

Solutions to Attendance Quiz # 1 for Dr. Z.'s Number Theory Course for Sept. 5, 2013

1. Using *unary* (no credit for other methods!), compute

$$1111 \times 111$$

**Sol. to 1:**  $1111 \ 1111 \ 1111 = 111111111111$ .

2. Write the integers 0 through 4 in von-Neumann notation

**Sol. to 2.:**

$$0 := \{ \} \ ,$$

$$1 := \{ \{ \} \} \ ,$$

$$2 := \{ \{ \}, \{ \{ \} \} \} \ ,$$

$$3 := \{ \{ \}, \{ \{ \} \}, \{ \{ \}, \{ \{ \} \} \} \} \ ,$$

$$4 := \{ \{ \}, \{ \{ \} \}, \{ \{ \}, \{ \{ \} \} \}, \{ \{ \}, \{ \{ \} \}, \{ \{ \}, \{ \{ \} \} \} \} \} \ .$$

3. List some **natural** members of Frege's class representing three .

**Sol. to 3:** There (infinitely) many possibilities.  $\{-1, 0, 1\}$ ,  $\{A, B, C\}$  are two of them.