

**Week 6**      Simple Algebras and the Brauer Group  
Jacobson II: 4.6, 4.7, 5.3

1. Jacobson II 4.6.1
2. Jacobson II 4.6.9
3. Jacobson II 5.3.1
4. Suppose that  $R$  is a semisimple algebra over a field  $K$ . Let  $L$  be a field containing  $K$ . Suppose that  $V, W$  are left  $R$ -modules which are finite dimensional vector spaces over  $K$ . Show that if  $V \otimes_K L$  and  $W \otimes_K L$  are isomorphic as  $R \otimes_K L$  modules, then  $V$  and  $W$  are isomorphic as  $R$  modules. (Hint: Consider the character of the modules involved and show that  $\chi_V(r) = \chi_{V \otimes L}(r \otimes 1)$  .) See Jacobson II exercise 5.3.3 for a generalization.