

Prob. 81, Sec. 6.1

Denote the acceleration as  $a(t)$ , the velocity as  $v(t)$ , the distance as  $d(t)$ .  
 $a(t) = k$  ( $k$  a number, a constant - this is given)

$$v'(t) = a(t)$$
$$v(0) = 0 \text{ initial velocity is } 0.$$

Thus  $v(t)$  is of the form  $\int k dt = kt + C$ .  $v(0) = 0$ , means  $k \cdot 0 + C = 0$ ,  $C = 0$ . This gives us the velocity,  $v(t) = kt$ .

$$d'(t) = v(t)$$
$$d(0) = 0 \text{ initial distance is } 0.$$

Thus  $d(t)$  is of the form  $\int kt dt = kt^2/2 + C$ .  $d(0) = 0$ , means  $k \cdot 0^2/2 + C = 0$ ,  $C = 0$ . This gives us the distance,  $d(t) = kt^2/2$ .

Finally, denote  $T$  the take-off time. Then  $240 = kT = v(T)$ , and  $800 = kT^2/2 = d(T)$ . The former gives  $T = 240/k$ , and the latter

$$800 = k \left( \frac{240}{k} \right)^2.$$

Simplify,  $800 = 57600/k$ , and  $k = 72 \text{ ft/sec}^2$ .