

Turn in starred problems, and only starred problems, Wednesday 09/17/2014.

**Multiple-page homework must be STAPLED when handed in.**

Section 4.3:

- 1 (a), (b), (c), (g), \*(n), \*(o)
- 2
- 6 (a), \*(h), \*(j), \*(p)

**Hints and remarks:** 1. Problem 1(n) may look a bit confusing as written, but just carry out one differentiation, using the product rule, before beginning:

$$[x^3(x-1)y']' = x^3(x-1)y'' + \dots$$

2. Problem 6(h) is very simple: it is an *Euler*, or *Cauchy-Euler*, or *equidimensional*, equation. I mentioned this type of equation in class on Monday 9/08; you can also read about it in Section 3.6.1. **You don't need to introduce a series to solve the equation; see class notes or Section 3.6.1.** (However, if you are so inclined it may be instructional to do so and see what happens.)

3. In solving problems 6(j) and 6(p) you should find that the roots  $r_1, r_2$  of the indicial equation do *not* differ by an integer, so the two independent solutions will have the forms  $y_1 = x^{r_1} \sum_n a_n x^n$  and  $y_2 = x^{r_2} \sum_n b_n x^n$ .

4. For problem 6(p) you will not be able to find the general recursion relation, due to the difficulty in carrying out the multiplication of series involved in the term  $e^x y'$ . Instead, just work with a few terms of the series, without using sigma notation. Find four non-zero terms of each of the two solutions, that is, if the solution is  $y(x) = x^r(a_0 + a_1x + a_2x^2 + a_3x^3 + \dots)$  find  $a_1$ ,  $a_2$ , and  $a_3$  in terms of  $a_0$ .