

Attendance Quiz # 22 for Dr. Z.'s Number Theory Course for Nov. 21, 2013

NAME: (print!) \_\_\_\_\_

E-MAIL ADDRESS: (print!) \_\_\_\_\_

1. Write down the generating function for the sequence, let's call it  $a(n)$ , for the number of partitions of  $n$  where each part shows up at most three times and whose largest part is  $\leq 5$ . Use it to find  $a(i)$  for all  $1 \leq i \leq 4$ .

2. i. Apply Glashier's bijection (in the odd- $\downarrow$ distinct direction) to the odd partition  $(7, 5, 5, 3, 3, 3, 1, 1, 1)$  to get a distinct partition, call it  $\lambda$

ii. Apply Glashier's bijection (in the distinct- $\downarrow$ odd direction) to the partition  $\lambda$  and show that you get  $(7, 5, 5, 3, 3, 3, 1, 1, 1)$  back.