Quiz # 10 for Dr. Z.'s Number Theory Course for Dec. 5, 2013

NAME: (print!) _____

E-MAIL ADDRESS: (print!)

1. An *extremely distinct* partition of n is a sequence of integers

$$(\lambda_1, \lambda_2, \ldots, \lambda_t)$$
,

such that

$$\lambda_1 + \lambda_2 + \ldots + \lambda_t = n \quad ,$$

and

$$\lambda_1 - \lambda_2 \ge 2$$
 $\lambda_2 - \lambda_3 \ge 2$,..., $\lambda_{t-1} - \lambda_t \ge 2$

and

$$\lambda_t > 0$$
 ,

Let q(n) be the number of partitions of n, and q(n, k) be the number of exteremely distinct partitions of n whose largest part is k.

(i) (5 points) Explain why

$$q(n,k) = \sum_{r=1}^{k-2} q(n-k,r)$$
,

and, of course

$$q(n,n) = 1 \quad .$$

(ii) Use the above recurrence, and

$$q(n) = \sum_{k=1}^{n} q(n,k)$$

to compute q(n) for $1 \le n \le 5$.