi-Hajnal Conjecture, the Marcus-Tardos Theorem (Stanley-Wilf Conjecture), notion of pattern avoidance and results for patterns of length 3 and 4, Robinson-Schensted-Knuth Correspondence, Standard Young Tableaux, the Hook Length Formula, generating trees, posets on $S_{n}$, Bruhat order, weak Bruhat order, posets on pattern avoiding permutations, simplicial complexes of restricted permutations
- Ramsey Theory: Ramsey's Theorem, probabilistic lower bounds, van der Waerden numbers, $R(3, n)$ upper and lower bounds
- Experimental Math: Maple programming, Golay code, gambler's ruin, Gaussian Quadrature, sorting algorithms, Gray code, Cassini identities, Prüfer bijection
- Hypergeometric functions and identities: definition and representation, Sister Celine's Algorithm, The Fundamental Theorem of Hypergeometric Series, Gosper's Algorithm, similarity among hypergeometric terms, existence of telescoped recurrences, Zeilberger's Algorithm, the WZ method and dual identities.


## Combinatorial Commutative Algebra

- Monomial ideals: degree, Hilbert function, Hilbert polynomial, radical, prime, irreducible, primary, primary decomposition
- Gröbner bases: monomial orderings, division algorithm, Dickson's lemma, Hilbert basis theorem, Buchberger's algorithm, Gröbner bases, minimal Gröbner bases, reduced Gröbner bases, properties of/applications of Gröbner bases, syzygies, improvements to Buchberger's algorithm, Hilbert Syzygy Theorem, Schreyer's algorithm for computing free resolutions
- Other: Macaulay's Theorem, Kruskal-Katona Theorem, Clements-Lindstrom Theorem

