More Practice for Exam 2

- 1. If $g(x) = \ln(3x^4 + 5x)$, find g'(x).
- 2. Find the slope of the tangent line to the curve $x^3 + y^3 \frac{9}{2}xy = 0$ at (2,1).

3. Find the intervals where the function $f(x) = \frac{x-1}{x^2+3}$ is increasing and decreasing. Find all horizontal and vertical asymptotes of this function.

- 4. Find $\lim_{x \to 0} \frac{1 \cos x}{\sec x}$.
- 5. Let $f(x) = \sqrt{2 + 7x^3}$.
 - a. Compute f(1).
 - b. Compute f'(1).
 - c. Using the differential or tangent line approximation, find an approximate value for f(1.08).
- 6. Find $\lim_{x \to 0^+} \sin x \ln x$.
- 7. Find the absolute extrema of $f(x) = x^{2/3}(5-2x)$ on the interval [-1, 2].

8. A farmer wishes to fence in a rectangular field containing an area of 600 square meters. If the field has a fence down the middle parallel to one side, what is the smallest amount of fencing that he can use?

See next page.

9. A person 6 ft tall stands 10 ft from point P directly beneath a lantern hanging 30 ft above the ground, as shown in the figure below. The lantern starts to fall, causing the person's shadow to lengthen. Given that the lantern falls $16t^2$ ft in t seconds, how fast will the shadow be lengthening when t = 1?

