PUBLICATIONS OF DORON ZEILBERGER

Last Update: May 4, 2005

This list, as well as most of the papers published after 1990, are available at http://www.math.rutgers.edu/~zeil

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Ph.D. Thesis

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